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Sec: B

Subject: Probability

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2166⁹

946260 - 915 su?

Q1

Compute and analyse the result of least regression and co-efficient of correlation of Y on X

SOLUTION:

X	Y	XY	X ²	Y ²
53	30 20	1060	2809	400
62	20 32	1984	3844	1024
57	30 45	2565	3249	2025
71	45 60	4260	5041	3600
78	80 80	6240	6054	6400
88	100	8800	7744	10000
86	120	10320	7396	14400
87	140	12180	7596	19600
96	160	15360	9216	25600
91	180	16360	8281	32400
94	200	19800	8836	40000
94	210	11980	8836	44100

$\Sigma X = 957$
 $\Sigma Y = 1347$
 $\Sigma XY = 110209$
 $\Sigma X^2 = 78902$
 $\Sigma Y^2 = 199549$

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$$y = a + bu \quad \text{--- (a)}$$

$$= \bar{y} - b\bar{u} \quad \text{--- (b)}$$

$$\bar{y} = \frac{\sum \bar{y}}{n} = \frac{1347}{12} = 112.25 \quad \text{(c)}$$

$$\bar{u} = \frac{\sum x}{n} = \frac{957}{12} = 79.57$$

where

$$b = \frac{n \sum xy - \sum x \sum y}{n \sum x^2 - (\sum x)^2}$$

$$b = \frac{12(109229) - (957)(1347)}{12(78905) - (957)^2}$$

$$b = \frac{21669}{31211}$$

$$b = 0.69$$

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$$a = \bar{y} - b\bar{x}$$

$$112.25 - 0.69(79.57)$$

$$a = 57.34$$

(ii) Co-efficient of co-relation

$$r = \frac{n(\sum xy) - \sum x \sum y}{\sqrt{[n\sum x^2 - (\sum x)^2][n\sum y^2 - (\sum y)^2]}}$$

$$\frac{12(110209) - (957)(1347)}{\sqrt{[12(78902) - (957)^2][12(99549) - (1347)^2]}}$$

$$r = 0.00015$$

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Question 2(a)

A box contains 4 red, 4 white and 5 green balls.

- (i) all of different colour
- (ii) all of same colour

Solution:

$$n(S) = \binom{13}{3} = 286$$

Let

A = Denote all of different colour

$$n(A) = \binom{4}{1} \binom{4}{1} \binom{5}{1} = 4 \times 4 \times 5 = 80$$

$$P(A) = \frac{n(A)}{n(S)} = \frac{80}{286} = 0.28$$

28% chance all will be different

B all denote same colour

$$n(B) = \binom{4}{3} \text{ or } \binom{4}{3} \text{ or } \binom{5}{3}$$

$$\binom{4}{3} + \binom{4}{3} + \binom{5}{3} = 4 + 4 + 10 = 18$$

$$P(B) = \frac{18}{286} \approx 0.063$$

6.3% chance all are same

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Q2 Part (b)

12 eggs in a refrigerator ---

(i) exactly one is bad

(ii) at least one is bad

SOLUTION:

$$n(S) = \binom{12}{4} = 495$$

A = Denote only one is bad

$$= \binom{2}{1} \binom{10}{3} = 2 \times 120 = 240$$

$$P(A) = \frac{240}{495} = 0.48$$

48% chance

Notes

let

$B =$ at least one is bad

$$= \binom{2}{1} \binom{10}{3} + \binom{2}{2} \binom{10}{2}$$

$$= 285$$

$$P(B) = \frac{n(B)}{n(S)}$$

$$= \frac{285}{495} = 0.58$$

58% chance at least one is bad

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QNO3

following are the score made by batsman A, B and C.

A	12	15	6	73	7	88	199	36	84	29
B	47	12	76	48	4	88	37	48	13	39
C	15	23	52	4	24	88	74	52	13	4

Find range of A, B and C.

Who is more consistent?

Compare A with B, B with C and A with C.

SOLUTION:

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A	B	C
12	47	15
15	12	23
6	76	52
73	48	4
7	4	24
88	88	88
199	37	74
36	48	52
84	13	13
29	3	4

$$\text{Range} = X_m - X_o$$

$$\begin{aligned} \text{Range of A} &= X_m - X_o \\ &= 199 - 6 \\ &= 193 \end{aligned}$$

$$\begin{aligned} \text{Range of B} &= X_m - X_o \\ &= 88 - 3 \\ &= 85 \end{aligned}$$

$$\begin{aligned} \text{Range of C} &= X_m - X_o \\ &= 88 - 4 \\ &= 84 \end{aligned}$$

Batsman A		Batsman B		Batsman C	
X	X ²	Y	Y ²	Z	Z ²
12	144	47	2209	15	225
15	225	12	144	23	529
6	36	76	5776	52	2704
73	5329	48	2304	4	16
7	49	4	16	24	576
88	7744	88	7744	88	7744
199	39601	37	1369	74	5476
36	1296	48	2304	52	2704
84	7056	13	169	13	169
29	841	3	9	4	16
$\Sigma X = 549$	$\Sigma X^2 = 62321$	$\Sigma Y = 376$	$\Sigma Y^2 = 22044$	$\Sigma Z = 349$	$\Sigma Z^2 =$

20157

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Batsman A =

$$\bar{x} = \frac{\sum x}{n} \quad \because n = 10$$

$$= \frac{549}{10} = 54.9$$

$$S_x = \sqrt{\frac{\sum x^2}{n} - \left(\frac{\sum x}{n}\right)^2}$$

$$= \sqrt{\frac{62321}{10} - \left(\frac{549}{10}\right)^2}$$

$$S_{\bar{x}} = 56.72$$

$$C.V = \frac{56.72 \times 100}{\bar{x}} = \frac{56.72}{54.9}$$

$$C.V = 1.03 \times 100$$

ate:

$$C.V = 103.31$$

Batsman B

$$Y = \frac{\sum Y}{n} = \frac{376}{10} = 37.6$$

$$S_y = \sqrt{\frac{\sum Y^2}{n} - \left(\frac{\sum Y}{n}\right)^2}$$

$$= \sqrt{\frac{22044}{10} - \left(\frac{376}{10}\right)^2}$$

$$= \sqrt{2204.4 - 1413.76}$$

$$= 28.11$$

$$C.V = 28.11 \times 100$$

$$= 37.6$$

$$= 74.76\%$$

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Batsman C =

$$z = \frac{\sum z}{n} = \frac{349}{10} = 34.9$$

$$s_z = \sqrt{\frac{\sum z^2}{n} - \left(\frac{\sum z}{n}\right)^2}$$

$$= \sqrt{\frac{20159}{10} - \left(\frac{349}{10}\right)^2}$$

$$= \sqrt{2015.9 - 1218.01}$$

$$\sqrt{797.9}$$

$$= 28.24$$

C.V

$$\frac{s_z}{z}$$

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$$= \frac{28.24}{34.9} \times 100$$

$$= 80.91$$

Batsman B is more consistent
as its value of coefficient of
variance is smallest

Compare A with B

B is consistent

Compare B with E

B is more consistent

Compare A with C

C is more consistent