

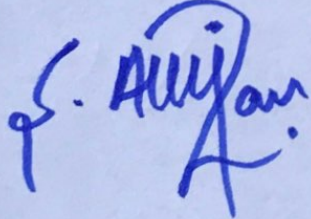
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SECTION : "A" Civil Deptt.

SUBJECT : MOs II

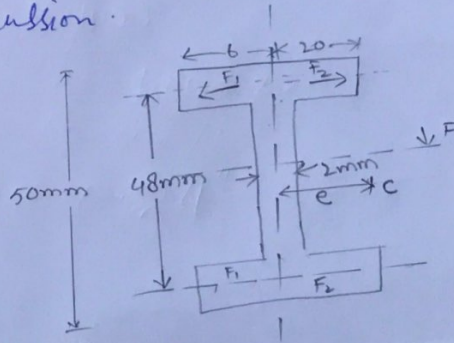
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STUDENT SIGN: 

DATE : 23-june-2020

Question No 15E:

Part "A" Determine the location of Shear Centre for the beams having the cross sectional dimension shown in the figure I. All members are to be considered thin walled and calculations should be based on the centroidal dimension.



Required: location of Shear Centre.

Solution: As we know that

$$e = \frac{2bh^2b^2}{4I}$$

and:

$$I = 2 \left(\frac{bh^3}{12} + Ay^2 \right) + \left(\frac{bh^3}{12} + Ay^2 \right)$$

$$= 2 \left(\frac{26(2)^3}{12} + (20 \times 2)(25)^2 \right) + \left(\frac{2(50)^3}{12} + 0 \right)$$

$$I = 5034.66 + 20833$$

$$I = 70867.98 \text{ mm}^4$$

$$e = \frac{2(50)^2(25)^2}{4(70867.98)}$$

$$\Rightarrow 11.02 \text{ mm}$$

So Shear Centre $e = 11.02 \text{ mm}$

Question NO 1st part "b"

Given:

• $H = 26 \text{ ft}$

• Assume diameter = $D = 22 \text{ ft}$

• tangential stress = 600 lb/ft^2

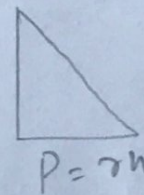
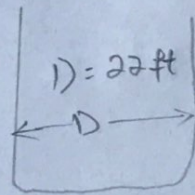
• Specific weight of water tank
= 62.4 lb/ft^3

Required: Find the thickness = ?

Solution:

The pressure developed by water $P = \gamma h$

$$\sigma_t = \frac{PD}{2t}$$



$$\sigma_t = \frac{PD}{2t} = \frac{\gamma h D}{2t}$$

$$2t \times \sigma_t = \gamma h D$$

$$2t = \frac{\gamma h D}{6t}$$

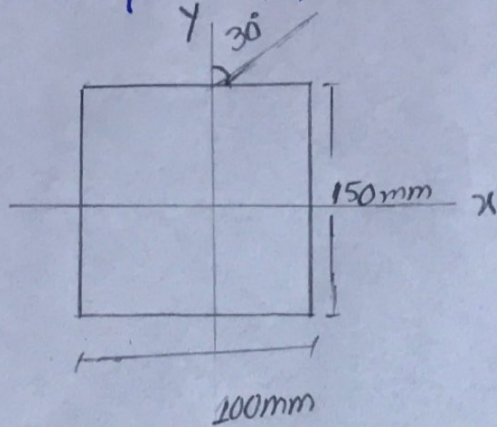
$$t = \frac{\gamma h D}{6t \times 2}$$

$$t = \frac{(62.4) \times (26 \times 12) \times (22 \times 12)}{(12)^3}$$

$$6000 \times 2$$

$$t = 0.24''$$

Question NO 2nd part (a)



MOMENT OF INERTIA :

$$I_z = \frac{bh^3}{12} = \frac{0.1(0.15)^3}{12}$$

$$I_z = 2.8125 \times 10^{-5}$$

NOW!

