

CSE-301 Computer Graphics

Final Exam

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SUBJECT	CG
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Question #1 (15 Marks)

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- a. What is 'Eight Way Symmetry' of a circle?
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ANS

The most important thing in drawing a circle is learning how the circle is drawn using 8-way symmetry. It is based on mirror reflection.

If we see right hand in the mirror we will see left hand, similarly if we see pixel (x,y) in mirror we will see $(x, -y)$, so point $p1 (x, y)$ will become $p2 (x, -y)$ after reflection.

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- b. Write the 8 coordinates for representing 8-way symmetry in terms of (x, y) .

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ANS B

Any circle following 8-way symmetry. This means that for every point (x, y) 8 points can be plotted.

these (x, y) , (y,x) , $(-y, x)$, $(-x, y)$, $(-x, -y)$, $(y, -x)$, $(x, -y)$

for any point $(x + a, y + b)$, points $(x - a, y - b)$ and $(y + a, x + b)$ also lie on the same circle. So it is sufficient to compute only 1/8 of a circle, and all the other

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- c. How does it help minimize the calculations?

ANS

$$X_1 = 1 \quad x_2 = 3$$

$$Y_1 = 1 \quad y_2 = 3$$

$$\hat{x} = 4$$

$$\hat{y} = 2$$

The initial decision parameter and the minimum calculation has the value.

$$P_k = 2^y - x$$
$$= 4 - 4 = 0$$

Question #2 (10 Mark)

- a. What happens if Refresh Rate of a display is too slow? Explain.
-

ANS . A

Typically a refresh rate of less than 60Hz will produce noticeable flicker , meaning you can tell the being redrawn instead of seeing a constant image .

if the refresh rate is too show , this flicker can be hard on your eyes and may cause them to tire quickly.

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- b. What happens if Refresh Rate of a display is too fast? Explain.
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ANS . B

If you specify a refresh rate that is too high for your monitser . your screen may become unsable and your hardware may be damage , also note , some monitors shiver at higher rates and some of the higher resolutions and color depdth may be unavabile at the higher frequancies . in my older monitor . it displayed resoulation from 60hz to 200 Hz .

Question #3 (10 Marks)

For plotting a line between two points, we can use algorithms such as

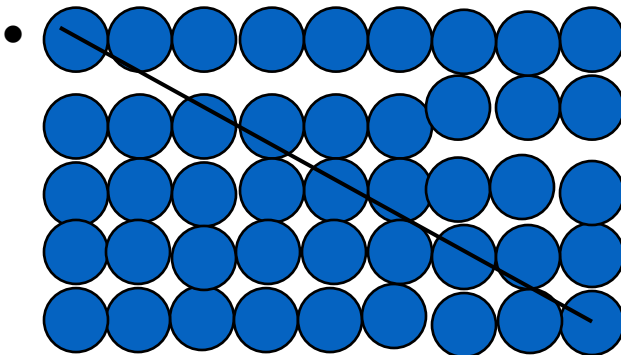
ANS

➤ Incremental Line Algorithm

learning algorithms inherently support incremental learning.
Other algorithms can be adapted to facilitate incremental learning.
Examples of incremental algorithms

- have got a pixel on the line (Current Pixel).
- How do I get the next pixel on the line?
- Compute one point based on the previous point:

➤ $(X_0, y_0) \dots\dots\dots (X_k, y_k) \text{ -----} == (X_{k+1}, y_{k+1}) \dots\dots$



Next pixel on next column
(when slope is small)

- Next pixel on next row
- (when slope is large

➤ Incremental Line Algorithm

➤ This algorithm exploits simple line equation

➤ $y = m x + b$

➤ where $m = dy / dx$

➤ and $b = y - m x$

➤ Now if $|m| < 1$

- Then $x = x + 1$
- Whereas $y = m x + b$
- why to check $|m|$
- Suppose a line has points
- p1 (10, 10) - p2 (20, 18)
- $dy = y_2 - y_1 = 18 - 10 = 8$
- $dx = x_2 - x_1 = 20 - 10 = 10$
- This means that there will be 10 pixels on the line in which for x-axis there will be distance of 1 between each pixel and for y-axis the distance will be 0.8.
- Now consider the reverse case
- Suppose a line has points
- p1 (10, 10) , p2 (16, 20)
- $dy = y_2 - y_1 = 20 - 10 = 10$
- $dx = x_2 - x_1 = 16 - 10 = 6$
- This means that there will be 10 pixels on the line in which for x-axis there will be distance of 0.6 between each pixel and for y-axis the distance will be

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➤ **Incrementing along x**

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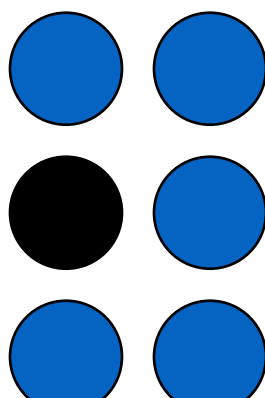
Current

Pixel

(x_k, y_k) 

(5,2)

(6,3)



6,2)

(6,1

➤ DDA Algorithm

• Digital differential analyzer (graphics algorithm)

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In its simplest implementation for linear cases such as lines, the DDA algorithm interpolates values in interval by computing for each x_i the equations

DDA may refer to: Dda (DNA-dependent ATPase), a DNA helicase Delhi Development Authority, the planning agency for Delhi, India Demand deposit account

DDA abbreviated for digital differential analyzer has a very simple technique.

