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Section ~~A~~ B

Subject Structure Analysis II

Submitted To;

Engnr Sir ADEED

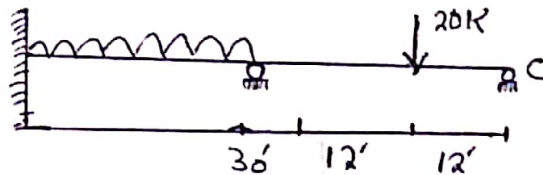
Jqra national University

# Question No 1

1)

Analyze the given beam shown in FIG-I by flexibility method.  
 $EI$  is constant.

1.

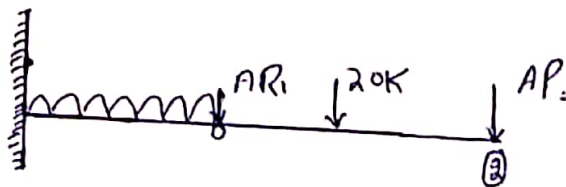


$E \cdot I$  constant

Sol:-

$$S.I = 2$$

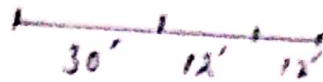
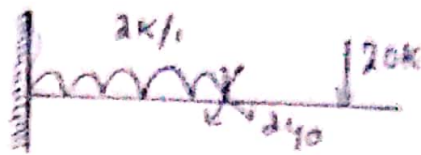
Step 1:- Select redundant actions.



$$\begin{bmatrix} DRS_1 \\ DRS_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix}, \quad \begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix}$$

$$[DRS] = [DRL] + F * AR.$$

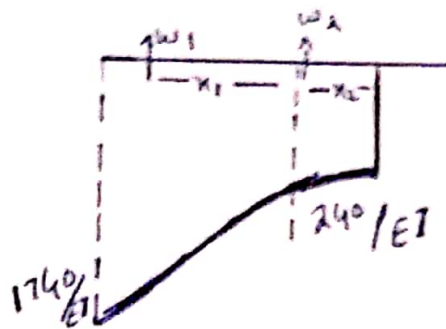
Step 2 = = Complete the values of  $[DRL]$



$$20 \times 12 = 240$$

$$20 \times 40 + 2 \times 30 \times 12$$

$$= 1140$$



$$w_1 = \left( \frac{240 + 0}{2EI} \right) \times 12 = 1440/EI$$

$$w_2 = \frac{1}{n+1} \times (b \times h) = \frac{1}{2+1} \left( \frac{1100}{EI} \right) \times 30 = 11000/EI$$

$$x_1 = \frac{L}{3} \left( \frac{a+2b}{a+b} \right)$$

$$x_1 = \frac{12}{3} \left( \frac{240 + 2(0)}{240 + 10} \right) = 4'$$

$$x_2 = \frac{3}{2n+2} \times b = \frac{3}{2+2} (30) = 22.5'$$

$$DRL_1 = w_1 (x_1 + 30) = 1440 (4 + 30) = 48960/EI$$

$$DRL_2 = w_1 (x_1 + 40) + w_2 (x_2 + 12)$$

$$= 442860$$

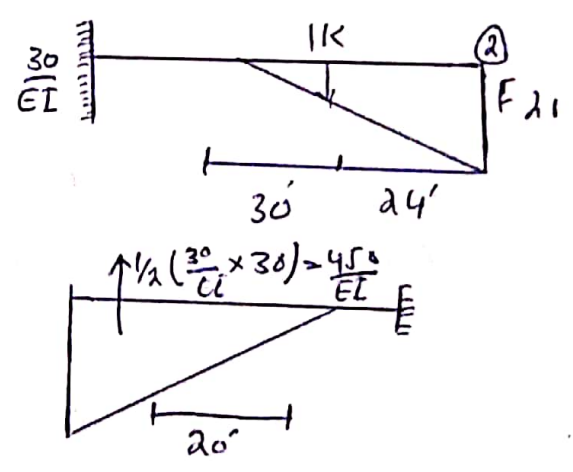
$$[DRL] = \frac{1}{EI} \begin{bmatrix} 48960 \\ 442860 \end{bmatrix}$$

Step 3:- Construct flexibility Co-efficient matrix.

$$F_{2 \times 2} = \begin{bmatrix} F_{11} & F_{12} \\ F_{21} & F_{22} \end{bmatrix}$$

a) Apply a unit value of  $D_{L1}$  at reference point

i. Complete the value of  $F_{11}$  and  $F_{21}$ .

