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Section " 'A'

Subject " Hydraulic Engineering

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Q No 2 Part "A"
 Let suppose a rectangular channel, discharge
 R lit/sec of water into 8m wide
 open with zero slope. Mean velocity is
 $R = 200$ ft/sec

Given:-

$$\begin{aligned} \text{Discharge (Q)} &= 7819 \text{ Lit/sec} \\ &= \frac{7819}{1000} = 7.819 \text{ m}^3/\text{sec} \end{aligned}$$

$$\text{Breadth (b)} = 8 \text{ m}$$

$$\begin{aligned} \text{Mean velocity (V)} &= \frac{7819 - 200}{8} \\ &= \frac{7619}{8} = 952.375 \text{ ft/sec} \\ &= \frac{952.375}{3.28} = 290.358 \text{ m/sec} \end{aligned}$$

Required:-

- 1) Height of hydraulic jump (in meter)
- 2) Power absorbed due to hydraulic jump (in kW).

1) Height of hydraulic jump :-

specific energy

(2)

As we know that "q" → discharge per unit breadth

$$q = \frac{Q}{b} = \frac{7.819}{8} = \boxed{0.977 \text{ m}^2/\text{sec}}$$

⇒ Critical depth:

$$y_c = \left(\frac{(q)^2}{g} \right)^{\frac{1}{3}} = \left(\frac{(0.977)^2}{9.81} \right)^{\frac{1}{3}}$$

$$\boxed{y_c = 0.468 \text{ m}}$$

⇒ critical velocity:

we know that,

$$q = v y$$

$$v = \frac{q}{y} \Rightarrow v_c = \frac{q}{y_c}$$

$$v_c = \frac{0.977}{0.468} \Rightarrow \boxed{2.087 \text{ m/sec}}$$

Depth of water on upstream side of Hydraulic Jump:

by discharge formula,

$$Q = A v$$

$$\Rightarrow Q = (b y) v \Rightarrow y = \frac{Q}{b v}$$

$$y_1 = \frac{Q}{v_c \times b} \Rightarrow \frac{7.819}{2.087 \times 8} \Rightarrow \boxed{y_1 = 0.468}$$

3

by formula:

water depth on Down Stream is,

$$y_2 = -y_1/2 + \sqrt{\frac{b_1^2}{4} + \frac{2y_1V_1^2}{g}}$$

$$y_2 = -\frac{0.468}{2} + \sqrt{\frac{(0.468)^2}{4} + \frac{2(0.468)(2.089)^2}{9.81}}$$

$$= -0.234 + 0.537077$$

$$y_2 = 0.489 \text{ m}$$

Differen in Depth:

$$\Delta y = y_2 - y_1 \\ = 0.489 - 0.468$$

$$\Delta y = 0.02$$

Also by formula:

$$Q_1 = Q_2$$

$$A_1 V_1 = A_2 V_2$$

$$(b_1 y_1) V_1 = (b_2 y_2) V_2 \quad \text{if } b_1, b_2 = b$$

$$(y_1) V_1 = (y_2) V_2$$

$$y_1 \cdot V_1 = y_2 \cdot V_2$$

(4)

$$v_2 = \frac{y_1 v_1}{y_2} = \frac{0.468 \times 2383.8}{0.489}$$

$$v_2 = 2281.46$$

Now $\Delta E = E_1 - E_2$

$$(E_1 - E_2) = \left(y_1 + \frac{v_1^2}{2g} \right) - \left(y_2 + \frac{v_2^2}{2g} \right)$$

$$= \left(0.468 + \frac{(2383.8)^2}{2(9.81)} \right) - \left(0.489 + \frac{(2281.46)^2}{2(9.81)} \right)$$

$$= 289,628.07 - 265279.63$$

$$E_1 - E_2 = 24,348.44$$

Power Dissipation In Hydraulic Jump
by using formula :-

$$\Delta P = \rho g Q (E_1 - E_2)$$

$$\Delta P = (1000)(9.81)(7.819)(24348.44)$$

$$\Delta P = 1,867,632,237.65 \text{ W}$$

$$\Delta P = 1,867,632,237.65 \text{ kW}$$

(5)

Q No #1 Part 'B'

A sluice gate controls the flow in a channel of width of 4m if the discharge is Q ft³/sec and the upstream and downstream water depth is 2.9m and 1.1m respectively calculate the downstream velocity. Also state the type of flow at upstream velocity and downstream side using any equation.

