

Page 1

1  
Name: Salman Farooq

(Sessional Assignment)

Q.1) A 3 phase 50-Hz over head transmission line 100 km long has the following constant:  
Resistance / km / phase =  $0.1 \Omega$   
Inductive reactance / km / phase =  $0.2 \Omega$   
Capacitive Susceptance / km / phase =  $0.04 \times 10^{-4}$  Siemen

Determine (i) the Sending end current (ii) Sending End Voltage (iii) Sending end power factor and (iv) transmission efficiency when supplying a balanced load of 1000 kW at 66 kV. pf 0.8  
Suggest use nominal  $\pi$  method.

Q.2 A (medium) Sigal phase transmission line 100 km long has the following constant.

Resistance / km =  $0.25 \Omega$  Reactance / km =  $0.8 \Omega$

Susceptance / km =  $14 \times 10^{-6}$  Siemen

2

②

Receiving end line voltage = 66000V  
 Assuming that the total capacitance of the line is localised at the receiving end alone determine.

- (i) The sending end current
- (ii) The sending end voltage
- (iii) Regulation and the supplying power factor.

Q-(3) Describe Ferranti Effect why Ferranti effect occurs? Detail Explanation of the Ferranti effect by considering a nominal  $\pi$  model. How to reduce Ferranti effect.



1/1/20

Q-2) A 3 phase so the overhead transmission line 100 km has the following constant.

$$\text{Resistance / km / phase} = 0.1 \Omega$$

$$\text{Inductive reactance / km / phase} = 0.2 \Omega$$

$$\text{capacitive susceptance / km / phase}$$

$$0.04 \times 10^{-4} \text{ Seimen} \quad \text{Determine}$$

(i) The sending end current (ii) Sending end voltage (iii) Sending end power factor and (iv) transmission efficiency

when supplying a balanced load

$$\text{of } 100 \text{ kW at } 66 \text{ kV pf } 0.8$$

lagging Use nominal T method

Solutions:-

$$\text{total resistance phase} = 0.1 \times 100 = 10$$

$$\Omega \text{ total resistance phase} \times 3 = 0.2 \times 100 = 20$$

$$\text{Capacitive susceptance } y = 0.04 \times 10^{-4} \times 100$$

$$= 4 \times 10^{-4} \text{ S}$$

$$\text{Receiving end voltage / phase, } V_R =$$

$$66000 / \sqrt{3} = 38105 \text{ V}$$

$$\text{Load current, } I_R = \frac{10000 \times 10^3}{\sqrt{3} \times 66 \times 10^3 \times 0.8} = 1094$$

$$\cos \theta_R = 0.8 \quad \sin \theta_R = 0.6$$

# 4



Impedance per phase,  $\vec{Z} = R + j \times L = 10 + j20$

(i) Taking receiving end voltage as the reference phase we have

Receiving end voltage  $\vec{V}_R = V_R + j0 = 38.105 \text{ V}$

Load current,  $I_R (\cos \phi_R - j \sin \phi_R)$   
 $= 109 (0.8 - j0.6) = 87.2 - j65.4$

voltage across C,  $\vec{V}_T = \vec{V}_R + I_R \vec{Z} = 38.105 + (87.2 - j65.4)(5 + j10)$   
 $= 38.105 + 436 + j872 - j327 + 654 = 39.195 + j545$

charging current,  $\vec{I}_C = jYV_T = j4 \times 10^{-4} (39.195 + j545)$   
 $= (0.218 + j15.6)$

Sending end current,  $\vec{I}_S = I_R + \vec{I}_C$   
 $= (87.2 - j65.4) + (0.218 + j15.6)$   
 $= 87.4 - j49.8 = 100 \angle 29^\circ 47.2 \text{ A}$



# 5

29(3)

Sending end current = 100A

(ii) Sending voltage  $\vec{V}_S = \vec{V}_R + I\vec{Z}$

$$\vec{V}_S = (39.195 + j 545) + (87.0 - j 49.8) \\ (5 + j 10)$$

$$= 39.195 + j 545 + 434.9 + j 870 \quad [j 249$$

$$+ 498 = 40128 + j 1170 = 40145 \angle 1.402^\circ \text{ V}$$

$\therefore$  Line value at sending end voltage.