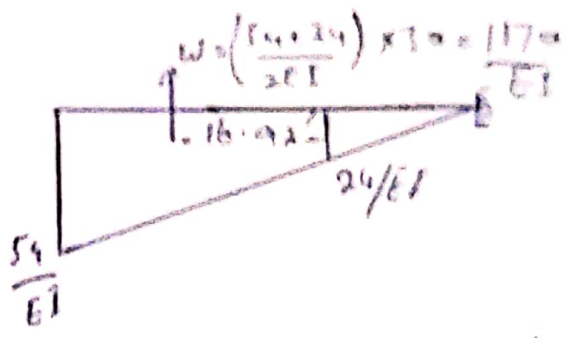
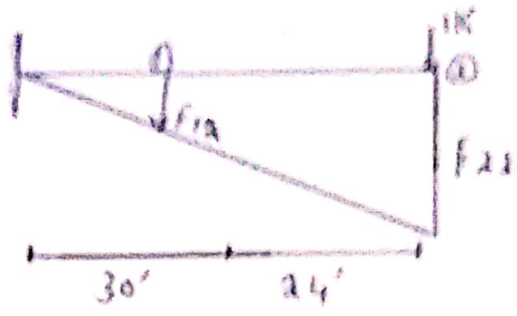


$$F_{11} = \frac{450}{EI} (20) = \frac{9000}{EI}$$

$$F_{21} = \frac{450}{EI} (20 + 24) = \frac{19800}{EI}$$

b: Apply a unit of  $A_{P2}$  at reference point (2) in compute the value of  $F_{12}$  &  $F_{22}$ .

4)



$$x = \frac{30}{3} \left[ \frac{24 + 2(54)}{54 + 24} \right] = 16.92'$$

$$F_{12} = \frac{1170}{EI} \times 16.92 = \frac{19800}{EI}$$

$$F_{22} = \frac{1}{2} (54 \times 54) \times \frac{1}{3} (30) + 24 = \frac{49572}{EI}$$



# Question No 2

Q → Difference between force method and displacement method and suggest which method is more suitable for structure analysis of matrix approach.

ANSWER:-

## Force Method

$$D_s < D_k$$

Forces are redundant or unknowns

starts with equilibrium of forces.

Forces found by Compatibility eqns of displacements

no of redundants =  $D_s$

not suitable for Comput

## Displacement Method.

$$D_s > D_k$$

Displacement are redundant or unknown

starts with compatible deformation

displacement found by equilibrium equal of forces.

no of redundants =  $D_k$ .

not of suitable for truss

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This method is more suitable for structural analysis of matrix approach.

There are two main methods of structural analysis of using matrix approach

(i) Force method

(ii) Displacement method.

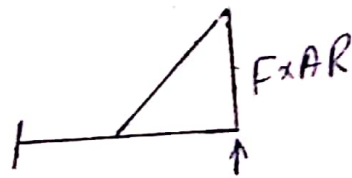
Force method.

This method is also known as flexibility or compatibility method. In this method the degree of static indeterminacy of the is determined and the redundants are identified. A co-ordinate is assigned to each redundant at co-ordinate

Thus  $AR_1, AR_2, \dots, AR_n$  are the redundants at co-ordinate  $1, 2, \dots, n$ .

If all the redundant are removed the resting structure known as

as the released stre is statically determined  
 from the principle of superposition  
 the net displacement at any point in a  
 statically determinate stre is the sum  
 of the displacement in the basic  
 determinate stre due to applied loads  
 and the redundant. Thus Condition, known  
 as compatibility Condition may be  
 exposed by the equation for "n"  
 redundant actions.



$$DRS = DRL + F \times AR$$

$$DRS_1 = DRL_1 + F_{11}AR_1 + F_{12}AR_2 + \dots + F_{1n}AR_n$$

$$DRS_2 = DRL_2 + F_{21}AR_1 + F_{22}AR_2 + \dots + F_{2n}AR_n$$

$$DRS_n = DRL_n + F_{n1}AR_1 + F_{n2}AR_2 + \dots + F_{nn}AR_n$$

Writing these equation in matrix form

$$\begin{bmatrix} DRS_1 \\ DRS_2 \\ DRS_n \end{bmatrix} = \begin{bmatrix} DRL_1 \\ DRL_2 \\ DRL_n \end{bmatrix} + \begin{bmatrix} F_{11} & F_{12} & \dots & F_{1n} \\ F_{12} & F_{22} & \dots & F_{2n} \\ F_{n1} & F_{n2} & \dots & F_{nn} \end{bmatrix} \begin{bmatrix} AR_1 \\ AR_2 \\ AR_n \end{bmatrix}$$



$$[DRS]_{n \times 1} = (DRL)_{n \times 1} + (F)_{n \times n} (AR)_{n \times 1}$$

8)

$$F(AR) = DRS - (DRL)$$

$$AR = (F)^{-1} (DRS - DRL)$$

$n$  = Degree of Indeforminary

where DRS = support settlement Relation

Corresponding to the redundant action.

