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PAPER: BIO STATISTIC

EXAM: FINAL

SUBMITTED TO: SIR ANWAR SHAMIM

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QUESTION No 1

PART : A

X	Y	X^2	Y^2	XY
3	25	9	625	75
4	24	16	576	96
5	20	25	400	100
6	20	36	400	120
7	19	49	361	133
8	17	64	289	136
9	16	81	256	144
10	13	100	169	130
11	10	121	100	110
12	8	144	64	104
$\Sigma = 76$	$\Sigma = 172$	$\Sigma = 670$	$\Sigma = 3240$	$\Sigma = 1148$

Formula For Correlation Coefficient.

$$r = \frac{n \sum xy - \sum x \sum y}{\sqrt{\{n \sum x^2 - (\sum x)^2\} \{n \sum y^2 - (\sum y)^2\}}}$$

For $n=10$

$$r = \frac{(10)(1148) - (176)(172)}{\sqrt{\{ (10)(670) - (176)^2 \} \{ (10)(3240) - (172)^2 \}}}$$

$$r = \frac{11480 - 13072}{\sqrt{(6700 - 5776)(32400 - 29584)}}$$

$$r = \frac{-1592}{\sqrt{(924)(2816)}}$$

$$r = \frac{-1592}{2601984}$$

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$$r_2 = \frac{-1592}{1613.06}$$

$$r_2 = -0.98 \text{ Ans}$$

PART B

X	Y	X ²	Y ²	XY
20	5	400	25	100
11	15	121	225	185
15	14	225	196	210
10	17	100	289	170
17	8	289	64	136
18	9	324	81	162
21	12	441	144	252
25	16	625	256	400
28	18	784	324	504

$$\Sigma = 165 \quad \Sigma = 114 \quad \Sigma = 3309 \quad \Sigma = 1604 \quad \Sigma = 2099$$

(a) Formula For least Square regression line for y or x

$$y = a + bx$$

$$b = \frac{n \Sigma xy - \Sigma x \Sigma y}{n \Sigma x^2 - (\Sigma x)^2}$$

$$b = \frac{(9)(2099) - (165)(114)}{(9)(3309) - (165)^2}$$

$$b = \frac{18891 - 18810}{29781 - 27225}$$

$$b = \frac{81}{2556}$$

$$b = 0.031$$

Now

$$a = \frac{1}{n} \{ \sum y - b \sum x \}$$

$$a = \frac{1}{9} \{ 114 - (0.031)(165) \}$$

$$a = \frac{1}{9} \{ 114 - 5.115 \}$$

$$a = \frac{1}{9} \{ 108.885 \}$$

$$a = 12.09$$

Hence

$$y = a + bx$$

$$y = 12.09 + 0.031x$$

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least Square regression line

For x as y

$$x = a + by$$

$$b = \frac{n \sum xy - \sum x \sum y}{n \sum y^2 - (\sum y)^2}$$

$$b = \frac{(9)(2099) - (165)(114)}{(9)(1604) - (114)^2}$$

$$b = \frac{18891 - 18810}{14436 - 12996}$$

$$b = \frac{81}{1440}$$

$$b = 0.056$$

Now

$$a = \frac{1}{n} \{ \sum x - b \sum y \}$$

$$a = \frac{1}{9} \{ 165 - (0.056)(114) \}$$

$$a = \frac{1}{9} \{ 165 - 6.384 \}$$

$$a = \frac{1}{9} \{ 158.616 \}$$

$$a = 17.62$$

Hence $X = a + by$

$$X = 17.62 + 0.056y$$

(b)

X	Y	$Y = 12.09 + 0.031x$	$X = 17.62 + 0.056y$
20	5	$= 12.09 + (0.031)(20) = 12.71$	$= 17.62 + 0.056(5) = 17.9$
11	15	$= 12.09 + (0.031)(11) = 12.44$	$= 17.62 + 0.056(15) = 18.45$
15	14	$= 12.09 + (0.031)(15) = 12.55$	$= 17.62 + 0.056(14) = 18.38$
10	17	$= 12.09 + (0.031)(25) = 12.8$	$= 17.62 + 0.056(17) = 18.55$
17	8	$= 12.8$	$= 18.2$
18	9	$= 12.09 + (0.031)(28) = 12.9$	$= 17.62 + 0.056(16) = 18.5$
21	12	$(28) = 12.9$	$= 17.62 + 0.056(18) = 18.6$
25	16		$= 18.6$
28	18		

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Q:- No 2

Ans:-

PART: A

(a) $n = 5$

let X denotes number of heads

$$X = 0, 1, 2, 3, 4, 5$$

By using Binomial distribution

$$P(X = r) = {}^n C_r p^r q^{n-r}$$

$$P = 2/3$$

$$q = 1 - p$$

$$q = 1 - 2/3$$

$$q = 1 - \frac{2}{3}$$

$$q = \frac{3-2}{3} = 1/3$$

$$q = 1/3$$

$$P(X=0) = {}^5 C_0 \left(\frac{2}{3}\right)^0 \left(\frac{1}{3}\right)^{5-0}$$
$$= \frac{1}{3^5}$$

