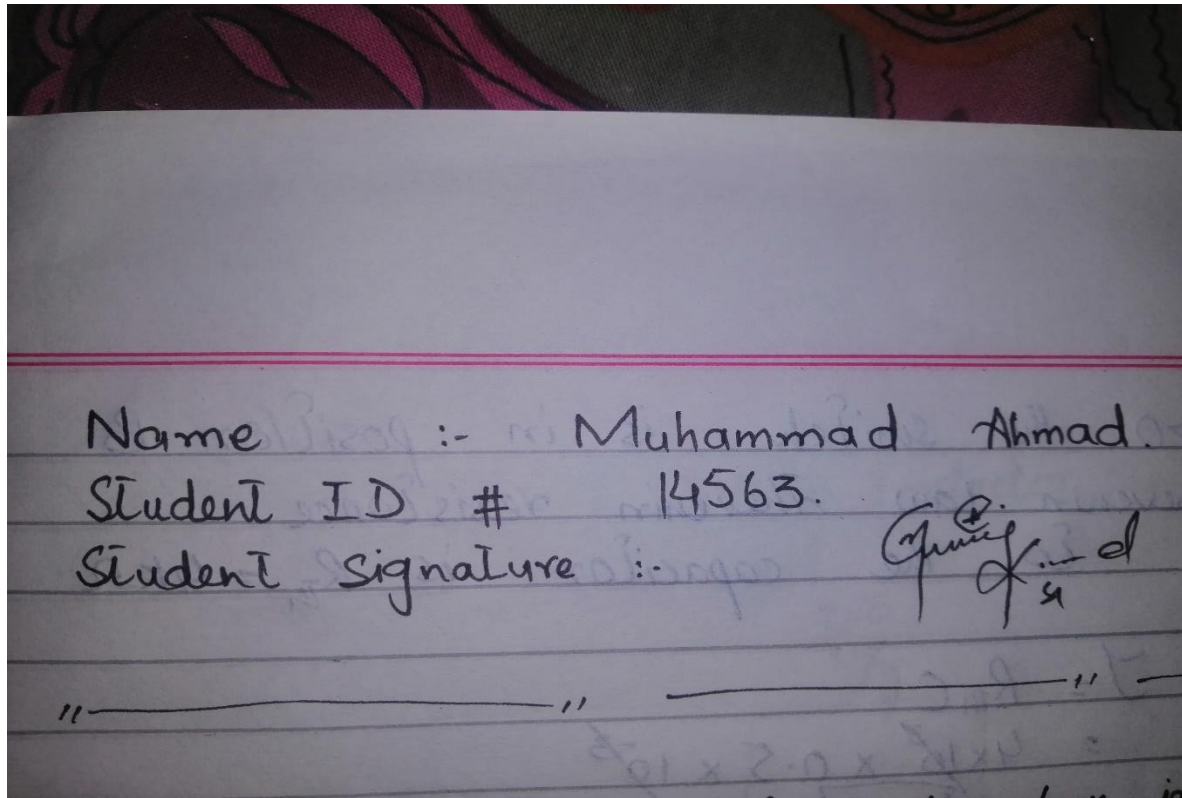


Department of Electrical Engineering

Course Title: Signal And System

Module: 4<sup>th</sup> semester

Student Detail



Name :- Muhammad Ahmad.

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Student signature :-

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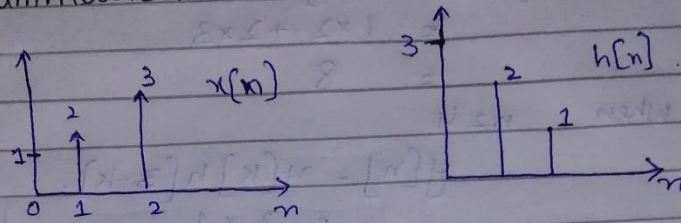
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(1)

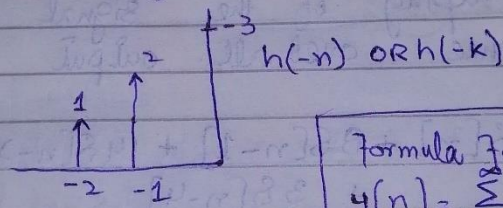
Q No 1 @ :- Evaluate  $y[n]$  using Convolution Summation.