DRL - Displacement (Rotation/translation)

Corresponding to the redundant action

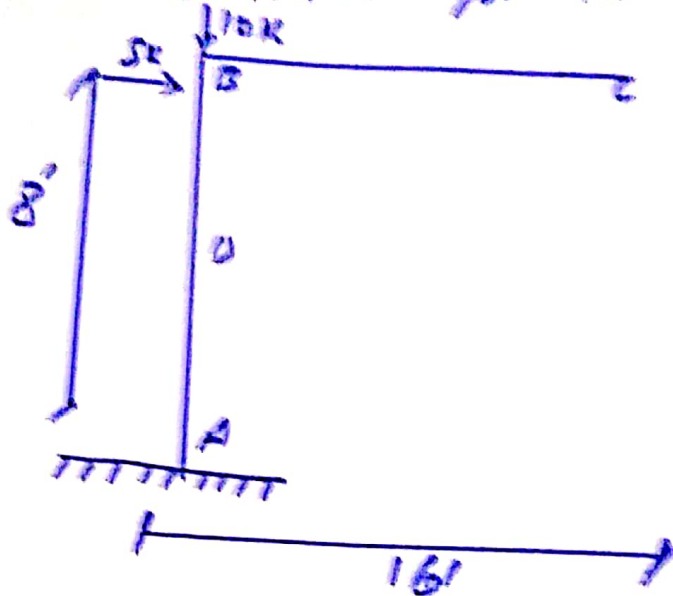
a released structure (Basic def str) due to applied loads.

AR = The redundant actions.

F = Flexibility Co-efficient i.e.

Displacement Caused by unit action.

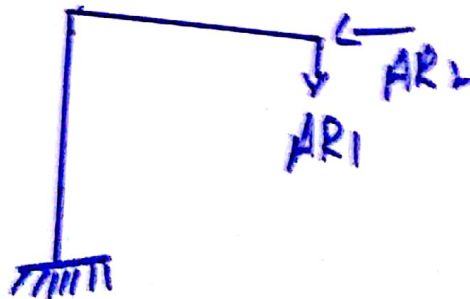
Q.103 Analyze the rigid-joint frame shown in Fig-2 by flexibility method. Assume EI is constant for all members.



Solution:-

$$\begin{aligned} S.I &= R-3 \\ &= 5-3 \\ &= 2^0 \end{aligned}$$

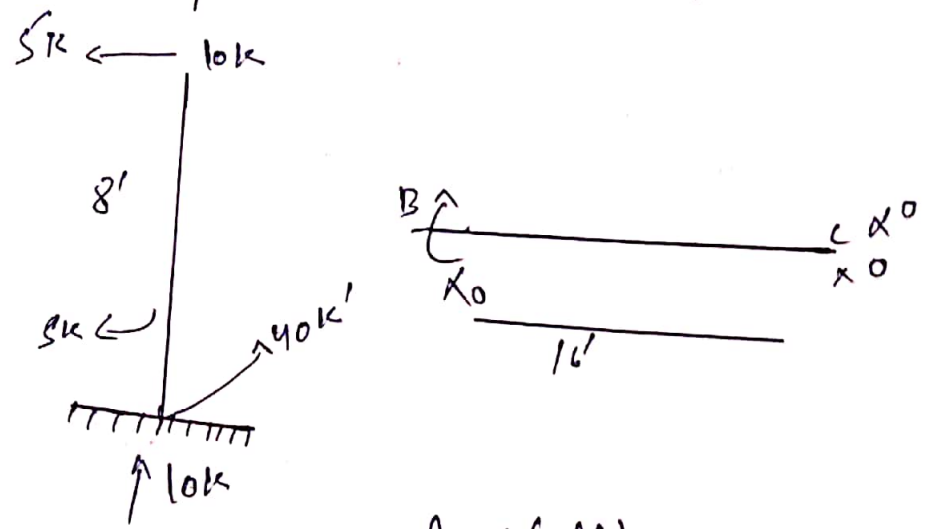
Step:01 Identifying the redundant action



