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→ 7986

→ Section "A"

→ Sem: → "4th"

→ Structure Analysis

→ Final Paper.

→ 26 - 06 - 2020.



Q No # 1 :->

Answer :->

①

=> Given Data :->



uniform load = 4 k/ft

Mod E = 29×10^3 Ksi

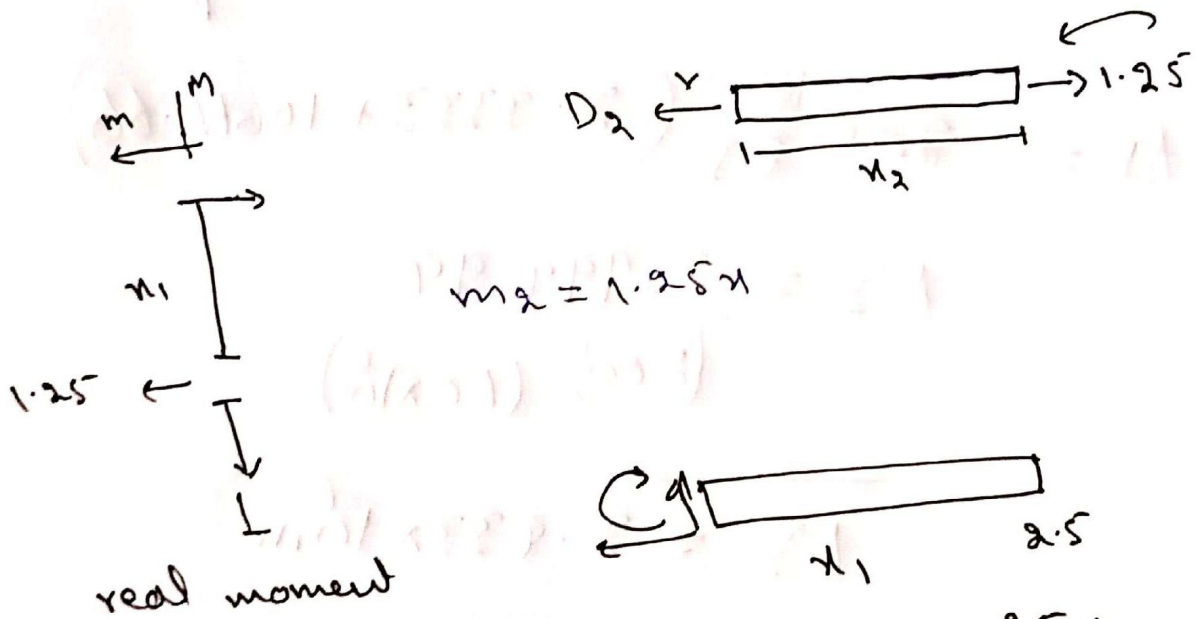
I = 600 in⁴

=> Required :->

Vertical Displacement.

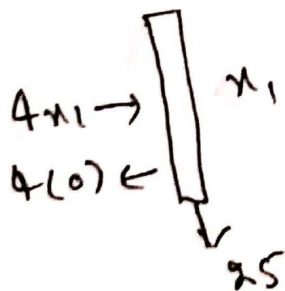
=> Solution :->

Now virtual moment.



$$m_2 = 1.25 x$$

$$m_2 = 2.5 x_2$$



$$(P - T - 0) \Rightarrow$$

$$m'' = \frac{40x_1 - \frac{1}{2} x_1 (x_2)}{40x_1 - 2x_1^2}$$

(2)

Now By virtual work equation.

$$\Delta D_F = \int_0^L \frac{m M du}{E}$$

$$\Delta I = \int_0^{10} (1x_1) \frac{(40x_2 - 2x_1^2)}{E} dx + \int_0^8 \frac{(1 \cdot 25x_2)(25x_2)}{E I} dx$$

$$\Delta I = \frac{1}{E I} \left[\frac{40x^3}{3} - \frac{2x^3}{4} \right]_0^{10} + \left(\frac{31.25}{3} x_2^3 \right) \Big|_0^8$$

