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Section: A

Subject : Fluid Mechanics

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Part A:- Q#1:-Total Energy Head:-

It is the sum of all energy head at a point in a fluid-

OR

From Bernoulli Principle the total energy at a given point in a fluid is the energy associated with movement of fluid, plus energy from static pressure in the fluid energy from height of fluid relative to an arbitrary datum height-

Forms of Energy Head:-

There are various forms of Energy Head which are as follow-

- ① Kinetic Head
- ② Potential Head-
- ③ Pressure Head-

### ① Kinetic Head:-

It is the kinetic energy per unit weight of the fluid

### Mathematical Form:-

$$\frac{K.E}{W} = \frac{\frac{1}{2} mv^2}{mg}$$

$$\frac{K.E}{W} = \frac{1}{2} \frac{v^2}{g}$$

→ This is also known as velocity head.

### UNIT:-

Its unit is meter (m).

## Potential Head:-

It is the Potential energy Per Unit weight of the Fluid-

## Mathematical Form:-

$$\frac{P.E}{W} = \frac{mgh}{mg} = h$$

## Pressure Head:-

The vertical height of the free surface above any point in a liquid at rest is Pressure Head-

OR

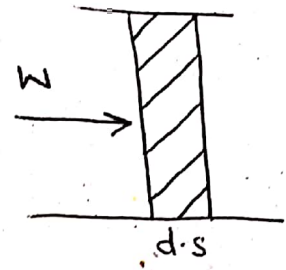
Level of fluid due to pressure exerted by fluid-

## Mathematical Form:-

$$\text{Pressure Head} = \frac{P.E}{\text{weight}} = \frac{P}{\gamma}$$

OR

$$\Rightarrow \frac{F \cdot ds}{W}$$
$$= \frac{P \cdot A \cdot ds}{W}$$



$$= \frac{P \cdot V}{W} = \frac{P}{\gamma} \text{ is Pressure}$$



## Q#1 :- [Part B]

Hyd

Hydraulic Grade Line:-

Hydraulic grade

line refers to the profile of water streaming in an open channel or a pipe streaming in a part full - when pipe is under pressure, the pressure driven review line is the level to which the water would ascend to in a little, verticle tube associated with a pipe.

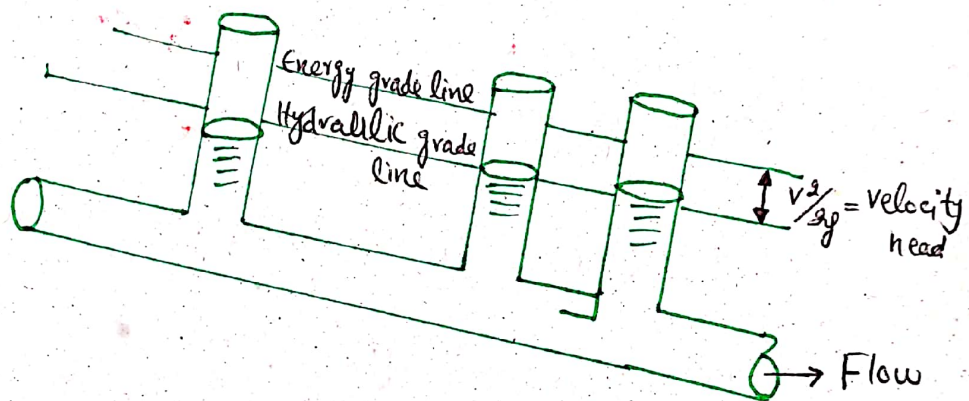
It is denoted as (HGL)-

→ The hydraulic grade line is a line representing the total head available to the fluid - minus velocity head and can be expressed as

$$HGL = \frac{P}{\rho + h}$$

where HGL = Hydraulic Grade line

The Hydraulic Grade line lies on velocity head below the Energy line-



### \* Energy Line:- (EGL)

Energy Grade line refer

to a line that represents to the height of energy head of water, streaming in a pipe course, or channel. The line is drawn over the Pressure Hydraulic grade line (inclination)