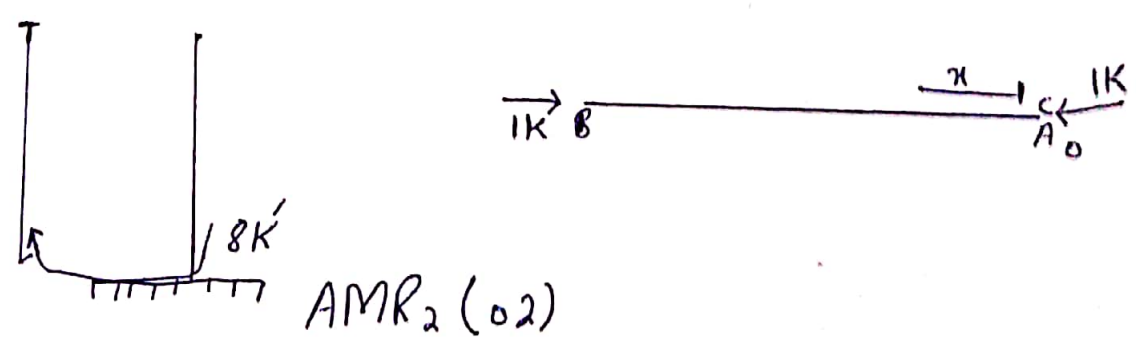
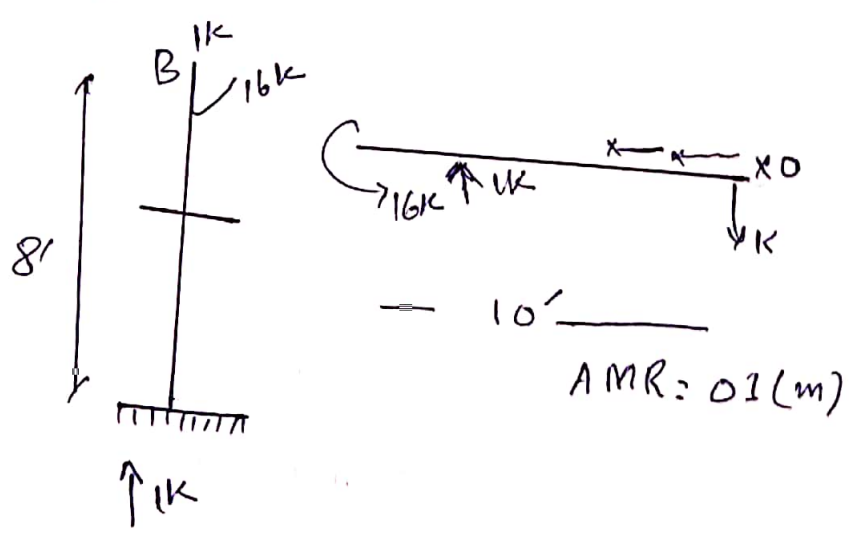
$$\begin{bmatrix} DRS1 \\ DRS2 \end{bmatrix} = \begin{bmatrix} 0 \\ 0 \end{bmatrix} \begin{bmatrix} AR1 \\ AR2 \end{bmatrix} = \begin{bmatrix} ? \\ ? \end{bmatrix}$$

Step: 02

compute the value of DRL and F



5 ΔM<sub>L</sub> - values (M)



Member	AB	BC	DPL <sub>1</sub>
Origin	A	C	
Limit	0-8	0-16	
I	I	2I	
M	$(5x-40)$	$0$	$\int (5x-40) dx$
$m_1$	$\downarrow$ $-16$	$\downarrow$ $x$	$x$
$m_2$	$8-x$	$0$	

$$DRL_1 = \int_0^8 \frac{(5x-40)(-16)}{EI} dx \Rightarrow DRL_2 = \int_0^8 \frac{(5x-40)(8-x)}{EI} dx = \frac{853.3}{EI}$$

$$F_{11} = \int_0^8 \frac{-(16)^2}{EI} dx + \int_0^{16} \frac{x^2}{2EI} dx = 2730.67/EI$$

$$F_{12} = \int_0^8 \frac{-(16)^2(8-x)}{EI} dx = -512/EI$$

$$F_{22} = -\int_0^8 \frac{(8-x)^2}{EI} dx = 170.67/EI$$

$$\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} F_{11} & F_{12} \\ F_{21} & F_{22} \end{bmatrix}^{-1} \begin{bmatrix} DRS_1 = DRL_1 \\ DRS_2 = DRL_2 \end{bmatrix}$$

$$\begin{bmatrix} AR_1 \\ AR_2 \end{bmatrix} = \begin{bmatrix} 2730.31 & -812 \\ -512 & 1700 \end{bmatrix} \begin{bmatrix} 0 & -2500 \\ 0 & -813.33 \end{bmatrix}$$

the End