

QNO 1:-

Part A:-

Given:-

$$\text{Discharge} = 7795 \text{ lit/sec} = 7.795 \text{ m}^3/\text{sec}$$

$$\text{Width of channel} = 8 \text{ m}$$

$$\text{mean velocity} = 7795 / 3.28$$

$$= 2375 \text{ lit/sec}$$

$$= 2375 / 3.28 = 2309.4 \text{ m/sec}$$

Req:-

⇒ Height of hydraulic jump

⇒ power absorbed due to hydraulic jump

Sol:- AS

Height of hydraulic jump:-

AS  $q$  is discharge per unit width

$$q = Q/b$$

$$= 7.795 / 8 = \boxed{q = 0.974 \text{ m}^2/\text{sec}}$$

⇒ AS critical depth ( $y_c$ ) is

$$y_c = (q^2/3)^{1/3} = \left( \frac{(0.974)^2}{3} \right)^{1/3}$$

$$\boxed{y_c = 0.45 \text{ m}}$$

⇒ Critical velocity:-

$$\text{AS } q = v y \Rightarrow v = q/y$$

$$v_c = \frac{q}{y_c} \Rightarrow v_c = 0.974 / 0.45$$

$$\boxed{v_c = 2.16 \text{ m/sec}}$$

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AS  $u_1 > v_c \Rightarrow$  super-critical flow

water depth on upstream side-

$$Q = AV$$

$$Q = (by) \cdot v \Rightarrow y = Q/v \cdot b$$

$$\Rightarrow y_1 = Q/v_1 \cdot b$$

$$= 7.795 / 2.16 \times 8$$

$$\boxed{y_1 = 0.45}$$

by formula

$$y_2 = \frac{-y_1}{2} + \sqrt{\frac{y_1^2}{4} + \frac{2y_1v_1^2}{g}}$$

$$= \frac{-0.45}{2} + \sqrt{\frac{(0.45)^2}{4} + \frac{2(0.45)(2.16)^3}{9.81}}$$

$$= \frac{-0.45}{2} + 0.691$$

$$\boxed{y_2 = 0.466\text{m}}$$

Difference in depth-

$$\Delta y = y_2 - y_1$$

$$= 0.466 - 0.45 = \boxed{0.016\text{m}}$$

AS

$$\Delta E = E_1 - E_2$$

$$= 0$$

Also,  $Q_1 = Q_2$

$$A_1 v_1 = A_2 v_2$$

$$b_1 y_1 v_1 = b_2 y_2 v_2$$

$$b \cdot y_1 \cdot v_1 = b \cdot y_2 \cdot v_2$$

$$\therefore b = b_1 = b_2$$

$$v_2 = \frac{y_1 v_1}{y_2}$$

$$= \frac{0.45 \times 2309.4}{0.466}$$

$$v_2 = 2330.1 \text{ m/sec}$$

$$\Delta E = E_1 - E_2$$

$$\left( y_1 + \frac{v_1^2}{2g} \right) - \left( y_2 + \frac{v_2^2}{2g} \right)$$

$$= \left( 0.45 + \frac{(2309.4)^2}{2 \times 9.81} \right) - \left( 0.466 + \frac{(2330.1)^2}{2 \times 9.81} \right)$$

$$= 0.45 + 271831.2 - 0.466 + 253483.48$$

$$E_1 - E_2 = 271831.85 - 253483.866$$

$$E_1 - E_2 = 18347.79$$

⇒ power dissipation of hydraulic jumps -

$$\Delta P = \rho g Q (E_1 - E_2)$$

$$= (1000)(9.81)(7.795)(18347.79)$$

$$= 1403036236 \text{ W}$$

$$\Delta P = 1403036236 \text{ kW}$$

part B:-

given:-

channel width (b) = 4 m

Discharge = 7795 m<sup>3</sup>/sec

height of upstream side = 2.9 m

height of downstream side = 1.1 m

Req:-

Down stream velocity = ?

Sol:-

As

Specific energy is

$$E_1 = E_2$$

$$y_1 + \frac{v_1^2}{2g} = y_2 + \frac{v_2^2}{2g} \rightarrow (1)$$

Also from discharge

$$Q = A_1 v_1$$

$$A_1 v_1 = A_2 v_2$$

$$b_1 y_1 v_1 = b_2 y_2 v_2$$

$$K \cdot y_1 \cdot v_1 = K \cdot y_2 \cdot v_2$$

$$y_1 v_1 = y_2 v_2$$

$$v_2 = \frac{y_1 v_1}{y_2}$$

$$v_2 = \frac{(2.9)}{1.1} v_1$$

$$v_2 = 2.63 v_1 \quad \text{put in eq (1)}$$

$$2.9 + \frac{v_1^2}{2(9.81)} = 1.1 + \frac{(2.63 v_1)^2}{2(9.81)}$$

$$2.9 + \frac{v_1^2}{2(9.81)} = 1.1 + \frac{6.91 v_1^2}{2(9.81)}$$

$$\frac{v_1^2}{2(9.81)} - \frac{6.91 v_1^2}{2(9.81)} = 1.1 - 2.9$$

$$\frac{-5.91 v_1^2}{2(9.81)} = -1.8$$

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$$5.91 \text{ m}^3 = (1.8)(2)(9.81)$$