$$\Delta I = \frac{1}{E I} (2 \cdot 3333 + 10666.66)$$

$$\Delta I = \frac{33999.99}{(200)(60 \times 10^6)}$$

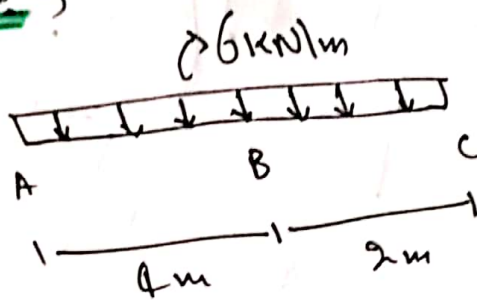
$$\Delta I = 2.833 \times 10^{-6} \text{ in}$$

x ————— x

QNO#2:->

3

Answer:->

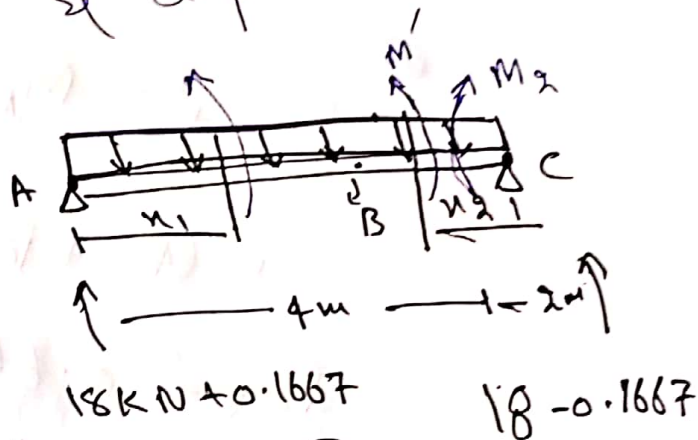


Required:->

slope & displacement at

Point "B".

Solution:->



(a)

$$R_1 + R_2 = 0 \quad \text{--- (1)}$$

(a)

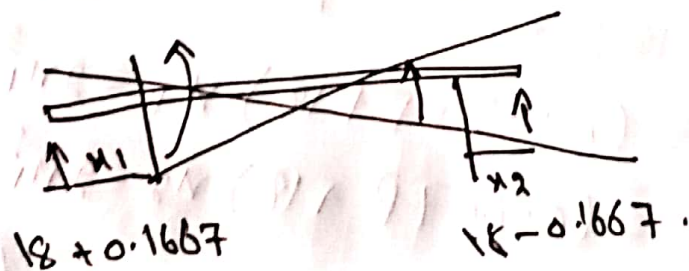
$$\sum M_A = 0 \quad \text{--- (2)}$$

$$1 + R_2 (6) = 0$$

$$\Rightarrow -0.16667 \text{ Put in (1)}$$

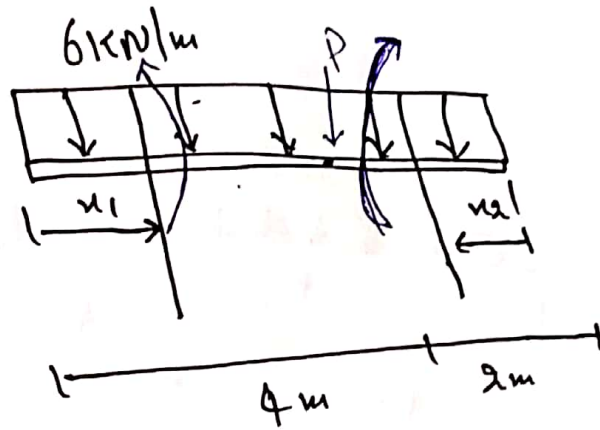
$$R_1 + (-0.16667) = 0$$

$$R_1 = 0.16667 \text{ kN}$$



~~_____~~

(b)



(4)