Find difference, dx and dy as:

$$dy = y_2 - y_1$$

$$dx = x_2 - x_1$$

if $|dx| > |dy|$ then

$$\text{step} = |dx|$$

else

$$\text{step} = |dy|$$

Now very simple to say that step is the total number of pixels required for a line.

Next step is to find xIncrement and yIncrement:

$$x\text{Increment} = dx/\text{step}$$

$$y\text{Increment} = dy/\text{step}$$

Next a loop is required that will run 'step' times.

In the loop drawPixel and add xIncrement to x1 and yIncrement to y1.

Now sum-up all above in the algorithm:

DDA_Line (Point p1, Point p2)

dx = p2.x - p1.x

dy = p2.y - p1.y

x1=p1.x

y1=p1.y

if $|dx| > |dy|$ then step = $|dx|$

else

 step = $|dy|$

xIncrement = dx/step

yIncrement = dy/step

for counter = 1 to step

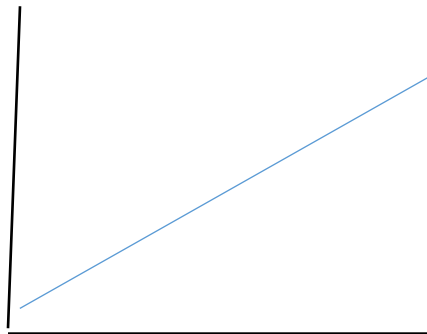
 drawPixel (x1, y1)

 x1 = x1 + xIncrement

 y1 = y1 + yIncrement

➤ Midpoint Algorithm

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$$f(x, y) = 0$$

Midpoint below line

Midpoint circle algorithm

midpoint circle algorithm is an algorithm used to determine the points needed for rasterizing a circle. Bresenham's circle algorithm is derived from the

➤ Bresenham's Algorithm

- The Bresenham algorithm is another incremental scan conversion algorithm
 - The big advantage of this algorithm is that it uses only integer calculations
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Bresenham Line Drawing Algorithm

Bresenham's algorithm finds the closest integer coordinates to the actual line, using only integer math. Assuming that the slope is positive and less than 1, moving 1 step in the x direction, y either stays the same, or increases by 1. A decision function is required to resolve this choice

. List of algorithms

imaginary line over the image Warnock algorithm Line Drawing: graphical algorithm for approximating a line segment on discrete graphical media. Bresenham's line

Timeline of algorithms

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Ford–Fulkerson algorithm developed by L. R. Ford, Jr. and D. R. Fulkerson 1962 – Bresenham's line algorithm developed by Jack E. Bresenham 1962 – Gale–Shapley

Question 3 Ans (A)

(1) Bresenham line drawing algorithm

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Bresenham algorithm finds the closest integer coordinates to the actual line, using only integer math. Assuming that the slope is positive and less than 1, moving 1 step in the x direction, y either stays the same or increases by 1. A decision function is required to resolve this choice.

Move across the x axis in unit intervals and at each step choose between two different y coordinates.

For example from the position (2, 3) we have to choose between (3, 3) and (3, 4) we would like the point that is closer to the original line at sample position $x_k + 1$ the vertical mathematical line are labeled upper and lower

The y coordinate on the mathematical line at $x_k + 1$ is

$$Y = M(x_k + 1) + b$$

1. input the two line and point, storing the left end point in (x1, y1) and plot this point.

2. calculate the constants x_{dx} and y_{dy} $2dy$ and $2dx$ get the first value for the decision parameter as $e = 2^y - x$

It produces all the sequence a line goes through pixels. The long measurement is among for every pixel. and with the fragmenter incline is collected.

Question 3 (b)

Drawback of Bresenham line drawing algorithm these are the drawbacks of incremental line algorithm. Though it improves the accuracy of generated points but still the resulted line is not smooth.

Drawbacked of DDA algorithm

The disadvantage of DDA algorithm are there is an extra overhead of using round off () function. Using round off () function increases time complexity of the algorithm. Resulted line are not smooth because of round off () function.

The points generated by this algorithm are not accurate.

