

## FINAL EXAM

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ID # 7812

SEC # 'A'

Subject # PRCD-I

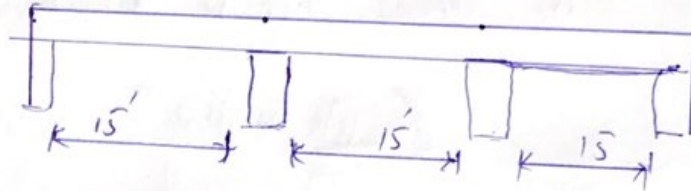
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①

Q No: 01

Given data



Given data

Three Span Reinforced Concrete slab

Clear span = 15 ft

live load = 160 psf

Service Floor finished load = 20 psf

$f'_c = 4000 \text{ psi}$

$f_y = 40 \text{ ksi}$

Solution

[Step # 01] Minimum Thickness of Slab

$$t_{\min} = \frac{L}{28} = \frac{15}{28} \quad (\text{by formula})$$

$$= 6.9$$

Say,

$$6.5''$$

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②

$$f_y = 40 \text{ ksi}$$

So finding a factor with this thickness

$$\text{factor} = \left( 0.4 + \frac{f_y}{100} \right)$$

$$\leq 0.4 + \frac{40}{100}$$

$$\leq 0.8$$

Hence the minimum thickness we have  $6.5 \times 0.8$

$$t_{\min} = 5.2''$$

Say,  $5.5''$

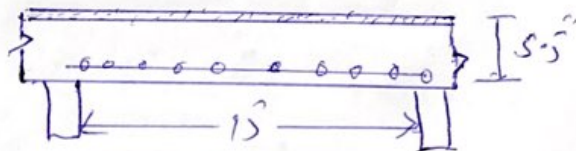
Step # 02

Effective Depth

$$d = t - \text{clear cover} - \frac{1}{2} (\text{dia of main bar})$$

$$d = 5.5 - 0.75 - \frac{1}{2} \left( \frac{5}{8} \right)$$

$$d = 4.5''$$



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③

Step #03 Self weight of Slab

$$= \frac{t}{12} \times \gamma_{\text{concrete}}$$

$$= \frac{5.5}{12} \times 150$$

$$\Rightarrow 68.75 \text{ lb/ft}^2$$

Step #04 Total Factored Load

Factored Live Load = 160 lb/ft<sup>2</sup>

So the Factored dead Load

$$D.L = 1.2(20 + 68.75)$$

$$= 106.5 \text{ lb/ft}^2$$

Total Factored Load = D.L + L.L

$$= 106.5 + 160$$

$$= 266.5 \text{ lb/ft}^2$$

$$= \frac{266.5}{1000} \Rightarrow 0.2665 \text{ k/ft}^2$$

Step #05 Ultimate moment

$$M_u = \frac{W_u \times L^2}{8} = \frac{0.2665 \times (15)^2}{8} \times 12$$

$$= 89.94 \text{ kips-inches}$$

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(4)

Step # 06

Area of Steel for main by trial and Repeat Method

Trial # 01

Let depth of Compression block

$$a = 0.2t = 0.2 \times 5.5 \Rightarrow 1.1 \text{ inch}$$

Now

$$A_{st} = \frac{M_u}{\phi \times F_y \times (d - \frac{a}{2})}$$

$$= \frac{89.94}{0.90 \times 40 \times (4.5 - \frac{1.1}{2})} \Rightarrow 0.63 \text{ in}^2$$

Trial # 02

$$a = \frac{A_{st} \times F_y}{0.85 \times f'_c \times b}$$

$$= \frac{0.63 \times 40}{0.85 \times 4 \times 12} \Rightarrow 0.62 \text{ in}^2$$

$$A_{st} = \frac{M_u}{\phi \times F_y \times (d - \frac{a}{2})} = \frac{89.94}{0.90 \times 40 \times (4.5 - \frac{0.62}{2})}$$

$$A_{st} = 0.59 \text{ in}^2$$

Trial # 03

$$a = \frac{0.59 \times 40}{0.85 \times 4 \times 12} \Rightarrow 0.57 \text{ in}^2$$