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$$P(X=1) = \binom{5}{1} \left(\frac{2}{3}\right)^1 \left(\frac{1}{3}\right)^{5-1}$$
$$= \binom{5}{1} \left(\frac{2}{3}\right) \left(\frac{1}{3}\right)^4$$

$$= \frac{5}{32}$$

$$P(X=2) = \binom{5}{2} \left(\frac{2}{3}\right)^2 \left(\frac{1}{3}\right)^{5-2}$$
$$= \binom{5}{2} \left(\frac{2}{3}\right)^2 \left(\frac{1}{3}\right)^3$$
$$= \frac{10}{32}$$

$$P(X=3) = \binom{5}{3} \left(\frac{2}{3}\right)^3 \left(\frac{1}{3}\right)^{5-3}$$
$$= \binom{5}{3} \left(\frac{2}{3}\right)^3 \left(\frac{1}{3}\right)^2$$

$$P(X=3) = \frac{10}{32}$$

$$P(X=4) = \binom{5}{4} \left(\frac{2}{3}\right)^4 \left(\frac{1}{3}\right)^{5-4}$$

$$P(X=4) = \binom{5}{4} \left(\frac{2}{3}\right)^4 \left(\frac{1}{3}\right)^1$$
$$= \frac{5}{32}$$

$$P(X=5) = \binom{5}{5} \left(\frac{2}{3}\right)^5 \left(\frac{1}{3}\right)^{5-5}$$

$$= \binom{5}{5} \left(\frac{2}{3}\right)^5 \left(\frac{1}{3}\right)^0$$

$$P(X=5) = \frac{1}{32}$$

Hence

probability of various heads

X	0	1	2	3	4	5
P(X)	1/32	5/32	10/32	10/32	5/32	1/32

Ans.

PART: B

Hence-

therefore the binomial distribution
with $n=10$

$$p = \frac{2}{3}$$

$$q = 1-p$$

$$q = 1 - \frac{2}{3}$$

$$q = \frac{1}{3}$$

let X denote the number of
won by A then.

$$(ii) \quad P(X \geq 4) = 1 - P(X < 4)$$

$$= 1 - \sum_{x=0}^3 \binom{10}{x} \left(\frac{2}{3}\right)^x \left(\frac{1}{3}\right)^{10-x}$$

$$= 1 - \left[\left(\frac{1}{3}\right)^{10} + 10 \left(\frac{2}{3}\right)^1 \left(\frac{1}{3}\right)^9 \right.$$

$$+ 45 \left(\frac{2}{3}\right)^2 \left(\frac{1}{3}\right)^8$$

$$\left. + 120 \left(\frac{2}{3}\right)^3 \left(\frac{1}{3}\right)^9 \right]$$

$$= 1 - \frac{1}{59049} [1 + 20 + 180 + 960]$$

$$= 1 - 0.0197$$

$$\boxed{P(X \geq 4) = 0.9803}$$

$$(ii) \quad P(X=4) = \binom{10}{4} \left(\frac{2}{3}\right)^4 \left(\frac{1}{3}\right)^6$$

$$= 210 \left(\frac{16}{81}\right) \left(\frac{1}{729}\right)$$

$$= \frac{3360}{59049}$$

$$\boxed{P(X=4) = 0.056}$$

(iii) $P(X=11) = \frac{1}{3} (0) =$
 because X can take
 only value
 $0, 1, 2, 3, \dots, 10.$

(iv) 6 or more games

$$\begin{aligned}
 P(X \geq 6) &= \sum_{k=6}^{10} \binom{10}{k} \left(\frac{2}{3}\right)^k \left(\frac{1}{3}\right)^{10-k} \\
 &= \binom{10}{6} \left(\frac{2}{3}\right)^6 \left(\frac{1}{3}\right)^4 + \\
 &\quad \binom{10}{7} \left(\frac{2}{3}\right)^7 \left(\frac{1}{3}\right)^3 + \\
 &\quad + \binom{10}{8} \left(\frac{2}{3}\right)^8 \left(\frac{1}{3}\right)^2 + \\
 &\quad + \binom{10}{9} \left(\frac{2}{3}\right)^9 \left(\frac{1}{3}\right)^1 \\
 &= 0.228 + 0.261 + 0.087 + 0.018
 \end{aligned}$$

$$P(X \geq 6) = 0.79$$

QUESTION No 3

Ans:-

PART A:-

2	6	1	5	4	3	3	8	10	1
4	3	3	0	5	2	4	4	10	3
5	3	3	6	3	3	2	2	7	4
1	4	2	4	4	4	6	8	10	7
7	5	6	5	5	3	3	9	2	2

(a) Construct in grouped Frequency distribution of these data.

X	f
0	4
1	8
2	11
3	7
4	5
5	4
6	3
7	2
8	1
9	3
10	3

PART: B:

(b) Group Frequency distribution

classes	f
0-2	5
2-4	19
4-6	12
6-8	7
8-10	3
10-11	3