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Section A

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subject Hydraulic Engineering

Assignment # 1

Q#1

→ Venturi flume :-

It is a critical flow open flume with a constricted flow which causes a drop in the hydraulic grade line, creating a critical depth.

It is used in flow measurement of very large flow rates, usually given in millions of cubic units. A venturi meter would normally measure in millimetres, whereas a venturi flume measures in metres.

Measurement of discharge with venturi flumes requires two measurements, one upstream and one at the throat (narrowest cross section) if the flow passes in a ^{sub}critical state through the flume. If the flumes are designed so as to pass the flow from subcritical to supercritical state while passing through the flume, a single measurement at the throat is sufficient for computation of discharge. To ensure the occurrence of critical depth at the throat, these are designed in such a way as to form a hydraulic jump on the downstream side of the structure. These flumes are called "standing wave flume".

Q# 2

→ Given data :-

width of channel = $b = 3\text{m}$
Discharge = $Q = 12\text{ m}^3/\text{sec}$.

→ Solution :-

① Critical depth

→ discharge per unit width

$$q = \frac{Q}{b} = \frac{12}{3} = 4\text{ m}^3/\text{sec}$$

→ For rectangular channel.

$$h_c = \left(\frac{q^3}{g}\right)^{1/3} = \left(\frac{4^3}{9.81}\right)^{1/3}$$

$$h_c = 1.18\text{ m}$$

② Minimum Specific Energy (E_c):

→ For rectangular channel.

$$E_c = \frac{3}{2} h_c = \frac{3}{2} \times 1.18$$

$$= 1.77\text{ m}$$

© The Alternate depth $E = 4\text{m}$.

→ As $E > E_c$, There are two possible depths for a given E_c

$$E = h + \frac{V^2}{2g} \quad \text{where } V = \frac{Q}{A} = \frac{Q}{bh}$$

(For rectangular channel.)

$$E = h + \frac{V^2}{2gh^2}$$

$$4 = h + \frac{0.8155}{h^2}, \quad h = 4 - \frac{0.8155}{h^2}$$

→ For the subcritical solution the first term, associated with potential energy dominates

→ Iteration (from $h = 4$) gives $h = 3.948\text{m}$ for the subcritical (first, shallow) solution. The term associated with kinetic energy dominates, rearrange as

$$\text{So, } h = \sqrt{\frac{0.8155}{4-h}}$$

→ Iteration (from $h = 0$) gives $h = 0.4814\text{m}$
So Alternate depths are 3.95m and 0.4814m .

Assignment # 2

Q # 1

→ First of all we find the Froude number to find the flow.

As we know that

$$F_r = \frac{v}{\sqrt{gy}} = \frac{6 \text{ m/s}}{\sqrt{9.81 \times 0.1}}$$

$$F_r = 6.06 > 1$$

So the flow is super-critical.

→ Alternate depth :-

As we know that

$$E = y + \frac{v^2}{2y}$$
$$= 0.1 + \frac{6^2}{2 \times 9.81} = 1.935 \text{ m}$$

The alternate for $E = 1.935 \text{ m}$

yields $y_{\text{alternate}} = 1.93 \text{ m}$

Q#2

→ Given data :-

- velocity = $V_1 = 2 \text{ m/s}$
- depth = $y_1 = 3 \text{ m}$
- Elevation = $60 \text{ cm} = 0.6 \text{ m}$
- down step = $15 \text{ cm} = 0.15 \text{ m}$