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$$A_{st} = \frac{89.194}{0.90 \times 40 \times \left(4.5 - \frac{0.75}{2}\right)}$$
$$= 0.59 \text{ in}^2$$

So Area of Steel will be used

$$A_{st} = 0.59 \text{ in}^2$$

Step # 07

Area of Steel For distribution Reinforcement

$$A_{min} = 0.002 \times b \times t \quad (\text{For grade 40 steel})$$

$$A_{min} = 0.002 \times 12 \times 5.5$$

$$A_{min} = 0.132 \text{ in}^2$$

Step # 08

Spacing for main bar

$$\text{Spacing} = \frac{A_b}{A_{st}} \times 12$$

use #6 bar  $\left(\frac{6}{8}\right)$

$$A_{sea} = \frac{\pi}{4} \left(\frac{6}{8}\right)^2 \quad (A_{sea} = \frac{\pi}{4} d^2)$$

$$= 0.442 \text{ in}^2$$

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Step #9

Spacing for Distribution bar

$$\text{Spacing} = \frac{A_b}{A_{sb}}$$

Use #5 bar

$$A_{sreq} = \frac{\pi}{4} \left(\frac{5}{8}\right)^2 = 0.31 \text{ in}^2$$

$$\begin{aligned} \text{Spacing} &= \frac{0.31}{0.132} \times 12 \\ &= \cancel{27.8} \quad 28.1 \\ &\text{Say, } 28'' \end{aligned}$$

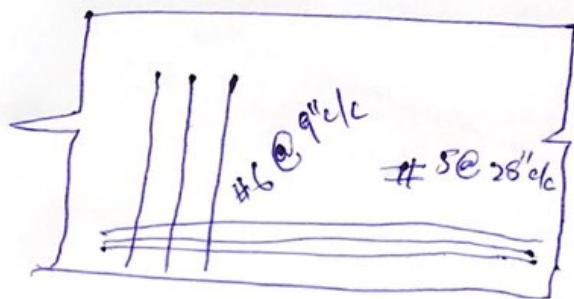
Step #10

Final Sketch

$f'_c = 4 \text{ ksi}$ ,  $f_y = 40 \text{ ksi}$

Main steel #6 at 9" c/c

Distribution steel #5 at 28" c/c

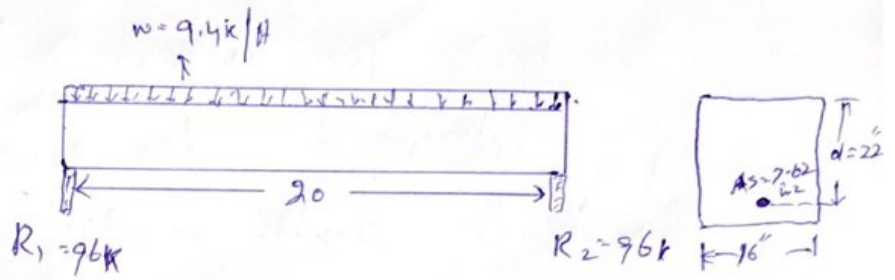


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Q: 02 :

Sol:-



First Find the unit Load of beam so  $b \times d$

$$\frac{16}{12} \times 150 = 200 \text{ lb/ft} = 0.2 \text{ k/ft}$$

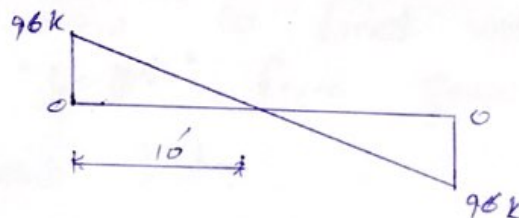
$$\begin{aligned} \text{Total Factored Load} &= 9.4 + 0.2 \\ &= 9.6 \text{ k/ft} \end{aligned}$$