Given data:

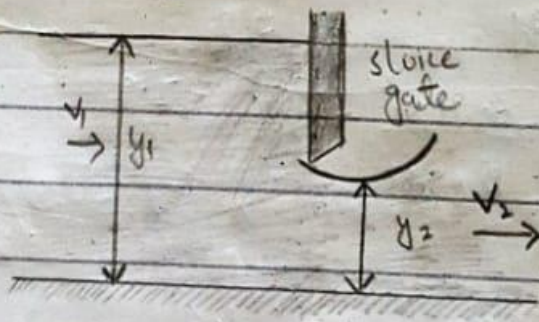
$$\text{channel width} = b = 4\text{m}$$

$$\text{discharge } Q = 7819 \text{ ft}^3/\text{sec}$$

$$Q = \frac{7819}{1000} = 7.819 \text{ m}^3/\text{sec}$$

$$\text{depth of upstream} = 2.9 \text{ m}$$

$$\text{depth of downstream} = 1.1 \text{ m}$$



Solution:

Downstream velocity:

(6)

As from specific energy equation

$$E_1 = E_2$$

$$y_1 + \frac{v_1^2}{2g} = y_2 + \frac{v_2^2}{2g} \rightarrow \text{(a)}$$

Also we know that

$$Q = AV$$

$$A_1 v_1 = A_2 v_2 \quad \Rightarrow b_1, b_2 = b$$

$$b \cdot y_1 \cdot v_1 = b \cdot y_2 \cdot v_2$$

$$v_2 = \frac{y_1 v_1}{y_2} = \frac{2.9 v_1}{1.1}$$

$$v_2 = 2.63 v_1 \rightarrow \text{(1)}$$

put in equation (a)

$$y_1 + \frac{v_1^2}{2g} = y_2 + \frac{v_2^2}{2g}$$

$$\frac{2.9 + \frac{v_1^2}{2g}}{2g} = \frac{1.1 + \frac{(2.63v_1)^2}{2g}}{2g}$$

$$\frac{v_1^2}{2 \times 9.81} - \frac{6.91 v_1^2}{2 \times 9.81} = 1.1 - 2.9$$

$$\frac{v_1^2 - 6.91 v_1^2}{19.62} = 1.8$$

$$+ 5.91 v_1^2 = + (1.8) (19.62)$$

$$v_1^2 = \frac{(1.8)(19.62)}{5.91}$$

(7)

$$\sqrt{v_1^2} = \sqrt{\frac{(1.8)(19.62)}{5.91}}$$

$$v_1 = 2.44 \text{ m/sec}$$

put the value of v_1 in eq (i)

$$v_2 = 2.63(v_1)$$

$$v_2 = 2.63(2.44)$$

$$v_2 = 6.41 \text{ m/sec}$$

Type of flow upstream side:-

$$F_{r1} = \frac{v}{\sqrt{g y_1}} = \frac{2.44}{\sqrt{9.81 \times 2.91}}$$

$$F_{r1} = 0.45$$

$F_{r1} < 1 \rightarrow$ sub critical flow

Type of flow downstream side:-

$$F_{r2} = \frac{v_2}{\sqrt{g y_2}} = \frac{6.41}{\sqrt{9.81 \times 1.11}}$$

$$F_{r2} = 1.95$$

$F_{r2} > 1 \rightarrow$ super critical flow

(8)

Q No # 02 Part "A"

What is the minimum height (in unit meter) of broad crested weir if it is to function critical depth on the crest if water flows along a rectangular channel at depth of 1.8 m with discharge of Q ft²/sec. The channel width is 66 ft.

