chapter \#9
7.00 am
$Q_{1}$
Exercise $9.1 \quad$ Sunday 8
Q Qu

$$
\text { (i) }\left[\begin{array}{ccc}
2 & 1 & 4 \\
3 & -1 & 0
\end{array}\right]+\left[\begin{array}{ccc}
6 & 3 & 0 \\
-2 & 1 & 0
\end{array}\right]
$$

10.00

$$
=\left[\begin{array}{ccc}
2+6 & 1+3 & 4+0 \\
3+(-2) & -1+1 & 0+0
\end{array}\right]
$$

Noon

$$
=\left[\begin{array}{lll}
8 & 4 & 4 \\
1 & 0 & 0
\end{array}\right] \text { Ans. }
$$

(ii) $\left[\begin{array}{llll}1 & 3 & 5 & 6\end{array}\right]+\left[\begin{array}{llll}0 & -2 & 1 & 3\end{array}\right]$
3.00

$$
=\left[\begin{array}{lll}
1+0 & 3+(-2) & 5+1 \\
6+3
\end{array}\right]
$$

4.00

$$
=\left[\begin{array}{llll}
1 & 1 & 6 & 9
\end{array}\right] \text { Ans. }
$$

5.00
(iii) $\left[\begin{array}{l}4 \\ 3 \\ 1\end{array}\right]+\left[\begin{array}{c}6 \\ 0 \\ -2\end{array}\right]$
$\left.\begin{array}{l}7.00 \\ \\ 4+6 \\ 3+0 \\ 1+(-2)\end{array}\right]=\left[\begin{array}{c}10 \\ 3 \\ -1\end{array}\right]$ Ans
$\qquad$
July
(2)


9 Monday -u.
$\left[\begin{array}{ccc}2 & 3 & 4 \\ -1 & 6 & 2 \\ 1 & 0 & 3\end{array}\right]+\left[\begin{array}{lll}0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0\end{array}\right]$
$=\left[\begin{array}{ccc}2 & 3 & 4 \\ -1 & 6 & 2 \\ 1 & 0 & 3\end{array}\right]$
(v) $=\left[\begin{array}{cc}6 & 1 \\ 0 & -3 \\ -1 & 2\end{array}\right]-3\left[\begin{array}{cc}4 & 2 \\ 0 & 1 \\ -5 & -1\end{array}\right]$
$=\left[\begin{array}{cc}12 & 2 \\ 0 & -6 \\ -2 & 4\end{array}\right]-\left[\begin{array}{cc}12 & 6 \\ 0 & 3 \\ -15 & -3\end{array}\right]$
$=\left[\begin{array}{cc}12-12 & 2-6 \\ 0-0 & -6-3 \\ -2+15 & 4+3\end{array}\right]$
$\left[\begin{array}{cc}0 & -4 \\ 0 & -9 \\ 13 & 7\end{array}\right]$ Ons
0000 m
.


$$
\left[\begin{array}{ll}
b_{11}-a_{11} & b_{12}-a_{12} \\
b_{21}-a_{21} & b_{22}-a_{22}
\end{array}\right] \text { is the }
$$

200 Solution of $X+A=B$

$$
A=\left[\begin{array}{ll}
a_{11} & a_{12} \\
a_{21} & a_{22}
\end{array}\right], \quad B=\left[\begin{array}{ll}
b_{11} & b_{12} \\
b_{21} & b_{22}
\end{array}\right]
$$

Sol:

$$
\begin{aligned}
& X \neq A=B \\
& X= B-A \\
&= {\left[\begin{array}{ll}
b_{11} & b_{12} \\
b_{21} & b_{22}
\end{array}\right]-\left[\begin{array}{ll}
a_{11} & a_{12} \\
a_{21} & a_{22}
\end{array}\right] } \\
&= {\left[\begin{array}{ll}
b_{11}-a_{11} & b_{12}-a_{12} \\
b_{21}-a_{21} & b_{22}-a_{22}
\end{array}\right] }
\end{aligned}
$$

Q4 Solve:
6.00

$$
\begin{aligned}
& X \neq\left[\begin{array}{cc}
3 & -1 \\
2 & 2
\end{array}\right]=\left[\begin{array}{cc}
5 & 1 \\
-3 & 1
\end{array}\right] \\
& X=\left[\begin{array}{cc}
5 & 1 \\
-3 & 1
\end{array}\right]-\left[\begin{array}{cc}
3 & -1 \\
2 & 2
\end{array}\right] \\
& =\left[\begin{array}{cc}
5-3 & 1+1 \\
-3 & -2
\end{array} 1-2\right]=\left[\begin{array}{cc}
2 & 2 \\
-5 & -1
\end{array}\right] \text { Ans }
\end{aligned}
$$