Step: 01

Find the reactions  $R_1$  &  $R_2$

$$\text{total Load} = 9.6 \times \frac{20}{2} = 96 \text{ k} \quad (R_1 = R_2)$$

Step: 02 Draw its Shear Force diagram

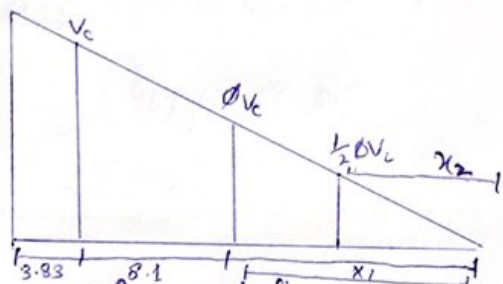


P.T.O



**Step: 03** find value of critical stress " $V_0$ " & its location

As we know that critical location is located distance " $d$ " from face of support  $d = \frac{22''}{12} = 1.83'$  value of critical shear at distance " $d$ " by similar triangles.



From Similar triangles ( $\Delta$ 's)

$$\frac{96}{10} = \frac{V_0}{8.17}$$

By crossing

$$V_0 = 778.43$$

$$V_0 = 78.43$$

**Step: 04** Now to find value of " $\phi V_c$ " & " $\frac{1}{2} \phi V_c$ " from zero shear of right side.

$$\begin{aligned}\phi V_c &= \phi \times 2 \times \sqrt{f_c} \times b_w \times d \\ &= \frac{0.75 \times 2 \times \sqrt{4000} \times 16 \times 22}{1000}\end{aligned}$$

$$\phi V_c = 33.40 \text{ k}$$

Location of  $\phi V_c$  by Similarity of triangles

$$\frac{96}{10} = \frac{33.40}{x_1}$$

by C.M

$$\underline{x_1 = 3.48'}$$

Now

$$\frac{1}{2} \phi V_c$$

$$= \frac{33.40}{2} \Rightarrow 16.70 \text{ k}$$

$\phi V_c$ 's Location by Similarity triangles

$$\frac{96}{10} = \frac{16.70}{x_2}$$

By C.M

$$\underline{x_2 = 1.74'}$$

Step # 05

Find the value of  $\phi V_s$   
as from formula ( $V_u = \phi V_s + \phi V_c$ )

$$\phi V_s = V_u - \phi V_c$$

$$\phi V_s = 78.43 - 33.40$$

$$\underline{\phi V_s = 45.03 \text{ K}}$$

Step # 06 Check for accuracy

$$\phi \times 8 \times \sqrt{f_c} \times b \times d$$

$$= \frac{0.75 \times 8 \times \sqrt{4000} \times 16 \times 22}{1000}$$

$$= 133.57 \text{ K}$$

As  $133.57 > \phi V_s$  (mean section  
is adequate)

Step # 07 Checking for minimum spacing

for stirrup

$$\phi \times 4 \times \sqrt{f_c} \times b \times d$$

$$= \frac{0.75 \times 4 \times \sqrt{4000} \times 16 \times 22}{1000}$$

$$= 66.79 \text{ K}$$

So,  $66.79 \text{ K} > \phi V_s = 44.83 \text{ K}$

PTD

→ According to ACI Cod

Maximum Spacing will be selected from following four conditions

$$\textcircled{1} - S_{\max} = 24''$$

$$\textcircled{2} \frac{d}{2} = \frac{22}{2} = 11''$$

$$\textcircled{3} S_{\max} = \frac{A_v \times F_y}{0.75 \times \sqrt{F_c} \times b_w}$$

