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SEC : B

Subject : Hydraulic  
Engineering

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Q 1

Ans

### Solution:-

The pressure drop  $\Delta p$  is expected to ~~dep~~ depend upon the gate opening  $h$ , the overall depth  $d$ , the velocity  $V$ , density  $\rho$  and viscosity  $\mu$ .

List the relevant variables:-

$\Delta p, h, d, V, \rho, \mu$

Write down dimensions:-

$\Delta p$	$ML^{-1}T^{-2}$
$h$	$L$
$d$	$L$
$V$	$LT^{-1}$
$\rho$	$ML^{-3}$
$\mu$	$ML^{-1}T^{-1}$

Number of variables,  $n = 6$   
Number of independent dimensions:  
 $M = 3$  (M, L and T)

Number of non-dimensional groups:  $n - M = 3$

Choose  $m (= 3)$  scaling variables:

Geometric ( $d$ ); Kinematic/time-dependent ( $V$ ); dynamic/mass-dependent ( $\rho$ ).

Form dimensionless groups by non-dimensionalising the remaining variables:  $\Delta p, h$  and  $\mu$ .



$$II_1 = \Delta p d^a V^b \rho^c$$

$$M^0 L^0 T^0 = (ML^{-1}T^{-2})(L)^a (LT^{-1})^b (ML^{-3})^c$$

$$= M^{1+c} L^{-1+a+b-3c} T^{-2-b}$$

$$M: 0 = 1+c \Rightarrow c = -1$$

$$T: 0 = -2-b \Rightarrow b = -2$$

$$L: 0 = -1+a+b-3c \Rightarrow a = 1+3c-b = 0$$

$$II_1 = \Delta p V^{-2} \rho^{-1} = \frac{\Delta p}{\rho V^2}$$

$$II_2 = \frac{h}{d} \text{ (by inspection, since } h \text{ is a length)}$$

$$II_3 = \mu d^a V^b \rho^c$$

$$M^0 L^0 T^0 = (ML^{-1}T^{-1})(L)^a (LT^{-1})^b (ML^{-3})^c$$

$$= M^{1+c} L^{-1+a+b-3c} T^{-1-b}$$

$$M: 0 = 1+c \Rightarrow c = -1$$

$$T: 0 = -1-b+0 \Rightarrow b = -1$$

$$L: 0 = -1+a+b-3c \Rightarrow a = 1+3c-b = -1$$

$$\Rightarrow II_3 = \mu d^{-1} V^{-1} \rho^{-1} = \frac{\mu}{\rho V d}$$

Recognition of the Reynolds number suggests that we replace  $II_3$  by

$$II_3' = (II_3)^{-1} = \frac{\rho V d}{\mu}$$

Hence, dimensional analysis yields.

$$II_3' = \left( \frac{\rho V d}{\mu} \right)_p = \left( \frac{\rho V d}{\mu} \right)_m$$

(a) From the last, we have a velocity ratio:

$$\begin{aligned} \frac{V_p}{V_m} &= \frac{(\mu/\rho)_p}{(\mu/\rho)_m} \frac{d_m}{d_p} = \frac{0.002/800}{1.0 \times 10^{-6}} \times \frac{1}{5} \\ &= \boxed{0.5} \end{aligned}$$

Hence,

$$V_m = \frac{V_p}{0.5} = \frac{3.0}{0.5} = 6.0 \text{ ms}^{-1}$$

(b) The ratio of the quantities of flow is.



(c) Finally, For the pressure drop:

$$II_1 = \left( \frac{\Delta P}{\rho V^2} \right)_p = \left( \frac{\Delta P}{\rho V^2} \right)_m = \frac{(\Delta P)_p}{(\Delta P)_m}$$

$$= \frac{P_p}{P_m} \left( \frac{V_p}{V_m} \right)^2 = \frac{800}{1000} \times 0.5^2 = 0.2$$

Hence,

$$\begin{aligned} \Delta P_p &= 0.2 \times \Delta P_m = 0.2 \times 60 \\ &= \boxed{12.0 \text{ kPa}} \end{aligned}$$

Q 2  
Ans

Given data:-

$$\text{Max length depth} = 78\text{m}$$

$$\text{Specific gravity} = 2.4$$

$$f_{av} = 788 \text{ T/m}^2$$

$$\text{Height of wave} = 1.2\text{m}$$

Solution:-

$$(1) H_{\text{Limiting}} = \frac{f_{av}}{\gamma_w(G - W + 1)}$$

$$= \frac{788 \times 1000}{1000(2.4 - 0 + 1)}$$

$$H_{\text{Limiting}} = \boxed{231.764}$$

(2) Top width "a" :-

$$\text{Free board} = 1.5 \times h \times \text{Wave}$$

$$= 1.5 \times 1.2$$

$$\text{Free board} = \boxed{1.8}$$

$$\text{Height of dam} = H_w + 1.8$$

$$= 78 + 1.8$$

$$H.D = 79.8$$

$$a = 14\% \text{ of } H.D$$

$$= 0.14 \times 79.8 = \boxed{11.172\text{m}}$$



(3) Base width:-

$$b' = \frac{HW}{M \cdot G_1} = \frac{78}{0.7 \times 2.4}$$
$$= 46.42 \text{ m}$$
$$= \boxed{47}$$