$$I_y = \frac{hb^3}{12} = \frac{0.15(0.1)^3}{12}$$

$$I_y = 1.25 \times 10^{-5}$$

$$\phi = \frac{M_z y}{I_z} + \frac{M_y z}{I_y}$$

$$\phi = \frac{M \cos \theta}{I_z} + \frac{M \sin \theta}{I_y}$$

Where

$$M = P \cos \theta = P \cos \theta = M_z$$

$$= 12 \cos 30^\circ = M_z$$

$$M_z = 1.8510$$

$$M \sin \theta = P \sin \theta = M_y$$

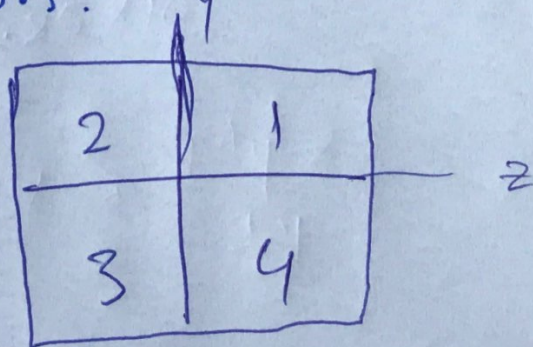
$$M_y = 12 \sin 30$$

$$M_y = -11.8563$$

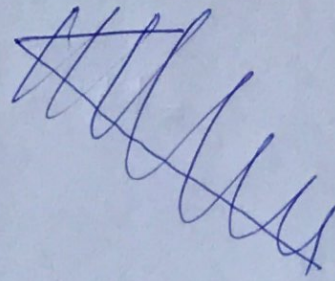
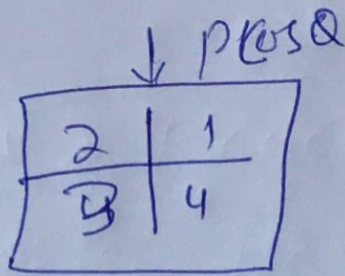
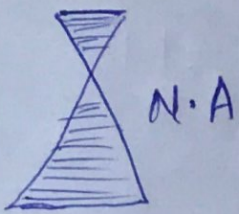
$$\sigma = \left(\frac{M_z}{I_z} \right) + \left(\frac{M_y}{I_y} \right)$$

$$\sigma = \frac{1.8510}{2.812 \times 10^5} + \left(\frac{-11.8563}{1.25 \times 10^5} \right) = 882628 \text{ Nm}^2$$

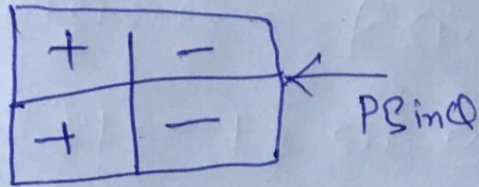
Sign Convention: y



If we take compression as negative and tension as positive and the beam is a simply supported.



Quadrant 1, 2 -ive
 Quadrant 3, 4 +ive



Quadrant 1, 4 -ive
 Quadrant 3, 2 +ive

In case of symmetrical loading the neutral axis lies at an angle of α to the principal axis and the algebraic sum of stress at N.A. is zero.

$$\sigma = \frac{M \cos \alpha}{I_x} y + \frac{M \sin \alpha}{I_y} z \quad \text{---} \textcircled{*}$$

In this ~~process~~ case N.A. passes through

2, 4, 2nd

$$\sigma = \frac{M \cos \alpha}{I_x} y + \frac{M \sin \alpha}{I_y} z$$

Let Consider a point A on N.A lies in Quadrant 2, where

- Bending stress due to $p \cos \theta$ is Compressive and
- Bending stress due to $p \sin \theta$ Tensile

$$\text{Eq } (*) = 0 = -\frac{M \cos \theta}{I_z} y_A + \frac{M \sin \theta}{I_y} z_A$$

$$0 = -\frac{M \cos \theta y_A}{I_z} + \frac{M \sin \theta z_A}{I_y}$$

$$\frac{y_A}{z_A} = \frac{I_z}{I_y} \frac{\sin \theta}{\cos \theta} = \tan \alpha = \frac{I_z}{I_y} \tan \theta \quad (**)$$

NOW! put the value of I_z , I_y and θ in eq (**)

$$\tan \alpha = \frac{I_z}{I_y} \tan 30$$

$$\tan \alpha = \frac{2.8125 \times 10^{-5}}{1.25 \times 10^{-5}} (\tan 30^\circ)$$

$$\tan \alpha = -14.4129.$$

$$\alpha = \tan^{-1} (-14.4129)$$

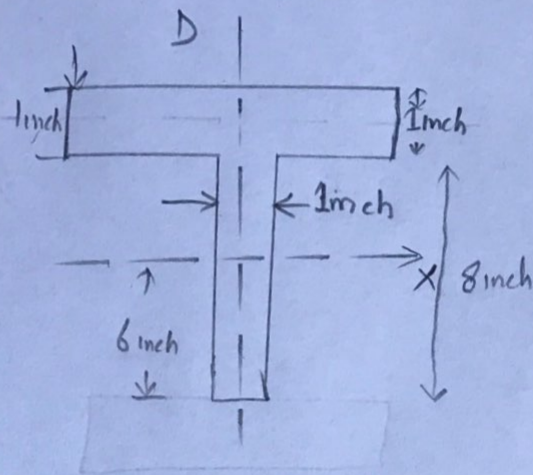
$$\alpha = 1.5^\circ$$

$$\alpha = 1^\circ 30' 5''$$

Question NO 2nd

Part NO "B"