11 Wednesday

$$
\left.\begin{array}{rl}
(i .00
\end{array} \quad x+\left[\begin{array}{cc}
-1 & 0 \\
0 & 2
\end{array}\right]=\left[\begin{array}{cc}
2 & 6 \\
1 & 5
\end{array}\right]+\left[\begin{array}{cc}
-4 & -8 \\
-2 & 0
\end{array}\right]\right)
$$

$X=\left[\begin{array}{cc}-2 & -2 \\ -1 & 5\end{array}\right]-\left[\begin{array}{cc}-1 & 0 \\ 0 & 2\end{array}\right]$
1.00
2.00

$$
=\left[\begin{array}{ccc}
-2+1 & -2 & -0 \\
-1-0 & 5 & -2
\end{array}\right]
$$

$=\left[\begin{array}{cc}-1 & -2 \\ -1 & 3\end{array}\right]$ Dons

$$
(i i i) 3 x+\left[\begin{array}{ccc}
1 & 0 & 2 \\
2 & 1 & 3 \\
4 & -1 & 5
\end{array}\right]=\left[\begin{array}{ccc}
-2 & 3 & 1 \\
-1 & -2 & 0 \\
0 & 1 & 5
\end{array}\right]
$$

$$
3 x=\left[\begin{array}{ccc}
-2 & 3 & 1 \\
-1 & -2 & 0 \\
0 & 1 & 5
\end{array}\right]-\left[\begin{array}{ccc}
1 & 0 & 2 \\
2 & 1 & 3 \\
4 & -1 & 5
\end{array}\right]
$$

$$
7.00 \mathrm{am} 3 x=\left[\begin{array}{ccc}
-2-1 & 3-0 & 1-2 \\
-1-2 & -2-1 & 0-3 \\
0-4 & 1+1 & 5-5
\end{array}\right]
$$

$$
3 X=\left[\begin{array}{rrr}
-3 & 3 & -1 \\
-3 & -3 & -3 \\
-4 & 2 & 0
\end{array}\right]
$$

$$
x=\frac{1}{3}\left[\begin{array}{ccc}
-3 & 3 & -1 \\
-3 & -3 & -3 \\
-4 & 2 & 0
\end{array}\right]
$$

Noon

$$
X=\left[\begin{array}{ccc}
-1 & 1 & -1 / 3 \\
-1 & -1 & -1 \\
-4 / 3 & 2 / 3 & 0
\end{array}\right] \text { Ans }
$$

(iv) $X+2 I=\left[\begin{array}{cc}3 & -1 \\ 1 & 2\end{array}\right]$
5.00

$$
\begin{aligned}
X & =\left[\begin{array}{cc}
3 & -1 \\
1 & 2
\end{array}\right]-2 I \\
& =\left[\begin{array}{cc}
3 & -1 \\
1 & 2
\end{array}\right]-2\left[\begin{array}{ll}
1 & 0 \\
0 & 1
\end{array}\right] \\
& =\left[\begin{array}{cc}
3 & -1 \\
1 & 2
\end{array}\right]-\left[\begin{array}{ll}
2 & 0 \\
0 & 2
\end{array}\right] \\
& =\left[\begin{array}{cc}
3-2 & -1-0 \\
1-0 & 2-2
\end{array}\right]=\left[\begin{array}{cc}
1 & -1 \\
1 & 0
\end{array}\right]
\end{aligned}
$$

6.00

Ans.

13 Friday
7000 Q5 product of Matrix
(i) $\left[\begin{array}{ccc}3 & 1 & -1 \\ 0 & -1 & 2\end{array}\right]\left[\begin{array}{cc}1 & -1 \\ 0 & 2 \\ 1 & 0\end{array}\right]$
$\frac{11.00}{}=\left[\begin{array}{ll}3+0+(-1) & -3+2-0 \\ 0+0+2 & 0-2+0\end{array}\right]$
Noon
$=\left[\begin{array}{ll}2 & -1 \\ 2 & -2\end{array}\right] \frac{\text { Ans }}{\overline{1}}$
200(ii) $\left[\begin{array}{lll}3 & -2 & 2\end{array}\right]\left[\begin{array}{c}1 \\ 2 \\ -2\end{array}\right]$