$$= 40145 \sqrt{3} = 69533 \text{ V} = 69.53 \text{ kV}$$

(iii) Referring to phases-

$\phi =$  angle between  $\vec{V}_R$  and  $\vec{V}_S$

$$= 1.402^\circ$$

$\phi_2 =$  angle between  $\vec{V}_R$  and  $\vec{I}$

$$= 29.4724^\circ$$

$\phi_5 =$  angle between  $\vec{V}_S$  and  $\vec{I}$

$$= \phi_1 + \phi_2 = 1.402 + 29.472 = 31.272^\circ$$

Sending end power =  $\cos \phi_5$

$$= \cos 31.27^\circ = 0.853 \text{ lag}$$

(iv) Sending end power = 3VSI

$$\cos \phi_5 = 3 \cdot 40145 \times 100 \cdot 9734 \times 0.853$$

$$= 10273105 \text{ W} = 10273.105 \text{ kW}$$

Power delivered = 10000 kW

(6)

6

$$\therefore \text{Transmission efficiency} = \frac{10000}{102773.165}$$

$$\times 100 = 87.34\%$$

(2)  
Q3

A (medium) single phase transmission line 100 km long has the following constant.

Resistance/km =  $14 \times 10^{-6}$  Siemens

Receiving line voltage = 6600 V

Assuming that the total capacitance of the line is localised at the receiving end alone determine



Page 4

- (i) The sending end current
- (ii) The sending end voltage
- (iii) Regulation and (iv) supply power factor. The line is delivering 15000 kW at 0.8 power factor lagging.

Draw the phasor diagram to illustrate your calculations.

Solution: →

total Resistance =  $R = 0.2 \times 100 = 25 \text{ ohms}$

total Reactance =  $X = 0.8 \times 100 = 80 \text{ ohms}$

Total Susceptance  $Y = 14 \times 14 \times 10^{-6} \times 100 - 14 \times 10^{-4} \text{ S}$

Receiving end voltage  $V_R = 66000 \text{ V}$

Load current  $I_R = \frac{15000 \times 10^3}{66000 \times 0.8} = 284 \text{ A}$

$\cos \phi_R = 0.8$        $\sin \phi_R = 0.6$

Taking Receiving end voltage as the reference phasor we have

$\vec{V}_R = V_R + j0 = 66000 \text{ V}$

Load current  $\vec{I}_R = I_R (\cos \phi_R$

$- j \sin \phi_R) = 284 (0.8 - j0.6) = 227 - j170$

8

8

Capacitive current  $I_C = I_T \times V_R =$

$$j14 \times 10^{-4} \times 66000 = j92$$

(i) Sending end current  $I_S = I_R$

$$+ I_C = (227 - j170 + j92) = 227 - j78$$

Magnitude of  $j78$  is  $= \sqrt{(227)^2$

$$+ (78)^2 = 240 \text{ A}$$

(ii) voltage drop  $= I_S Z = (R + jXl)$

$$= (227 - j78)(25 + j80)$$

$$= 5675 + j1816 - j1950 + 6240$$



$$= 11.915 + j 16210$$

Sending end voltage  $\vec{V}_S = \vec{V}_R + \vec{I}Z$

$$Z = 66000 + j 11915 + j 16210$$

$$= 77915 + j 16210$$

$$\text{Magnitude of } V_S = \sqrt{(77915)^2 + (16210)^2}$$

$$= 7983 \text{ V}$$

$$\text{(III) \% voltage regulation} = \frac{V_S - V_R}{V_R} \times 100$$

$$= \frac{7983 - 66000}{66000} \times 100 = 20.58\%$$

(iv) reversing exp (ii) phase angle between  $\vec{V}_R$  and  $\vec{V}_S$  is:

$$\phi_1 = \tan^{-1} \frac{16210}{77915} = \tan^{-1} (0.208) = 11.50^\circ$$

Supplying power factor angle

$$\phi_S = 18.96^\circ + 11.50^\circ = 30.46^\circ$$

$$\text{Supplying pf} = \cos \phi_S = \cos 30.46^\circ$$

$$= 0.86 \text{ lag.}$$

# 10

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Q

Describe Ferranti effect. Why Ferranti effect occurs? Detail explanation of the Ferranti effect by considering a nominal  $\pi$  model. How to reduce Ferranti effect.