$$v_1 = \sqrt{\frac{(1.8)^2(9.81)}{5.91}}$$

$$v_1 = 2.44 \text{ m/sec}$$

put in eq (v)

$$v_2 = 2.63(2.44)$$

$$v_2 = 6.42 \text{ m/sec}$$

Type of flow using Froude number

⇒ on upstream side

$$F_{r1} = \frac{v_1}{\sqrt{g y_1}} = \frac{2.44}{\sqrt{9.81 \times 2.91}}$$

$$= 0.45$$

$F_r < 1$  sub-critical flow

⇒ on downstream side

$$F_{r2} = \frac{v_2}{\sqrt{g y_2}} = \frac{6.42}{\sqrt{9.81 \times 1.1}}$$

$$= 1.95$$

$F_r > 1$   
super-critical flow.

Q No 2  
Part A:-  
Given:-

Depth of channel = 1.8m

Discharge  $7795 \text{ m}^3/\text{sec} = 7795 / (3.28)^3 = 220.8 \text{ m}^3/\text{sec}$

Width of channel = 66ft = 20.1m

Req:-

$p = \text{weir height} = ?$

Solo AS

$Q = AV$

$V = Q/A \Rightarrow V_1 = Q_1/A$   
 $= Q/b y$

$V_1 = \frac{220.8}{20.1 \times 1.8} = \boxed{6.11 \text{ m/sec}}$

Critical depth:-

$y_c = \left( \frac{q^3}{g} \right)^{1/3}$

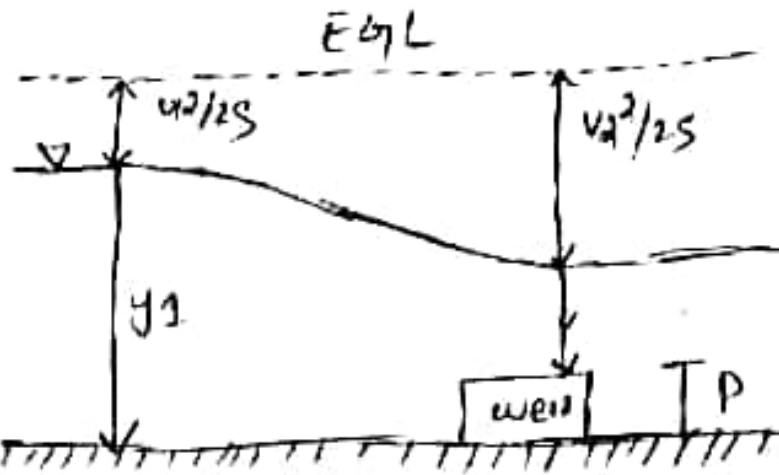
AS,  $q = Q/b$   
 $= 220.8 / 20.1$   
 $= 10.9 \text{ m}^2/\text{sec}$

$y_c = \left( \frac{(10.9)^3}{9.81} \right)^{1/3} = \boxed{2.29 \text{ m}}$

Also  $V = \sqrt{g y}$   
 $V_c = \sqrt{g y_c}$   
 $V_c = \sqrt{9.81 \times 2.29}$

$V_c = \boxed{4.73 \text{ m/sec}}$

From the figure



$$\frac{v_1^2}{2g} + y_1 = \frac{v_2^2}{2g} + y_2 + P$$

$$\frac{(6.10)^2}{2 \times 9.81} + 1.8 = \frac{(4.73)^2}{2 \times 9.81} + 2.29 + P$$

$$1.89 + 1.8 = 1.14 + 2.29 + P$$

$$3.69 = 3.43 + P$$

$0.26 \text{ m} = P$  The well should have height of 0.26m.