Solve:-

Step No 1.

Reflect signal  $h[x]$  to  $h[k]$ .



Formula for convolution

$$y[n] = \sum_{k=-\infty}^{\infty} x[k] h[n-k]$$

As we know,

$$y[0] = \cancel{x[0]} \cdot 0$$

when  $n < 0$ .

Now for  $n \geq 0$ ,

$$\begin{aligned} y[0] &= x[0] h[0-0] \\ &= 1 \times 3 \\ &= 3 \end{aligned}$$

when  $n = 1$ .

$$\begin{aligned} y[1] &= x[1] \cdot h[1-1] \\ &= 1 \times 2 + 2 \times 3 \\ &= 8 \end{aligned}$$

when  $n = 2$ .

$$\begin{aligned} y[2] &= x[2] h[2-2] \\ &= 1 \times 1 + 2 \times 2 + 3 \times 3 \\ &= 1 + 4 + 9 = 14 \end{aligned}$$

②

when  $n=3$

$$y[n] = \sum_k x[k] \cdot h[n-k]$$
$$= 1 \times 2 + 2 \times 3$$
$$= 8$$

when  $n=4$

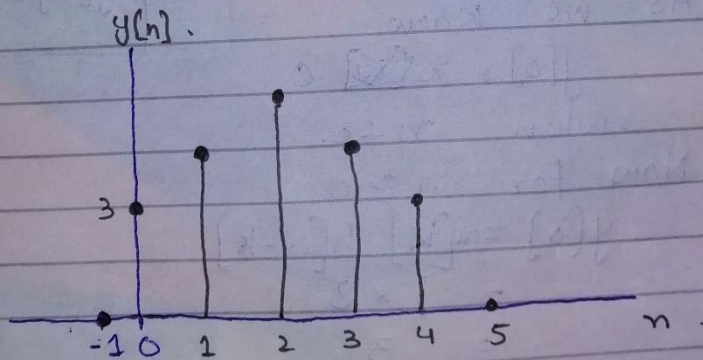
$$y[n] = \sum_k x[k] \cdot h[3-k]$$
$$= 3 \times 1$$
$$= 3$$

when  $n > 4$

$$y[n] = 0$$

Overlapping of the signal  $x[k]$  &  $h[n-k]$   
Hence, over all, output  $y[n]$ .

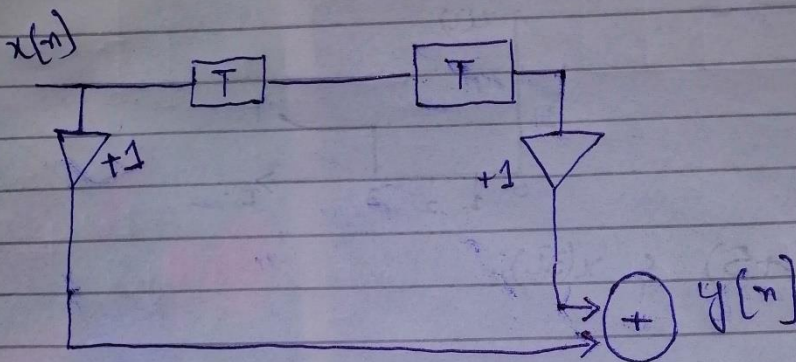
$$y[n] = 3\delta[n] + 8\delta[n-1] + 14\delta[n-2] + 8\delta[n-3] + 3\delta[n-4]$$



(3)

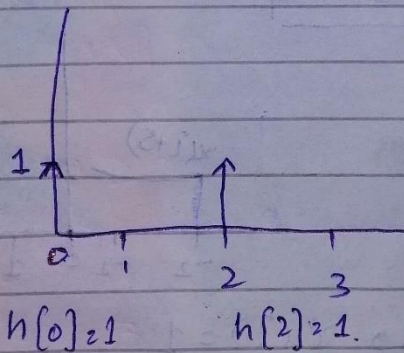
QNO 1(b)

Sketch the diagram for the given system.



$$h[n] = \delta[n] + \delta[n-2]$$

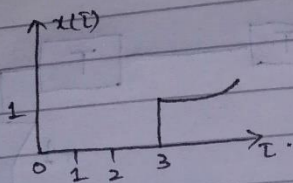
$$h[0] = 1; h[1] = 0; h[2] = +1 \text{ and } h[n] = 0 \text{ for } n \geq 3$$



(4)

QNo2 part a)

QNo2a) Sketch the L-transformed versions for the signal  $x(l)$  mentioned



①  $x(l+5)$  &  $x(3l)$ .