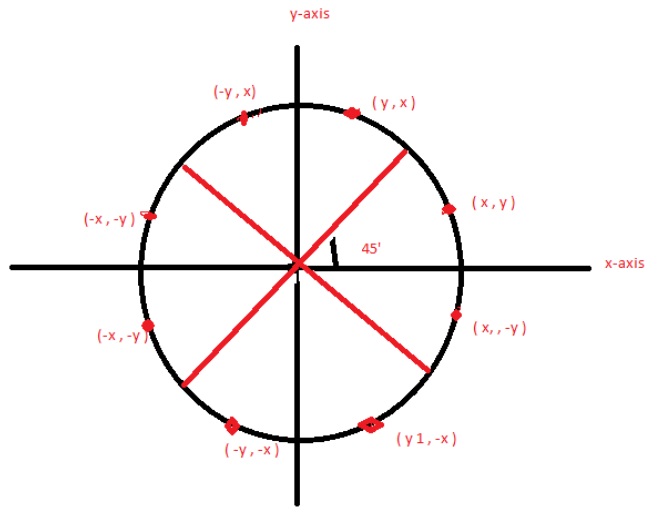
Question #4 (15 Marks)

When plotting a circle, the convention is to draw the arc of first quadrant and then impose the same values in all the other 7 quadrants. To plot the arc in first quadrant, we just need the radius of the circle.

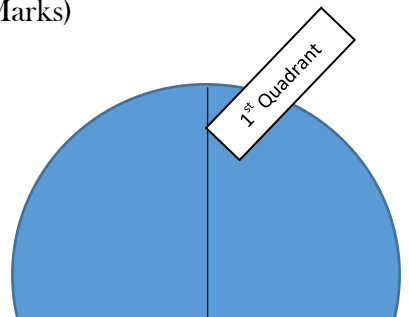
- a. Draw the first arc of the circle centered at (0, 0) and radius $r = 13$. (10 Marks)
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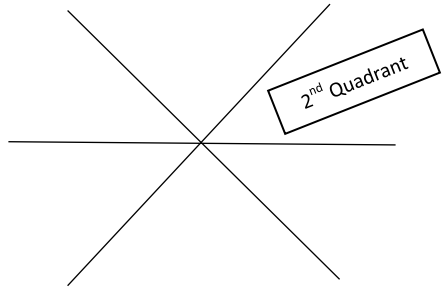
ANS . A

The first arc of the circle centered at (0, 0) and radius $r = 13$.



b. Convert the (x, y) values determined in part 'a' to the second quadrant. (5 Marks)





Q1104 Part = B

Page 1

Convert (x, y) values determined in Part 'a' to The Second quadrant.

Ans: $x = B$, $(x, y) = (a, 0)$

If $d > 0$ Then $(x+1, y-1)$
else $(x+1, y)$

Initially $(x, y) = (0, 13)$

where $d = 3 - (2 \times 6)$ and
 $x = 0$ $y = 13$

$$d = 3 - (2 \times 13)$$
$$= 3 - 26$$

$$d = -23 < 0$$

So $(x+1, y) = (1, 13)$

Now

$x < y$ $1 < 13$ So repeat above step.

$$d = -32 < 0 \text{ So}$$

$$d = d + (4 \times x) + 6$$

$$= -23 + (4 \times 1) + 6$$

$$d = -13 < 0$$

So $(x+1, y) = (2, 13)$ Here $x < y$

$$d = -13 + (4 \times 2) + 6 \quad 2$$
$$= -13 + 8 + 6$$
$$= 1 > 0$$

$$(x+1, y) = (3, 13)$$

$x < y$ and $d > 0$ So

$$d = d + 4 \times (x - y) + 10$$

$$= 1 + 4 \times (3 - 13) + 10$$

$$d = -29 < 0$$

and $(x, y-1) = (2, 12)$

$(x < y)$ and $(d < 0)$ Therefore

$$d = -29 + (4 \times 3) + 6 = -11 < 0$$

$$(x+1, y) = (4, 12)$$

$x < y$ and $d < 0$ Therefore

$$d = -11 + (4 \times 4) + 6 = 11$$

$$(x+1, y-1) = (5, 11)$$

$x < y$ and $d > 0$ Therefore

$$d = 11 + 4 \times (5 - 11) + 10$$

$$d = 19$$

So

(3)

$$(x+1, y-1) = (6, 10)$$

$x < y$ and $d > 0$ Therefore

$$d = 10 + 4 \times (6 - 10) + 10$$

$$d = 4 > 0$$

So

$$(x+1, y-1) = (7, 9)$$

$x < y$ and $d > 0$ Therefore

$$d = 9 + 4 \times (7 - 9) + 10$$

$$d = 6 > 0$$

$$\text{So } (x+1, y-1) = (8, 8)$$

Here $x = y$ So exit The

Program.