Q No 2

Part B

Given:-

width = 2.8 m

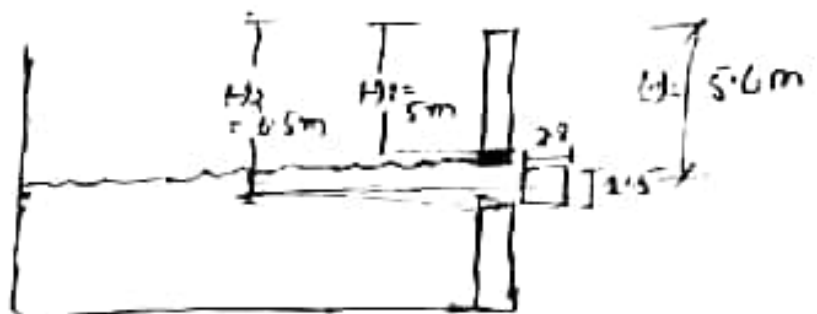
depth = 1.5 m

$H_1 = 5 \text{ m}$

$H_2 = 6.5 \text{ m}$

$H = 5.6 \text{ m}$

$C_d = 0.7795$



Sol:-

submerged position

$$Q_1 = C_d \times b \times (H_2 - H_1) \times \sqrt{2gH}$$

$$Q_1 = 0.7795 \times 2.8 (6.5 - 5.6) \times \sqrt{2 \times 9.81 \times 5.6}$$

$$Q_1 = 20.53 \text{ m}^3/\text{sec}$$

Free portion

$$Q_2 = \frac{2}{3} c_d \times b \sqrt{2g} \times [H^{3/2} - H_1^{3/2}]$$

$$Q_2 = \frac{2}{3} (0.7795) \times (2.8) \sqrt{2(9.81)} \times [5.6^{3/2} - 5^{3/2}]$$

$$Q_2 = (1.46)(4.429)(13.25 - 11.18)$$

$$Q_2 = (6.466)(2.07)$$

$$Q_2 = 13.38 \text{ m}^3/\text{sec}$$

$$\text{Total} = Q_1 + Q_2$$

$$Q = 20.53 + 13.38$$

$$Q = 33.91 \text{ m}^3/\text{sec}$$

Q No 3:-  
Part A:-  
Given:-

$$d_1 = R - 200 \text{ mm} \\ = 7795 - 200 = 7595 \text{ mm}$$

$$d_2 = R + 3000 \text{ mm} \\ = 7795 + 3000 \text{ mm} = 10795 \text{ mm}$$

Flow rate (Q) = 0.95 m<sup>3</sup>/sec

pressure in large pipe

$$= P + 800 \text{ N/m}^2 \\ = 7795 + 800 \\ = 8595 \text{ N/m}^2$$



Req:-

- ⇒ The loss of head due to sudden enlargement.
- ⇒ The power loss due to sudden enlargement.
- ⇒ The pressure in the smaller pipe.

Sol:- As

⇒ loss of head due to sudden enlargement:-

$$\Rightarrow d_1 = 7595 \text{ mm} = 7.59 \text{ m}$$

$$\Rightarrow A_1 = \frac{\pi}{4} (7.59)^2 = 45.22 \text{ m}^2$$

$$\Rightarrow d_2 = 10795 \text{ mm} = 107.95 \text{ m} = 107.95 \text{ m}$$

$$\Rightarrow \frac{\pi}{4} (107.95)^2 = 8474 \text{ m}^2$$

$$\text{As, } Q = AV$$

$$V = Q/A \quad \Rightarrow \quad v_1 = Q/A_1$$

$$v_1 = \frac{0.95}{45.22} = \boxed{0.021 \text{ m/sec}}$$

Similarly

$$v_2 = Q/A_2$$

$$v_2 = 0.95 / 8474 = \boxed{0.011 \text{ m/sec}}$$

Formula of sudden enlargement:-

$$h_e = \left(1 - \frac{A_1}{A_2}\right)^2 \times \left(\frac{v_1 - v_2}{2g}\right)^2$$

$$= \left(1 - \frac{45.22}{8474}\right)^2 \times \left(\frac{0.021 - 0.011}{2 \times 9.81}\right)^2$$

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$$= (0.217) (5.09 \times 10^{-6})$$

$$h_e = 1.106 \times 10^{-6} \text{ m}$$

2. power loss due to sudden enlargement:-

$$P = \rho g \phi h_e$$

$$= (1000)(9.81)(0.95)(1.106 \times 10^{-6})$$

$$P = 0.010 \text{ W}$$

3) pressure in smaller pipe:-

by using bernoullis equation

$$\frac{P_1}{\rho g} + \frac{v_1^2}{2g} \pm \frac{P_2}{\rho g} + \frac{v_2^2}{2g} + h_e$$

$$\frac{P_1}{\rho g} + \frac{(0.021)^2}{2g} = \frac{8595}{\rho g} + \frac{(0.011)^2}{2g} + 1.106 \times 10^{-6}$$

$$\frac{P_1}{(1000)(9.81)} + 2.34 \times 10^{-5} = 0.876 + 6.16 \times 10^{-6} + 1.106 \times 10^{-6}$$

$$\frac{P_1}{9810} = 0.875$$

$$P_1 = 8583.75 \text{ N/m}^2$$

$$P_1 = 8583.75 \text{ N/m}^2$$

QNO3

Part B:-

specific energy:-

Specific energy is a parameter that can be used to identify the meaning of super-critical, sub-critical and critical flow. In an open channel critical depth is the depth corresponding to maximum specific energy.

$$\begin{aligned} \Rightarrow y > y_c &; E > E_{min} \text{ (sub-critical flow)} \\ y = y_c &; E = E_{min} \text{ (critical flow)} \\ y < y_c &; E < E_{min} \text{ (super critical flow)} \end{aligned}$$

We know that

$$(E - y) y^3 = \text{const } q^2 / 2g \rightarrow (3)$$

$q$  and  $2g$  constant and this equation is used to prepare a plot of specific energy.