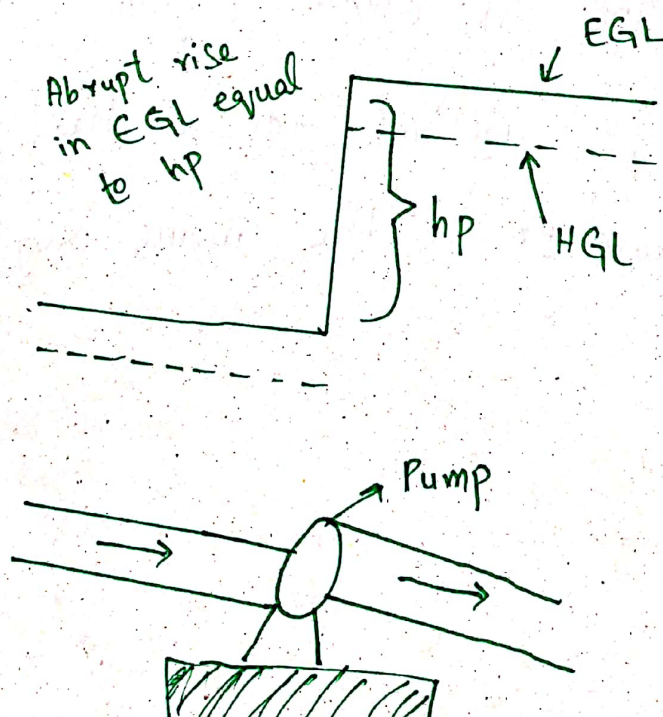
The separation equivalent to speed head ( $\frac{v^2}{2g}$ ) of the water streaming at every area or a point along the pipe or channel-

→ The Energy line is a line that represent the total head available the fluid can be expressed as-

$$EL = H = P/\gamma + \frac{v^2}{2g} = \text{Constant}$$

along a stream line

EL = Energy line



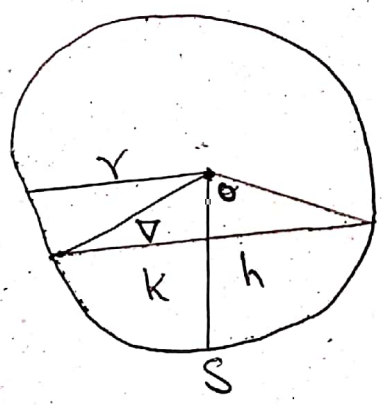


## ⇒ Hydraulic Radius:-

Hydraulic Radius is the area of water Prism in a Pipe or channel divided by the wetted Perimeter- Thus for a Sound Conduit flowing full or half full the hydraulic radius is  $d/4$ -

- Hydraulic radius measure the flow efficiency of a Pipe-
- In trenchless technology, it is a function of the shape of the Pipe in which liquid-
- It does not indicate half of the diameter as the name suggests-

→ Another term sometimes used for this quantity is hydraulic mean depth-



Q# 2:- Part A

Given data:-

$$V = 2 \text{ m/sec}$$

$$P = 300 \text{ kps} = 300 \times 10^3 \text{ N/m}^2$$

$$Z = 5 \text{ m}$$

$$\gamma = 9810$$

Required:-

H = total energy per weight = ?