(4) For no tension criteria:-

$$b' = \frac{HW}{\sqrt{G_1}} = \frac{78}{\sqrt{2.4}}$$
$$b' = \boxed{50.34}$$

(5) Depth of vertical portion on u/s sides:-

$$h' = 2a \sqrt{G_1 \cdot W}$$
$$= 2 \times 11.172 \sqrt{2.4 - 0}$$
$$= 34.60$$
$$h' = \boxed{35 \text{ m}}$$

(7) Total width of the base of the dam.

$$b = b' + \frac{a}{16} = 50.34 + \frac{11.172}{16}$$
$$= \boxed{51.03}$$

$$(8) \tan \alpha = \frac{b'}{H} = \frac{50.34}{78}$$

$$\alpha = \tan^{-1}(0.64)$$

$$\alpha = 32.8^\circ$$

(9) Depth of vertical position on D/s  
(from WL on u/s side)

$$\tan \alpha = \frac{a}{d'} = \frac{11.172}{d'}$$

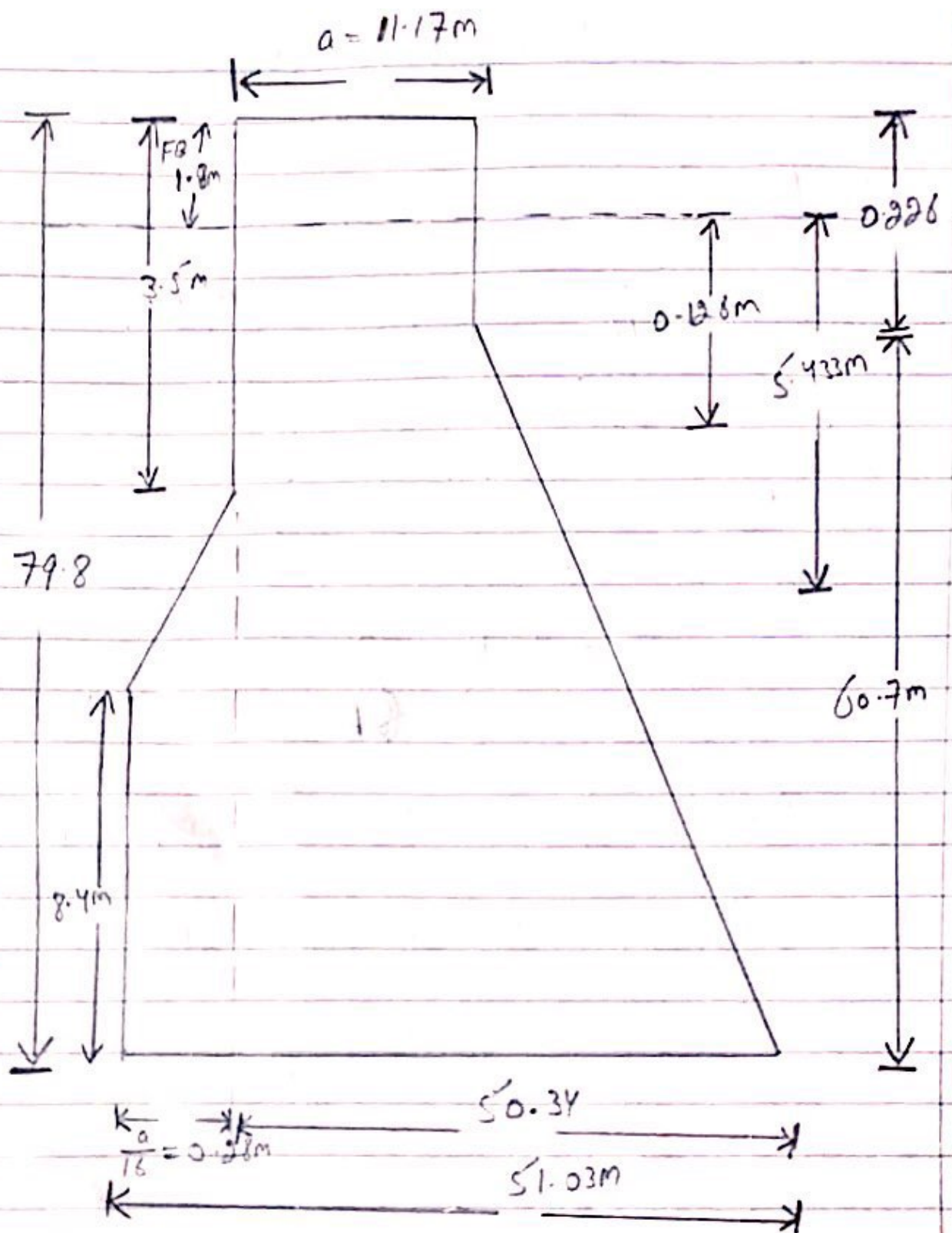
$$\tan \alpha = \frac{11.172}{d'}$$

$$\boxed{d' = 0.126}$$

(10) Depth of vertical position

$$d = d' + FB = 0.126 + 1.8$$





Q 3  
Ans Model analysis & Similitude:-

The prototype that I will take for my analysis is "Water turbine"

By means of model analysis or Dimensional analysis we take replica of prototype. on that model we conclude tests so whenever we are constructing actual "Water turbine" we will know the requirement for the considered "Water turbine". Dimensional analysis is a research work due to which we gathered information. By means of similitude is similarities b/w model and prototype. There are three types of similarities.

(1) Linear Similarity.

(2) Kinematic Similarity.

(3) Dynamic Similarity.

• Linear Similarity:-

It is a ratio b/w length of prototype and length of model.

$$\text{Mathematically:- } \frac{L_P}{L_N} = L_r = \frac{W_P}{W_N} = L_r$$



$$\frac{A_p}{A_m} = \frac{L_p \times b_p}{L_m \times b_m}$$

\* Kinematic Similarity:- It is the ratio of velocity b/w prototype and model.

$$= \frac{V_p}{V_m} = V_r = \frac{V_{p2}}{V_{m2}}$$

Kinematic similarity depends on the flow except forces.

\* Dynamic Similarity:- Dynamic similarity is the ratio of force b/w prototype & model.

$$\frac{F_{2p}}{F_{1m}} = F_r = \frac{F_{v_p}}{F_{v_m}}$$