$$= \frac{0.22 \times 6000}{0.75 \times \sqrt{4000} \times 16}$$

$$= 17.40''$$

$$\textcircled{4} S_{\max} = \frac{A_v \times F_y}{50 \times b_w}$$

$$= \frac{0.22 \times 6000}{50 \times 16}$$

$$= 16.50''$$

From above four condition value of spacing #3 bar as

$$S_{\max} = 11'' \text{ c/c}$$

Step #08

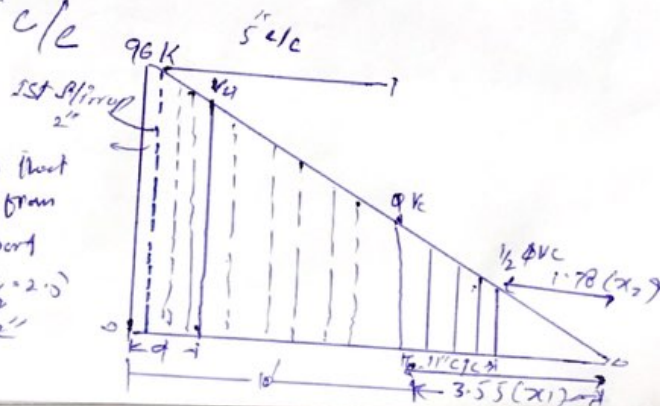
Spacing of stirrup at critical section

$$S = \frac{\phi \times A_v \times F_y \times d}{V_u - \phi V_c} = \frac{0.75 \times 0.22 \times 60 \times 22}{78.93 - 33.40} = 4.84$$

say,

$$S = 5'' \text{ c/c}$$

We know that  
1st stirrup from  
face of support  
 $= \frac{S}{2} = \frac{5}{2} = 2.5$   
 $\Rightarrow 2''$



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Q No: 03

Given data

12 inch<sup>2</sup> Square Column

Steel = 4 #9

Ties #3 @ 12"

$F'_c = 4000 \text{ psi}$

$f_y = 60 \text{ ksi}$

Sol:

Step # 01

gross area of concrete

$$A_g = b \times b$$

$$A_g = 12 \times 12 = 144 \text{ in}^2 \text{ (Actual)}$$

Step # 02

Area of Steel

$A_s$ ,

$$A_s = 5\% \text{ of } A_g$$
$$= 0.05 \times 144$$

$$A_s = 7.2 \text{ in}^2$$

Step # 03

ultimate Load Carrying Capacity

$$P_u = \phi \times 0.80 \times [0.85 \times F'_c \times (A_g - A_s) + A_s \times f_y]$$

$$= 0.65 \times 0.80 \times [0.85 \times 4 (144 - 7.2) + 7.2 \times 60]$$

$$P_u = 466.50 \text{ k}$$

Step # 04

Sketch & design of ties

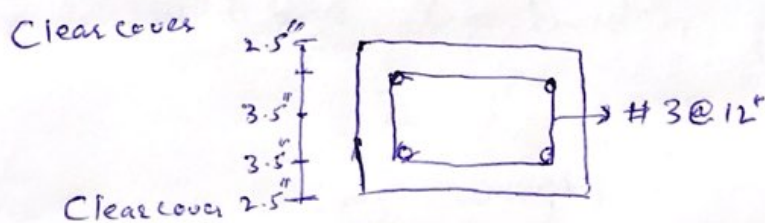
From the following value we choose the least value of all

$$\textcircled{1} \rightarrow 16 \times \text{dia of Long bar} = 16 \times \frac{9}{8} = 18''$$

$$\textcircled{2} \rightarrow 48 \times \text{dia of Tie bar} = 48 \times \frac{3}{8} = 18''$$

$$\textcircled{3} \rightarrow \text{Least Column dimension} = 12''$$

So c/c distance between ties = 12''



Since This is a tie Square Column so here is no spiral stirrup used The stirrup used in this rectangular shape due to the given specification of the structure Therefore we will use tie stirrup instead of spiral stirrup.

Given data :