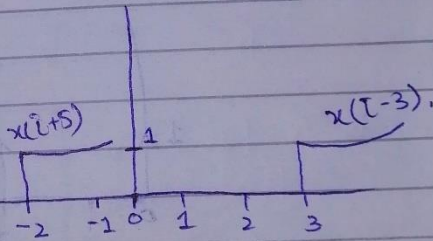
Sol:-

$$x(l+5)$$

$$l = 3 \rightarrow x(l) = 1$$

$$Al \quad l+5 = 3 \rightarrow x(l) = 1$$

$$\boxed{l = -2}$$



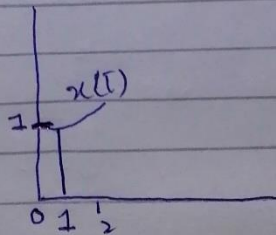
Sol

$$l = 3 \rightarrow x(l) = 1$$

$$Al \quad 3l = 3 \rightarrow x(l) = 1$$

$$l = 1$$

$$\boxed{l = 1}$$



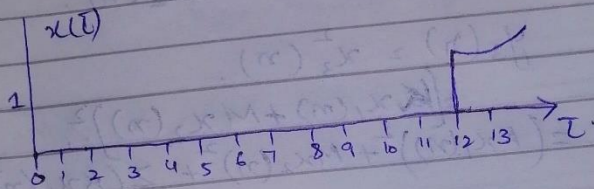
(ii)  $x(\bar{l}/4)$  &  $x(\bar{l}-2)$ .

$$A\bar{l} = \bar{l} = 3, \quad x(\bar{l}) = 1.$$

$$A\bar{l} = \bar{l}/4 = 3, \quad x(\bar{l}/4) = 1.$$

$$\bar{l} = 3 \times 4$$

$$\boxed{\bar{l} = 12}$$

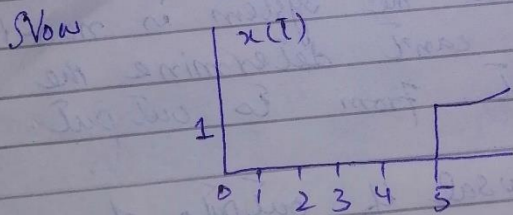


$$x(\bar{l}-2)$$

$$A\bar{l} = \bar{l} = 3, \quad x(\bar{l}) = 1.$$

$$A\bar{l} = \bar{l}-2 = 3, \quad x(\bar{l}) = 1.$$

$$\boxed{\bar{l} = 5}$$



QNo2:- Outline the given system as invertible or non-invertible, linear or non linear, causal or non causal. Given Reason.

Ans:-  $y[n] = x^2[n]$ .

Sol:- Let  $x_1(\bar{l})$  be the input to the

system then,

$$y_1(n) = x_1^2(n).$$

Similarly the response to the input.

$$x_2(n)$$

$$y_2(n) = x_2^2(n).$$

Let another input  $x_3(n)$

$$x_3(n) = ax_1(n) + bx_2(n).$$

Now,

$$y_3(n) = x_3^2(n).$$

$$= [ax_1(n) + bx_2(n)]^2 \\ = (ax_1(n))^2 + Mx_2(n)^2 + 2(ax_1(n) \cdot bx_2(n))$$

$$y_3(n) = \cancel{a}x_1^2(n) + Mx_2^2(n)$$

↳ As super position principle is not satisfied, the given system is non linear. Also the system is non-invertible because we can't determine the sign of input from output.

↳ A system is causal if output of any time depends on the value of input.

(7)

(ii)  $y[n] = x[n+2]$ .

A system that whose output involves future or anticipated values of the input is said to be non-causal system.

$$y[n] = x[n+1]$$

$$y[n] = x[n] + x[n+2]$$

↑                    ↑  
Non-causal system.

QNo 3 Fill in the blanks.

Answer:-

If a time shift in the input signal results in an identical times shift in the output signal, the system is said to be

Time Invariance

————— " —————

→ This system is also linear because it satisfied the super position.