Given data:-

$$\text{channel depth} = 1.8 \text{ m}$$

$$\text{discharge } Q = \frac{7819}{(3.28)^3} = 221.5 \text{ m}^3/\text{sec}$$

$$\text{depth of channel} = 1.8 \text{ m}$$

$$\text{width of channel} = 66 \text{ ft} = 20.1 \text{ m}$$

Required

$$\text{weir height} = P = ?$$

Solution

As we know that

$$Q = AV$$

$$V = \frac{Q}{A} \Rightarrow V = \frac{Q}{b \times y}$$

$$V = \frac{221.57}{20.1 \times 1.8} = 6.12 \text{ m/sec}$$

$$V = 6.12 \text{ m/sec}$$

(9)

Critical depth:-

$$y_c = \left(\frac{Q^2}{g}\right)^{1/3}$$

$$Q = \frac{\pi}{6} \times \frac{2.21 \times 57}{2011} = 11.02 \text{ m}^3/\text{sec}$$

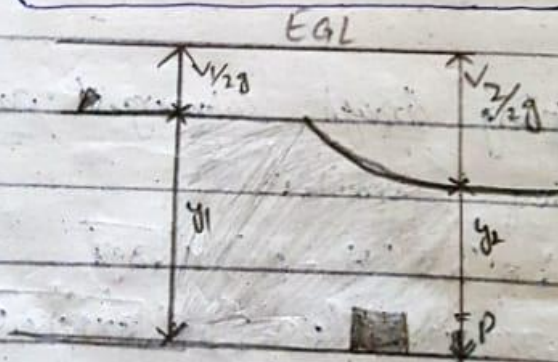
$$y_c = \left(\frac{(11.02)^2}{9.81}\right)^{1/3}$$

$$y_c = 2.31 \text{ m}$$

Also $V = \sqrt{gy}$

$$V_c = \sqrt{gy_c} = \sqrt{9.81 \times 2.31}$$

$$V_c = 4.76 \text{ m/sec}$$



According to the given figure

$$\frac{V_1^2}{2g} + y_1 = \frac{V_2^2}{2g} + y_c + P$$

$$\frac{(6.12)^2}{2 \times 9.81} + 1.8 = \frac{(4.76)^2}{2 \times 9.81} + 2.31 + P$$

(10)

$$1.908 + 1.8 = 1.154 + 2.31 + P$$

$$P = 0.24 \text{ m}$$

Q No # 2 Part "B"

Given data:

$$\text{breadth} = b = 2.8 \text{ m}$$

$$\text{depth} = d = 1.5 \text{ m}$$

$$H_1 = 5 \text{ m}$$

$$H_2 = 5 + 1.5 = 6.5 \text{ m}$$

$$H = 5 + 0.6 = 5.6 \text{ m}$$

$$cd = 0.7819$$

Required

$$\text{discharge} = Q = ?$$

Solution:

discharge through submerged portion

by using formula:-

$$Q_1 = cd \times b \times (H_2 - H_1) \times \sqrt{2gH}$$

$$Q_1 = 0.7819 \times 2.8 \times (6.5 - 5) \times \sqrt{2 \times 9.81 \times 5.6}$$

$$Q_1 = 20.64 \text{ m}^3/\text{sec}$$

Free portion:-

$$Q_2 = \frac{2}{3} cd \times b \sqrt{2g} (H^{3/2} - H_1^{3/2})$$

$$Q_2 = \frac{2}{3} (0.7819 \times 2.8 \sqrt{2 \times 9.81} [(5.6)^{3/2} - (5)^{3/2}])$$

$$Q_2 = 13.38 \text{ m}^3/\text{sec}$$

(11)

Total discharge

$$Q = Q_1 + Q_2$$

$$Q = 20.64 + 13.38$$

$$Q = 34.02 \text{ m}^3/\text{sec}$$

Q No # 3 Part "A"

calculate:-

- 1) The loss of head due to sudden enlargements
- 2) The power lost due to sudden enlargement
- 3) The pressure in the smaller pipe (pipe is horizontal)

Given data:-

$$d_1 = R - 200 \quad d_2 = R + 3000$$

$$d_1 = 7819 - 200 \quad d_2 = 7819 + 3000$$

$$d_1 = 7619 \text{ mm} \quad d_2 = 10819 \text{ mm}$$

$$\text{discharge} = 0.95 \text{ m}^3/\text{sec}$$

$$\text{pressure in larg pipe} = R + 800$$

$$= 7819 + 800$$

$$= 8619 \text{ N/m}^2$$

Solution

Head lost due to sudden enlargement

$$d_1 = 7619 \text{ mm} = 7.619 \text{ m}$$

$$A_1 = \frac{\pi}{4} d^2 = \frac{\pi}{4} (7.619)^2 = 47.9 \text{ m}^2$$

(2)