Solution:-

As we know that

H = Pressure Head + kinetic energy (Head)  
+ Potential energy (Head) -

$$H = \frac{P}{\gamma} + \frac{V^2}{2g} + Z$$

Putting the values in the above equation

$$H = \frac{300 \times 10^3}{9810} + \frac{(2)^2}{2(9.81)} + 5 \text{ m}$$

$$H = 30.581 + 0.20 + 5$$

$$H = 35.784 \text{ m}$$



Q#2 [Part B] :-

Given data:-

$$\text{Diameter} = d_1 = 300 \text{ mm}$$

$$\text{Diameter} = d_2 = 200 \text{ mm}$$

$$\text{Pressure} = P_1 = 300 \text{ kpa} = 300 \times 10^3 \text{ N/m}^2$$

$$P_2 = 120 \text{ kpa} = 120 \times 10^3 \text{ N/m}^2$$

$$\text{Datum} = Z = ?$$

Sol:-

$$Q = \frac{40 \text{ m}^3/\text{sec}}{1000} = \boxed{0.04}$$

$$d_1 = 300 \text{ mm} = 0.3 \text{ m}$$

$$d_2 = 200 \text{ mm} = 0.2 \text{ m}$$

Required :-

$$Z = ?$$

Sol:-

$$A_1 = \frac{\pi d^2}{4}$$

$$= \frac{(3.14)(0.3)^2}{4}$$

$$A_1 = 0.0706 \text{ m}^2$$

$$A_2 = \frac{\pi d^2}{4}$$

$$= \frac{(3.14)(0.2)^2}{4}$$

$$A_2 = 0.0314 \text{ m}^2$$

We know that

$$Q = V_1 A_1$$

$$V_1 = \frac{Q}{A_1} = \frac{0.04}{0.0706}$$

$$V_1 = 0.566$$

$$V_2 = \frac{Q}{A_2}$$

$$V_2 = \frac{0.04}{0.0314}$$

$$V_2 = 1.27$$

Now

$$\frac{P_1}{\gamma} + \frac{V_1^2}{2g} + Z_1 = \frac{P_2}{\gamma} + \frac{V_2^2}{2g} + Z_2$$

Put

$$Z_1 = 0$$

$$\gamma = 9810$$

$$\frac{300 \times 10^3}{9810} + \frac{(0.566)^2}{2(9.81)} + 0 = \frac{120 \times 10^3}{9810} + \frac{(1.27)^2}{2(9.81)} + Z_2$$

$$30.597 + Z_1 = 12.314 + Z_2$$

$$Z_2 = 30.597 - 12.314$$

$$Z_2 = +18.283$$

$$\text{Now Datum} = Z = +18.283$$



Q# 3:-Given Data:-

$$\text{Length of Pipe} = L = 500\text{m}$$

$$\text{Dia} = D = 0.2\text{m}$$

$$\text{Specific gravity} = \rho = 0.9$$

$$\text{Flow rate} = Q = 0.06 \text{ m}^3/\text{s}$$

$$\text{Viscosity} = \mu = 6 \times 10^{-5} \text{ Ns/m}^2$$

Required:-

$$\text{Pressure loss} = \Delta P = ?$$

Solution:-

we know

$$f = \left[ 0.0032 + \frac{0.221}{R^{0.237}} \right] \rightarrow \textcircled{1}$$

Here !

R = Reynolds number

$$R = \frac{v \times d}{\mu}$$



$$\text{and } \nu = \frac{\mu}{\rho} = \frac{6 \times 10^{-5}}{900}$$

$$\rightarrow \nu = 6.67 \times 10^{-8} \text{ m}^2/\text{s}$$

$$\text{and } V = \frac{Q}{A} \quad \therefore A = \frac{\pi D^2}{4}$$

$$\Rightarrow V = \frac{0.06}{0.031}$$

$$\Rightarrow \boxed{V = 1.9356 \text{ m/s}}$$

$$\Rightarrow R = \frac{1.9356 \cdot 0.2}{6.67 \times 10^{-5}} = 5.8 \times 10^3$$

Hence

$$\text{eq ①} \Rightarrow f = 0.0032 + \frac{0.221}{(5.8 \times 10^3)^{0.237}}$$

$$\Rightarrow \boxed{f = 0.0684}$$

According to Bernoulli's equation

$$\text{head loss} = h_2 = \frac{f L V^2}{2gD} \rightarrow \text{②}$$

Putting value in equation (II)

$$h_L = \frac{(0.0664)(500)(1.9356)^2}{2(9.81)(0.9)}$$

$$h_L = 31.786$$

To find Pressure loss

$$h_L = \frac{\Delta P}{\rho g} \Rightarrow \Delta P = h_L \times \rho g$$

Putting values

$$\Delta P = 31.786 \times 900 \times 9.81$$

$$\Rightarrow \Delta P = 280638 \text{ Pa}$$

$$\Rightarrow \Delta P = 280.638 \text{ kPa}$$