ANS  $\Rightarrow$

Ferranti effect:

Definition: The effect in which the voltage at the receiving end of the transmission line is more than the sending voltage is known as the Ferranti effect. Such type of the effect mainly occurs because of lights load or open circuit at the receiving end.



# 11

(pg 16)

Ferranti effect occurs:  
capacitance and inductance are  
The main parameters of the  
line having a length 240 km  
or above. On such transmission  
lines the capacitance is not  
concentrated at the same  
distributed points. It is the  
distributed uniformly along  
the whole length of the line.  
When the voltage is applied  
at the sending end the  
current drawn by the capacitance  
of the line is more than  
current associated with the  
load. Thus at no load or  
light load the voltage at  
the receiving end is quite  
large as compared to the  
constant voltage at the  
sending end.

# 12

Ferranti effect by considering a nominal  $\pi$  ( $\pi$ ) model  $\rightarrow$

Let us consider the long transmission line in which OE represent the receiving end voltage - OI represent the current through the capacitor at the receiving end.

The phasor PE represents the voltage drop across the  $X$  (inductance)

The phasor OB represent the sending end voltage under a no load condition.

It is seen from phasor that OE

In other words the voltage at the receiving end is greater than the voltage at the sending end when the line is at no load.



## 13

Page 77

For a small  $\pi$  (T) replica:

$$V_S = (1 + ZY/2)V_R + ZI_Y$$

where  $I_Y = 0$  at no load

condition.

$$V_S = (1 + ZY/2)V_R + Z(0)$$

$$= (1 + ZY/2)V_R$$

$$V_S = V_R = (1 + ZY/2)V_R - V_R$$

$$V_S - V_R = V_R [1 + ZY/2 - 1]$$

$$V_S - V_R = (ZY/2)V_R$$

$$Z = (r + j\omega l)S \text{ and } Y = (j\omega c)S$$

If the transmission line's resistance is unnoticed.

$$V_S - V_R = (ZY/2)V_R$$

Substitute  $Z = (r + j\omega l)S$  and

$Y = (j\omega c)S$  in the above  $V_S$

$$V_S - V_R = 1/2 (j\omega l S)(j\omega c S) V_R$$

$$V_S - V_R = -1/2 (\omega^2 l c S^2) V_R$$

(14)  
14

Page (8)

For the lines of overhead:  
 $1/\sqrt{LC} = 3 \times 10^8 \text{ m/s}$  (velocity of  
the electromagnetic wave  
transmission on the broadcast  
lines)  $3/\sqrt{LC} = 3 \times 10^8 \text{ m/s}$

$$\sqrt{LC} = 1/3 \times 10^8$$

$$LC = 1/(3 \times 10^8)^2$$

$$V_S - V_R = -\frac{1}{2} \omega^2 L C \cdot (1/(3 \times 10^8)^2)$$

2)  $V_R$

$$\omega = 2\pi R$$

The above eq illustrates that  
( $V_S - V_R$ ) is negative, that  
means  $V_R$  is greater than  $V_S$ .

This is also illustrated that  
this effects will also determine  
by electrical period of the  
transmission line and frequency  
Generally for each line:

$$V_S = AV_R + B I_R$$

On no load state-

$$I_R = 0, V_R = V_{RNL}, V_S = AV_{RNL}$$

$$|V_{RNL}| = |V_S|/|A|$$



How to reduce Ferranti effect in transmission line?

Electrical machine work on

Specific electrical energy.

If the voltage is far above the ground at the consumer

end then device get damaged,

and the winding of the

device also burn due to

high electrical energy.

Ferranti effect on extensive

transmission line is no-load

status. then the voltage

will increase at the collecting

end.

This can be restricted

by keeping the shunt

reactor next to the

collecting end of the

transmission lines.

# 16

The reactor allied between the lines along with natural to give back the capacitive current at o.b transmission lines. As the out comes happens in lengthly transmission lines, these reactor pay off the transmission lines and thus the voltage is regulated within the set limits.