Given:



$$L = 16 \text{ ft}$$

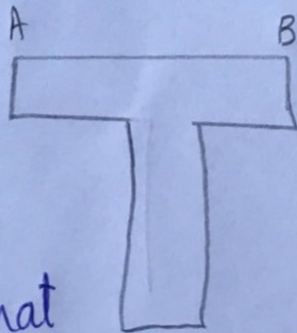
$$I_x = 112 \cdot 6 \text{ inch}^4$$

$$I_y = 18.7 \text{ inch}^4$$

$$\sigma_c = 12000 \text{ psi}$$

$$\sigma_t = 5000 \text{ psi}$$

Solution:



By given figure we can judge that maximum compression would occur at A and a actual maximum tension c at B there will tension as well as compression which will reduce that effect of each other

So!

We we will calculate stress
at A & C.

• So now!

$$\delta A = \frac{M_x y}{I_x} + \frac{M_y x}{I_y} \text{ comp.}$$

$$\delta C = \frac{M_x y}{I_x} + \frac{M_y x}{I_y} \text{ (Tension)}$$

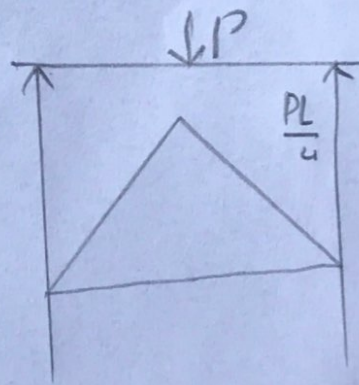
NOW M_x & M_y

$$M_x = \frac{P \cos 60 (16 \times 12)}{4}$$

$$* \quad M_x = 48 P \cos 60$$

$$M_y = \frac{P \sin 60 (16 \times 12)}{4}$$

$$M_y = 48 p \sin 60$$



$$\delta A = \frac{M_{xy}}{I_x} + \frac{M_{yx}}{I_y}$$

$$1200 = \frac{48p \cos 60^\circ \times 3.07}{112.6} + \frac{48p \sin 60^\circ \times 3}{18.7}$$

Solving the Equation

$$P = 1638.6 \text{ lb}$$

Now!

$$\delta c = \frac{M_{xy}}{I_x} + \frac{M_{yx}}{I_y}$$

$$5000 = \frac{48p \cos 60^\circ \times (5.93 \text{ ft})}{112.6} + \frac{48p \sin 60^\circ \times 0.5}{18.7}$$

Solving the Equation.

$$P = 2104.9 \text{ lb}$$

⇒ So the maximum load p applied should be (1638.6 lb) .

Question no 3rd:

Given = $L = 10 \text{ ft}$

• As both sides are hinged

SO! $L_e = L$

• $E = 10.3 \times 10^6$

• Factor of Safety = 2

• $b = 0.75 \text{ inch}$

• $h = 2 \text{ inch}$.

Required data:

Determine Safe load = ?

Solution: As

$$P_{cr} = \frac{\pi^2 EI}{L_e^2}$$

As we know that $I = Ar^2$

$$I = Ar^2$$

$$r = \sqrt{I/A}$$

$$r = \frac{\sqrt{\frac{hb^3}{12}}}{bh} \Rightarrow \sqrt{\frac{b^2}{12}}$$

$$r = \frac{b}{2\sqrt{3}} \Rightarrow \frac{0.75}{2\sqrt{3}}$$

$$r = 0.216 \text{ inch}$$

$$P_{Cr} = \frac{\pi^2 EA}{\left(\frac{L_e}{r}\right)^2}$$

$$\Rightarrow \frac{(3.14)^2 (10.3 \times 10^6) (1.5)}{\left(\frac{10}{0.216}\right)^2}$$

$$P_{Cr} = 853.8343$$

$$\text{Safe load} = \frac{\text{Crippling load}}{\text{factor of safety}}$$

$$\Rightarrow \frac{853.8343}{2}$$

$$\text{Safe Load} \Rightarrow 426.917$$

\Rightarrow For Fixed ended column

$$L_e = L/2 = 10/2$$

$$L_e = 5 \text{ ft}$$

$$P_{cr} = \frac{\pi^2 EA}{(L_e/\gamma)^2} = \frac{(3.14) \times (10.3 \times 10^6)(1.5)}{(60/0.216)^2}$$

$$P_{cr} = 1874.207$$

$$\text{Safe load} = \frac{P_c}{\text{Factor of safety}}$$

$$\text{Safe load} = \frac{1874 \cdot 207}{2} = 987 \cdot 103$$

So! safe load as = $987 \cdot 103$
Ans