(b)

$$R_1 + R_2 = 1$$

$$\sum M_A = 0$$

$$-(1)(4) + R_2(6) = 0$$

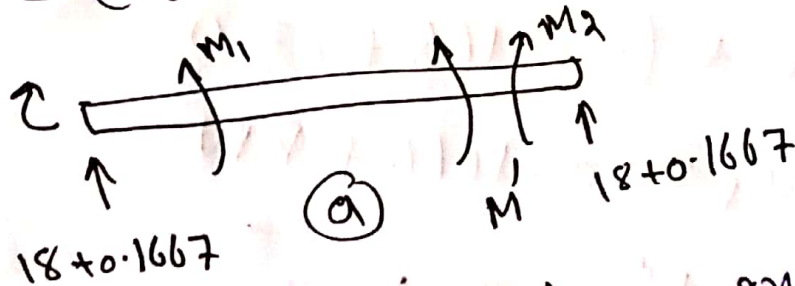
$$R_1 = 0.6667 \text{ kN}$$

$$R_2 = 1 - 0.6667 \text{ kN}$$

$$R_2 = 0.3333 \text{ kN}$$

$$M_1 = (18 + 0.16667M')x_1 - 2x_1^2$$

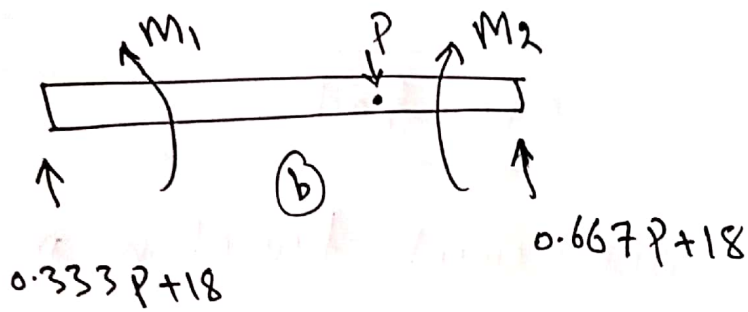
$$M_2 = (18 - 0.6667M')x_2 - 2x_2^2$$



$$M_1 = (0.3333P + 18)x_1 - 2x_1^2$$

$$M_2 = (0.6667P + 18)x_2 - 2x_2^2$$

$$(P - T - 0) \Rightarrow$$



The displacement function shows in the figure "a" above

$$\frac{\partial M_1}{\partial M'} = 0.1667x_1 \text{ and } \frac{\partial M_2}{\partial M'} = 0.1667x_2 -$$

- set $M' = 0$ then

$$M_1 = (18 + 0.1667(0))x_1 - 2x_1^2$$

$$\rightarrow M_1 = (18x_1 - 2x_1^2)$$

$$\rightarrow M_2 = (18x_2 - 2x_2^2)$$

$$\textcircled{Q}B = \int_0^L M \left(\frac{\partial M}{\partial M'} \right) \frac{dx}{EI} = \int_0^L \frac{(18x_1 - 2x_1^2)(0.1667x_1)}{EI} dx_1 + \int_0^L \frac{(18x_2 - 2x_2^2)(0.1667x_2)}{EI} dx_2$$

$$QB = \frac{42.65}{EI} + \frac{6.66}{EI}$$

$$QB = \frac{49.31}{EI}$$

$$QB = \frac{49.31}{200 \times 10^6 \text{ kPa} (0.00006)}$$

$$(P \rightarrow 0) \Rightarrow$$

$$\theta_B = 0.4411 \text{ rad}$$

(6)

→ For the displacement functions are shown in figure "b"

$$\frac{\partial M_1}{\partial P} = 0.333 x_1 \text{ and } \frac{\partial M_2}{\partial P} = 0.6667 x_2 \text{ also}$$

then set $P = 0$

$$M_1 = (18x_1 - 2x_1^2) \text{ KN}\cdot\text{m}$$

$$M_2 = (18x_2 - 2x_2^2) \text{ KN}\cdot\text{m}$$

Thus

$$\Delta_B = \int_0^L M \left(\frac{\partial M}{\partial P} \right) \frac{dx}{EI}$$

~~$$\Delta_B = \int_0^4 (30x_1 - 2x_1^2)(0.333x_1) dx + \int_0^2 (30x_2 - 2x_2^2)(0.6667x_2) dx$$~~

$$\Delta_B = \frac{\int_0^4 (30x_1 - 2x_1^2)(0.333x_1) dx}{EI} + \frac{\int_0^2 (30x_2 - 2x_2^2)(0.6667x_2) dx}{EI}$$

$$\Delta_B = \frac{218.5}{EI} \Rightarrow \frac{218.5}{(200 \times 10^6)(0.00008)}$$

$$= 0.018 \text{ m}$$

(or) 18 mm

Ans



Q No #3 :->

Answer :->

(7)

Given Data :->

Uniform Load " w_0 " = 400 lb/ft

$h = 10$ ft

$L = 15$ ft

Required Data :->

Equation of Curve and force in cable = ?