$$F_c' = 3 \text{ ksi}$$

$$F_y = 60 \text{ ksi}$$

$$q_a = 2.50 \text{ ksf}$$

$$\gamma_{\text{void}} = 120 \text{ psf}$$

$$D.L = 100 \text{ kips}$$

$$L.L = 120 \text{ kips}$$

$$Z = 5$$

Sol: Thickness of footing

Step # 01

Assume

$$h = 2 \text{ in}$$

Step # 02 Overburden pressure,  $w$

$$Z = 5'$$

$$\text{Total weight} = W_{\text{con}} + W_{\text{fill}}$$

$$W = \gamma_{\text{con}} h + \gamma_f (Z - h)$$

$$= (1.25 \times 150) + 120(5 - 1.25)$$

$$W = 187.5 + 450$$

$$W = 637.5 \text{ psf} \quad \therefore \div \text{ing by } 1000$$

$$W = 0.6735 \text{ Ksf}$$

Step #03 Effective bearing Capacity

$$q_c = q_a - W$$

$$= 2.5 - 0.6735$$

$$q_c = 1.8625 \text{ Ksf}$$

Step #04 Bearing Area

$$A_{req} = \frac{\text{Service Load}}{q_c} \quad \text{--- (1)}$$

$$A_{req} = \frac{100 + 120}{1.8625}$$

$$A_{req} = \frac{220}{1.8625}$$

$$A_{req} = 118.120 \text{ ft}^2$$

$$A_{req} = B \times B$$

$$= 118.120$$

$$B > 10.86 \approx 11 \text{ ft}$$

$$B = 11 \text{ ft}$$

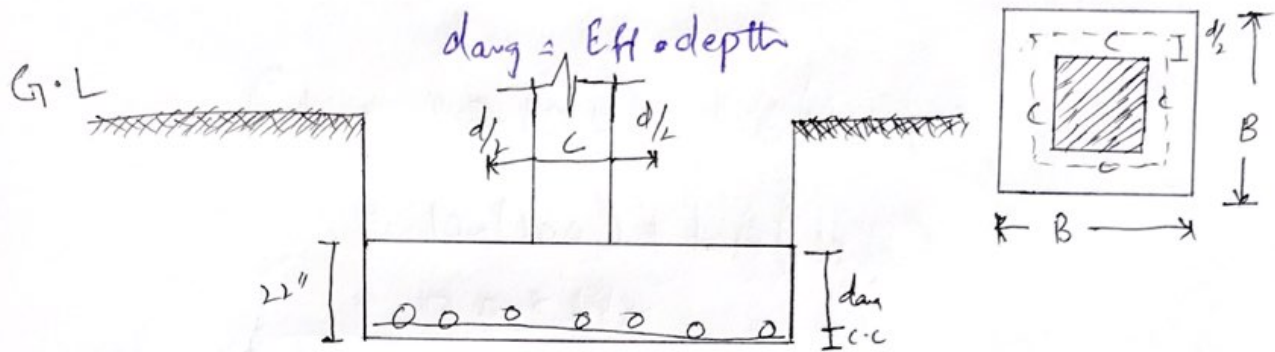


Step #5 Critical Shear parameter

$$b_o = 4 \times (c + d_{avg}) \quad \text{--- (1)}$$

$\therefore c = \text{column dia}$

$d_{avg} = \text{Eff depth}$



use #8 bars

$$d = h - (c.c. - \text{dia of bar} - \frac{1}{2} \text{ dia of bar})$$

$$= 22 - (3 + 1 + 0.5)$$

$$= 22 - 4.5$$

$$= 17.5$$

put in eq (1)

$$b_o = 4 \times (16 \times 17.5)$$

$$b_o = 134 \text{ inch}$$

Step # 06

Design pressure due to  
Factor Load

$$q_u = \frac{F.L}{A_{eq}} \quad \text{--- (2)}$$

$$\begin{aligned} F.L &= 1.2(D.L) + 1.6(L.L) \\ &= 1.2(100) + 1.6(120) \\ &= 120 + 192 \end{aligned}$$

$$F.L = 312 \text{ kips}$$

$$q_u = \frac{312}{121}$$

$$q_u = 2.57 \text{ ksf}$$

Step # 07

punching Shear  $V_{up}$ 

$$\begin{aligned} V_{up} &= q_u \left\{ B^2 - (c+d_{avg})^2 \right\} \\ &= 2.57 \left\{ 11^2 - \frac{(16+17.5)}{12} \right\} \end{aligned}$$

$$V_{up} = 290.94 \text{ kips}$$

Step #8 punching Shear Capacity:

$$V_{up} = 290.94$$

$$\begin{aligned} \phi V_{cp} &= \phi 4 \sqrt{f'_c} b_o \times d \\ &= \frac{0.75 \times 4 \times \sqrt{3000} \times 134 \times 17.5}{1000} \end{aligned}$$

$$\phi V_{cp} = 385.32 > 290.94$$

so it's okay

Step #09

Beam Shear (one way slab)

$$\begin{aligned} V_{u1} &= q_u \times B \times \left( \frac{B}{2} - \frac{C}{2} - d \right) \\ &= 2.57 \times 11 \times \left( \frac{11}{2} - \frac{16/12}{2} - \frac{175}{12} \right) \end{aligned}$$