$$F_r = \frac{F_{g_p}}{F_{g_m}}$$

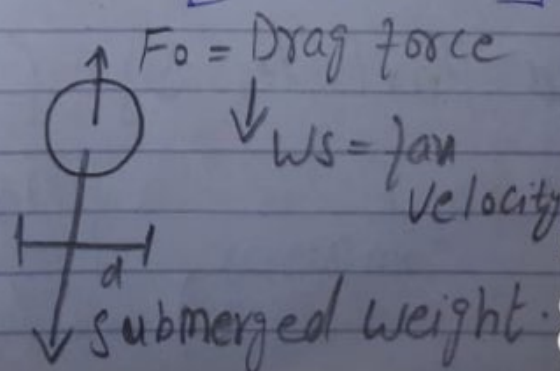
Q 4  
Ans

The downward velocity in a low dense fluid at equilibrium in which the sum of the gravity force, buoyancy force and fluid drag force are equal to zero.

When a grain falls down in still water it obtains a constant velocity when the upward fluid drag force on the grain is equal to the downward submerged weight of the grain. This is also called settling velocity.

Fall velocity effected due to the following terms:

- Particle diameter.
- Particle density.
- Particle Concentration.
- Particle Shape.
- Viscosity of water [temperature]
- Turbulence.





The force balance b/w the drag force and the submerged weight gives.

$F_D = \text{Submerged weight}$

$$\frac{1}{2} f C_D \frac{\pi}{4} d^2 W_s^2 = (\rho_s - \rho) g \frac{\pi d^2}{6}$$

$A = \frac{\pi d^2}{4} = \text{projected Area}$

$C_D = \text{Drag Co-efficient}$

$W_s = \text{fall velocity of sediment}$

$$= \sqrt{\frac{4gd}{3C_D} \left( \frac{\rho_s - \rho}{\rho} \right)}$$

$\rho = \text{Density of Water}$

$\rho_s = \text{Density of sediment}$

Particle

Lets define the terms by which Fall velocity effected.

Particle Size (diameter) ::

Particle Size is a notion introduced for comparing dimensions of solid particles, liquid particles or gaseous

## Particles.

### \* Particle density:-

The particle density or true density of a particulate solid or powder, is the density of the particles that make up the powder.

### \* Particle Shape:.

It defined by the relative dimensions of the long, intermediate and short axes of the particles.

### \* Viscosity of Water:-

Viscosity defines a fluid's internal resistance to flow and may be thought of as a measure of fluid friction.

### \* Turbulance:-

Turbulence or turbulent flow is fluid motion characterized by chaotic changes in pressure and flow velocity. It is an contrast to laminar flow