Solution :->

we know that

$$y = \frac{w_0}{2L^2} x^2$$

Putting the values

$$y = \frac{10}{(15)^2} x^2 = 0.044 x^2$$

$$y = \frac{10}{(15)^2} x^2 = 0.044 x^2$$

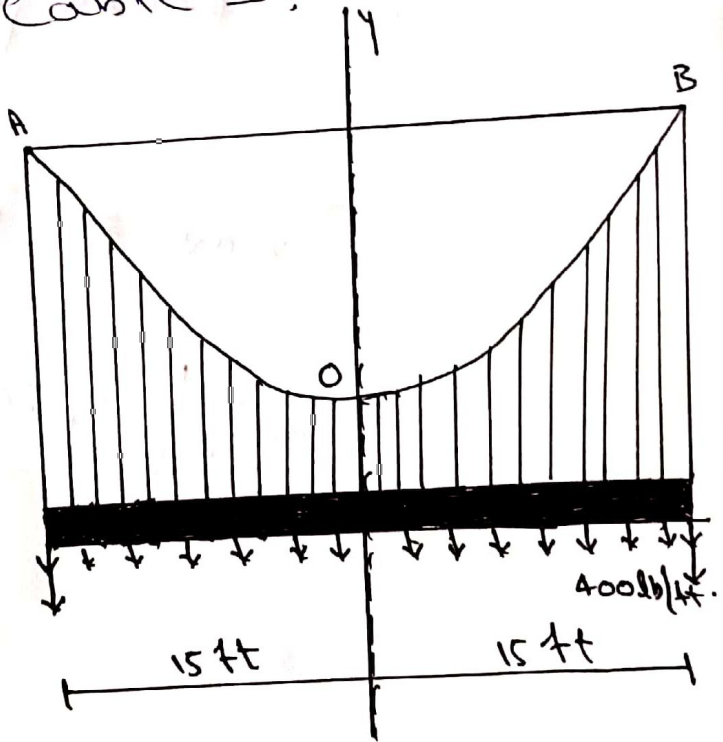
$$T_0 = FH = \frac{w_0 L^2}{2h} \Rightarrow \frac{400 \times (15)^2}{2 \times 10}$$

$$T_0 = 4500 \text{ lb}$$

$$\boxed{= 4.5 \text{ K}}$$

$$T_B = T_{\text{max}} = \sqrt{(FH)^2 + (w_0 L)^2}$$

$$(P - T - 0) \Rightarrow$$



$$T_B = T_{max} = \sqrt{(FH)^2 + (WOL)^2}$$
$$= \sqrt{(4500)^2 + (400 \times 15)^2}$$

(8)

Now "T_{max}" By another equation

$$T_B = T_{max} = WOL \sqrt{1 + \left(\frac{L}{2h}\right)^2}$$

$$\Rightarrow: 400 \times 15 \sqrt{1 + \left(\frac{15}{2 \times 10}\right)^2}$$

$$T_{max} = 7500 \text{ lb}$$

$$\Rightarrow \boxed{= 7.5 \text{ K}}$$



Q No # 4 :->

9

Answer :->

Given Data :->

Uniform load = 30 kN/m

Required :->

Internal moment at D = ?

Solution :->

Dividing into two members
AB and BC.