$$d_2 = 10.819 = 10.819 \text{ m}$$

$$A = \frac{\pi}{4} (10.819)^2 = 91.8 \text{ m}^2$$

As we know that

$$Q = AV$$

$$v_1 = Q/A_1 \Rightarrow 0.95 / 47.9 = 0.019 \text{ m/sec}$$

$$v_2 = Q/A_2 \Rightarrow 0.95 / 91.8 = 0.010 \text{ m/sec}$$

As sudden enlargement:-

$$h_e = \left(1 - \frac{A_1}{A_2}\right)^2 \times \left(\frac{v_1 - v_2}{2g}\right)^2$$

$$h_e = \left(1 - \frac{47.9}{91.8}\right)^2 \times \left(\frac{0.019 - 0.010}{2 \times 9.81}\right)^2$$

$$h_e = 9.44 \times 10^{-7} \text{ m}$$

Power loss due to sudden enlargement

As we know that

$$P = \rho g Q h_e$$

$$P = (1000)(9.81)(0.95)(9.44 \times 10^{-7})$$

$$P = 8.79 \times 10^{-3} \text{ N}$$

Pressure in smaller pipe :-

using Bernoulli equation:

$$\frac{P_1}{\rho g} + \frac{v_1^2}{2g} = \frac{P_2}{\rho g} + \frac{v_2^2}{2g} + h_e$$

(13)

$$\frac{P_i}{(1000)(9.81)} + \frac{(0.019)^2}{2 \times 9.81} = \frac{(8.7 \times 10^3)^2}{2 \times 9.81}$$
$$= \frac{8619}{9810} + \frac{(0.019)^2}{2 \times 9.81} + 9.44 \times 10^{-7}$$

$$\frac{P_i}{9810} + 0.000177 = \frac{8619}{9810} + 0.0004905 + 0.000000944$$

$$\frac{P_i}{9810} = \frac{8619}{9810} + 0.0004905 + 0.000000944 - 0.000177$$

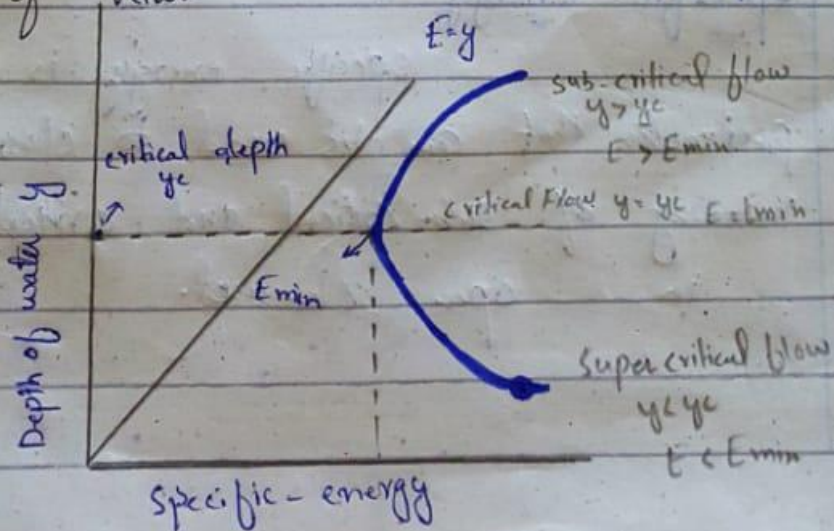
$$\frac{P_i}{9810} = 0.883$$

$$P_i = 8665.39 \text{ N/m}^2$$

Q No H 03 Part .B:

What does the curve indicate How its obtain the below Figur from each and every point

of View:-



Blue Curve:

from the above figure the blue curve is the 3 degree polynomial curve which show the flow is critical, sub critical and super critical, sub critical and super critical flow. the middle point show the depth of water is equal to the critical depth corresponding to minimum energy so the flow is critical flow.

$$y = y_c \text{ and } E = E_{min}$$

The top point show the depth of water is greater than the critical depth

$$y < y_c \text{ and } E < E_{min}$$

The lower point show the depth of water is less than the critical depth

$$y > y_c \text{ and } E > E_{min}$$

Specific Energy

specific energy is a parameter that can be used to classify the meaning of sub critical and critical flow in open channel.