$$V_{u1} = 95.45 \text{ k}$$

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Step #10 Self Shearing Capacity

$$\phi V_c = \phi \times 2 \times \sqrt{f_c} \times B \times d$$

$$= \frac{0.75 \times 2 \times \sqrt{3000} \times (11 \times 12) \times 17.5}{1000}$$

$$\phi V_c = 189.785 > V_u \rightarrow \text{okay}$$

Step #11 ultimate Moment

$$M_u = q_u B \frac{k^2}{2} \quad \text{--- (3)}$$

$$k = \left( \frac{B - c}{2} \right) = \left( \frac{11 - \frac{16}{12}}{2} \right)$$

K = 4.83  
put in eq (3)

$$M_u = \frac{2.57 \times 11 \times 4.83^2}{2}$$

$$M_u = 329.75 \text{ kft}$$

$M_u = 3957 \text{ in-kips}$

Step # 12

Area of for main bar  
by trial & error method  
where,

$$M_u = 3957 \text{ in-kip}$$

Let Suppose

$$a = 0.2h \Rightarrow 0.2 \times 22 = 4.4''$$

Trial # 1  $a = 4.4''$

$$A_s = \frac{M_u}{\phi \times f_y \left(d - \frac{a}{2}\right)}$$

$$A_s = \frac{3957}{0.9 \times 60 \times \left(17.5 - \frac{4.4}{2}\right)}$$

$$A_s = \frac{3957}{780.3}$$

$$A_s = 4.789$$

Trial # 02

$$\begin{aligned} a &= \frac{A_s f_y}{0.85 \times f'_c \times B} \\ &= \frac{4.79 \times 60}{0.85 \times 8 \times (11 \times 12)} \end{aligned}$$

$$a = 0.852$$

$$A_s = \frac{M_u}{\phi F_y \left(d - \frac{a}{2}\right)} = \frac{3957}{0.9 \times 60 \left(17.5 - \frac{0.852}{2}\right)}$$

$$A_s = 4.29 \text{ in}^2$$

Trial # 03

$$a = \frac{A_s f_y}{0.85 \times F_c \times B}$$

$$= \frac{4.29 \times 60}{0.855 \times 3 \times (11 \times 12)}$$

$$a = 0.7602$$

$$A_s = \frac{M_u}{\phi f_y \left(d - \frac{a}{2}\right)}$$

$$= \frac{3957}{0.9 \times 60 \times \left(17.5 - \frac{0.7602}{2}\right)}$$

$$A_s = 4.28$$

Step #13 Check minimum requirement of steel.

$$\begin{aligned} \text{(i)} \quad A_{smin} &= 0.0018 \times B \times h \\ &= 0.0018 \times (11 \times 12) \times 22 \end{aligned}$$

$$\boxed{A_{smin} = 5.2272 \text{ in}^2}$$

$$\begin{aligned} \text{(ii)} \quad A_{smin} &= \frac{200}{f_y} \times B \times d \\ &= \frac{200}{60000} \times (11 \times 12) \times (17.5) \end{aligned}$$

$$A_{smin} = 7.7 \text{ in}^2$$

$$\begin{aligned} \text{(iii)} \quad A_{smin} &= \frac{3 \times \sqrt{f_c'} \times B \times d}{f_y} \\ &= \frac{3 \times \sqrt{3000} \times (11 \times 12) \times (17.5)}{60000} \end{aligned}$$

$$\boxed{A_{smin} = 6.32 \text{ in}^2}$$

greater will be selected

$$(A_{smin} = 7.7 \text{ in}^2)$$

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Step #14

No of bars  
using # 8 bar

$$A_b = \frac{\pi}{4} d^2$$

$$= \frac{3.14}{4} (1)^2 \Rightarrow 0.785 \text{ in}^2$$

$$\begin{aligned} \text{No of bars} &= \frac{A_s}{A_b} = \frac{7.7}{0.785} \\ &= 9.8 \approx 10 \text{ bars} \end{aligned}$$

Spacing:

$$\frac{10.5 \times 12}{9}$$

$$\text{Spacing} = 14 \text{ in c/c}$$