AB :->

$\sum M_A = 0$

$B_x(5) + B_y(8) - 240(4) = 0 \quad \text{--- (a)}$

BC :->

$\sum M_C = 0$

$-B_x(5) + B_y(8) + 240(4) = 0 \quad \text{--- (b)}$

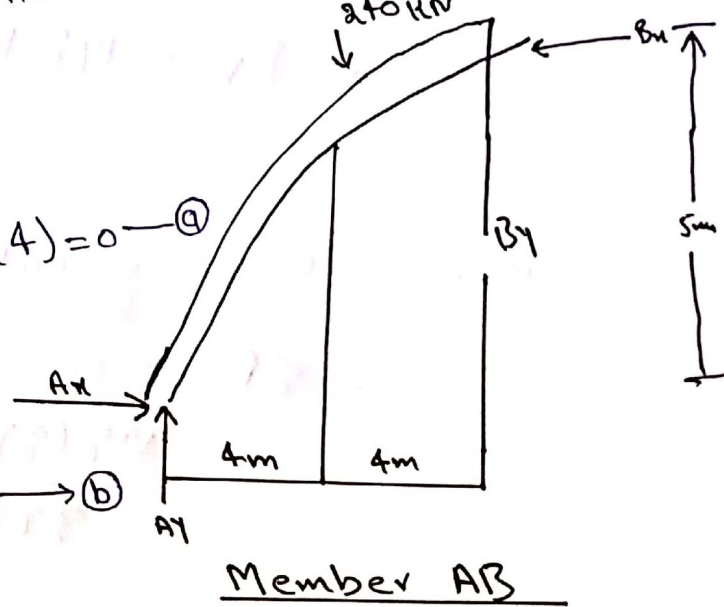
Adding eq (a) and (b)

~~$B_x(5) + B_y(8) - 240(4) = 0$~~

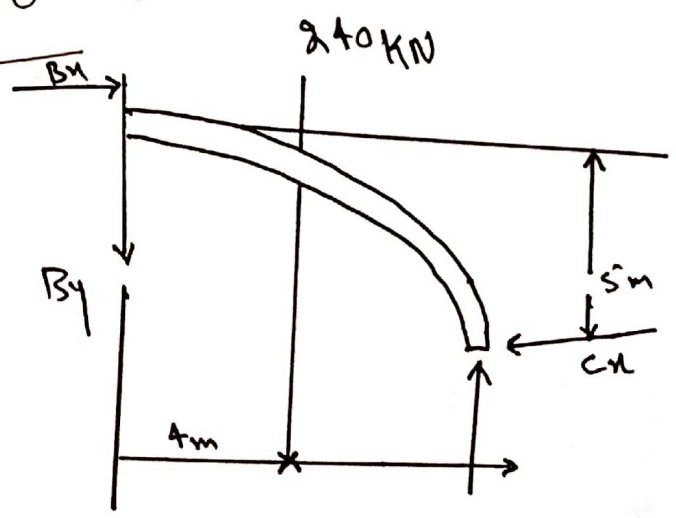
~~$-B_x(5) + B_y(8) + 240(4) = 0$~~

$0 + 2B_y(8) + 0 = 0$

(P-T-O) =>



Member AB



Member BC

$$2B_y(s) = 0$$

$$\Rightarrow B_y = 0 \text{ kN}$$

(10)

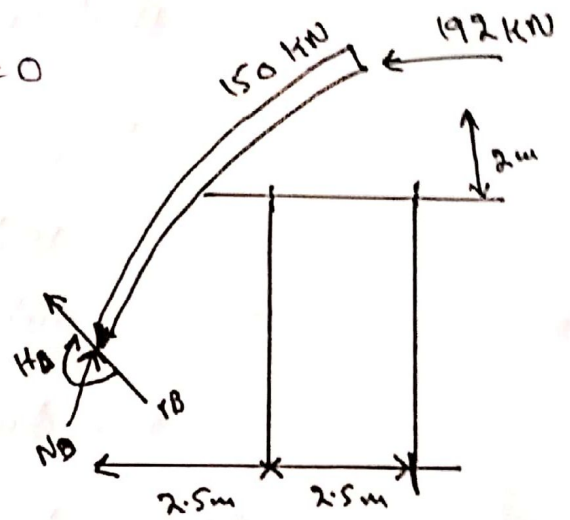
Putting the value of "B_y" in eq (b)

$$\text{eq (b)} \Rightarrow -B_x(s) + 0(s) + 960 = 0$$

$$B_x(s) = 960$$

$$\frac{B_x(s)}{(s)} = \frac{960}{(s)}$$

$$B_x = 192 \text{ kN}$$



Member DB

"Now at segment DB"

$$\sum M_D = 0$$

$$192(2) - 150(2.5) - M_D = 0$$

$$384 - 375 - M_D = 0$$

$$9 - M_D = 0$$

$$\Rightarrow M_D = 9 \text{ kN}\cdot\text{m}$$



The End.