→ Solution :- As we know that

$$E_1 = y_1 + \frac{V_1^2}{2g}$$

$$E_1 = 3 + \frac{2^2}{2 \times 9.81}$$

$$\rightarrow E_1 = 3.20 \text{ m}$$

Now $E_2 = E_1 - 1Z$

$$= 3.2 - 0.6$$
$$= 2.60 \text{ m}$$

Also $E_2 = y + \frac{V^2}{2gy^2}$

$$2.60 = y^2 + \frac{6^2}{2 \times 9.81 \cdot y^2}$$

$$y_2 = 2.24 \text{ m}$$

$$\Delta y = y_2 - y_1$$

$$= 2.24 - 3$$

$$= -0.76 \text{ m}$$

So water surface drop = 0.16 m

- For a downward step of 15 cm or 0.15 m we have

$$E_2 = E_1 - \Delta z = 3.20 - (-0.15)$$

$$\rightarrow E_2 = 3.35 \text{ m}$$

$$\text{Now } y_2 = 3.17 \text{ m}, \Delta y = y_2 - y_1$$

$$= 3.17 - 3$$

$$\Delta y = 0.17 \text{ m}$$

\rightarrow So water surface rises 0.02 m.

- The maximum upstep possible before effecting upstream water surface level is for

$$y_2 = y_c \rightarrow y_c = \sqrt[3]{\frac{q^2}{g}}$$

$$y_c = \sqrt[3]{\frac{6^2}{9.81}}$$

$$y_c = 1.54 \text{ m}$$

Assignment # 3

Q#1

→ Given data :-

$$y_1 = 3.6 \text{ m} \quad , \quad y_2 = 0.9 \text{ m}$$

$$b = 3.9 \text{ m}$$

→ Solution :- As we know that
 $E_1 = E_2$

$$y_1 + \frac{v_1^2}{2g} = y_2 + \frac{v_2^2}{2g} \quad \text{--- (1)}$$

→ Also

$$Q = A_1 v_1 = A_2 v_2 \quad (b_1 = b_2)$$
$$b_1 y_1 \cdot v_1 = b_2 y_2 \cdot v_2$$
$$y_1 \cdot v_1 = y_2 \cdot v_2$$

$$v_2 = \frac{y_1}{y_2} \times v_1$$

$$v_2 = \frac{3.6}{0.9} \times v_1$$

$$\rightarrow v_2 = 4v_1 \quad \text{--- (2)}$$

putting in eq ①

$$y_1 + \frac{v_1^2}{2g} = y_2 + \frac{v_2^2}{2g}$$

$$\rightarrow 3.6 + \frac{v_1^2}{2g} = 0.9 + \left(\frac{4v_1}{2g}\right)^2$$

$$3.6 + \frac{v_1^2}{2g} = 0.9 + \frac{16v_1^2}{2g}$$

$$\frac{v_1^2}{2g} - \frac{16v_1^2}{2g} = 0.9 - 3.6$$

$$\frac{v_1^2 - 16v_1^2}{2g} = -2.7$$

$$\frac{-15v_1^2}{2g} = -2.7$$

$$\sqrt{v_1^2} = \sqrt{\frac{2.7 \times 2(9.81)}{15}}$$

$v_1 = 1.879$ m/sec \rightarrow putting in eq ② we get.

$$v_2 = 4v_1 \\ = 4(1.879)$$

$$v_2 = 7.516 \text{ m/sec.}$$

→ A_c

~~Q1 = A1 V1~~

$$Q_1 = A_1 V_1 = b y_1 \cdot V_1$$

$$= 3.9 \times 3.6 \times 1.879$$

$$\bullet Q_1 = 26.38 \text{ m}^3/\text{sec}$$

$$Q_2 = A_2 V_2 = b \cdot y_2 \cdot V_2$$

$$= 3.9 \times 0.9 \times 7.516$$

$$\bullet Q_2 = 26.38 \text{ m}^3/\text{sec}$$

$$Q_1 = Q_2 = 26.38 \text{ m}^3/\text{sec}$$

① Froude number → At upstream side

$$Fr_1 = \frac{V_1}{\sqrt{g y_1}} = \frac{1.879}{\sqrt{9.81 \times 3.6}} = 0.31 \rightarrow \text{sub-critical flow.}$$

② Froude number → At downstream side

$$Fr_2 = \frac{V_2}{\sqrt{g y_2}} = \frac{7.516}{\sqrt{9.81 \times 0.9}} = 2.59$$

↓

super-critical flow.