$$
=[3-4-4]
$$

$$
=[-5] \text { Ans }
$$

7.00 ar (iii) $\left[\begin{array}{lll}2 & -2 & -1\end{array}\right]\left[\begin{array}{lll}-1 & -1 & 5\end{array}\right]$
8.00

$$
\left[\begin{array}{ccc}
2 & -2 & -1 \\
1 & 1 & -2 \\
1 & 0 & -1
\end{array}\right]\left[\begin{array}{lll}
-1 & -2 & 5 \\
-1 & -1 & 3 \\
-1 & -2 & 4
\end{array}\right]
$$

$=\left[\begin{array}{lll}-2+2+1 & -4+2+2 & 10-6-4 \\ -1-1+2 & -2-1+4 & 5+3-8 \\ -1+0+1 & -2+0+2 & 5+0-4\end{array}\right]$
Noon $=\left[\begin{array}{lll}1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1\end{array}\right]$ Ans.
2.00 (iv) $\left[\begin{array}{ccc}-1 & -2 & 5 \\ -1 & -1 & 3 \\ -1 & -2 & 4\end{array}\right]\left[\begin{array}{ccc}2 & -2 & -1 \\ 1 & 1 & -2 \\ 1 & 0 & -1\end{array}\right]$

$$
\begin{aligned}
& =\left[\begin{array}{ccc}
-2-2+5 & 2-2+0 & 1+4-5 \\
-2-1+3 & 2-1+0 & 1+2-3 \\
-2-2+4 & 2-2+0 & 1+4-4
\end{array}\right] \\
& \\
& \\
& \text { 7.00 }
\end{aligned}
$$

$$
\text { Q6 } A=\left[\begin{array}{ll}
1 & 4 \\
2 & 1
\end{array}\right], B=\left[\begin{array}{cc}
-3 & 2 \\
4 & 0
\end{array}\right], C=\left[\begin{array}{ll}
1 & 0 \\
0 & 2
\end{array}\right] \text {. }
$$





5.00
6.00
7.00
(9) July
$\qquad$ Q7 $A=\left[\begin{array}{cc}-1 & 2 \\ 0 & 1\end{array}\right] \quad B=\left[\begin{array}{cc}1 & 0\end{array}\right]$ 8.00 9.00

$$
\begin{gathered}
(A+B)(A+B) \neq A^{2}+2 A B+B^{2} \\
(A+B)(A+B)
\end{gathered}
$$

$$
\Rightarrow\left(\left[\begin{array}{cc}
-1 & 2 \\
0 & 1
\end{array}\right]+\left[\begin{array}{cc}
1 & 0 \\
-1 & 2
\end{array}\right]\right) \cdot\left(\left[\begin{array}{cc}
-1 & 2 \\
0 & 1
\end{array}\right]+\left[\begin{array}{cc}
1 & 0 \\
-1 & 2
\end{array}\right]\right)
$$

$$
\begin{aligned}
& \Rightarrow\left(\left[\begin{array}{cc}
-1+1 & 2 \\
-1 & 3
\end{array}\right]\right) \cdot\left(\left[\begin{array}{cc}
0 & 2 \\
-1 & 3
\end{array}\right]\right) \\
& =\left[\begin{array}{cc}
0-2 & 0+6 \\
0-3 & -2+9
\end{array}\right]=\left[\begin{array}{cc}
-2 & 6 \\
-3 & 7
\end{array}\right]
\end{aligned}
$$

3.00 Now

$$
\begin{aligned}
& A^{2}+2 A B+B^{2} \\
& A^{2}=\left[\begin{array}{cc}
-1 & 2 \\
0 & 1
\end{array}\right] \cdot\left[\begin{array}{cc}
-1 & 2 \\
0 & 1
\end{array}\right]=\left[\begin{array}{cc}
1+0 & -2+2 \\
0+0 & 0+1
\end{array}\right] \\
&=\left[\begin{array}{ll}
1 & 0 \\
0 & 1
\end{array}\right]
\end{aligned}
$$

6.00

$$
\begin{aligned}
2 A B & =2\left[\begin{array}{cc}
-1 & 2 \\
0 & 1
\end{array}\right]\left[\begin{array}{cc}
1 & 0 \\
-1 & 2
\end{array}\right] \\
= & 2\left[\begin{array}{cc}
-1-2 & 0+4 \\
0-1 & 0+0
\end{array}\right]=2\left[\begin{array}{ll}
-3 & 4 \\
-1 & 0
\end{array}\right] \\
& =\left[\begin{array}{ll}
-6 & 8 \\
-2 & 0
\end{array}\right] \text { Ons }
\end{aligned}
$$

17 Tuesday

$$
\begin{aligned}
B^{2} & =\left[\begin{array}{cc}
1 & 0 \\
-1 & 2
\end{array}\right] \cdot\left[\begin{array}{cc}
1 & 0 \\
-1 & 2
\end{array}\right] \\
& =\left[\begin{array}{cc}
1-0 & 0+0 \\
-1-2 & 0+4
\end{array}\right]=\left[\begin{array}{cc}
1 & 0 \\
-3 & 4
\end{array}\right]
\end{aligned}
$$

1000

$$
A^{2}+2 A B+B^{2}
$$

$$
\left[\begin{array}{ll}
1 & 0 \\
0 & 1
\end{array}\right]+\left[\begin{array}{ll}
-6 & 8 \\
-2 & 0
\end{array}\right]+\left[\begin{array}{cc}
1 & 0 \\
-3 & 4
\end{array}\right]
$$

$$
=\left[\begin{array}{ll}
1-6+1 & 0+8+0 \\
0-2-3 & 1+0+4
\end{array}\right]
$$

$$
=\left[\begin{array}{cc}
-4 & 8 \\
-5 & 5
\end{array}\right] A^{2}+\angle A B
$$

So $(A+B)(A+B) \neq A^{2}+2 A B+B^{2}$
(b) $(A+B)(A-B) \neq A^{2}-B^{2}$

$$
\begin{aligned}
\Rightarrow A+B & =\left[\begin{array}{cc}
-1 & 2 \\
0 & 1
\end{array}\right]+\left[\begin{array}{cc}
1 & 0 \\
-1 & 2
\end{array}\right] \\
& =\left[\begin{array}{cc}
0 & 2 \\
-1 & 3
\end{array}\right]
\end{aligned}
$$

$$
|4-n| \quad r, \quad \text { Wednesday } 18
$$

$$
(A-B)=\left[\begin{array}{cc}
-1 & 2 \\
0 & 1
\end{array}\right]-\left[\begin{array}{cc}
1 & 0 \\
-1 & 2
\end{array}\right]
$$

800
$=\left[\begin{array}{cc}-2 & 2 \\ 1 & -1\end{array}\right]$

$$
\begin{aligned}
A^{2}-B^{2} & =\left[\begin{array}{ll}
1 & 0 \\
0 & 1
\end{array}\right]-\left[\begin{array}{ll}
1 \\
0 & 0 \\
3 & -3
\end{array}\right] \text { 006 }
\end{aligned}
$$

$$
\text { So }(4+B)(4-B) \neq A^{2}-B^{2}
$$

5.00
6.00
7.00

$$
\begin{aligned}
& 11.00 \\
& 11.00 \\
& \text { Noon } \\
& \begin{array}{ll} 
& B^{2}=\left[\begin{array}{cc}
1 & 0 \\
-3 & 4
\end{array}\right]
\end{array}
\end{aligned}
$$

$$
\begin{aligned}
& \begin{array}{c}
(A+B)(A-B) \\
A^{2}=\left[\begin{array}{cc}
1 & 0 \\
0 & 1
\end{array}\right]
\end{array} \\
& 10.00
\end{aligned}
$$

July
(12)

19 Thursday
Q8 (i) $\left[\begin{array}{ccc}-1 & 2 & 3 \\ 2 & 1 & 0 \\ 3 & 5 & -1\end{array}\right]\left[\begin{array}{l}a \\ b \\ c\end{array}\right]=\left[\begin{array}{c}-a+2 b+3 \\ 2 a+b \\ 3 a+5 b-c\end{array}\right]$
$\Rightarrow\left[\begin{array}{c}-a+2 b+3 c \\ 2 a+b+0 \\ 3 a+5 b-c\end{array}\right]=\left[\begin{array}{c}-a+2 b+3 c \\ 2 a+b \\ 3 a+5 b-c\end{array}\right)$
11.00

$$
\Rightarrow\left[\begin{array}{l}
-a+2 b+3 c \\
3 a+b \\
3 a+5 b-c
\end{array}\right]=\left[\begin{array}{l}
11
\end{array}\right]
$$

(ii) $\left[\begin{array}{ccc}\cos \theta & 0 & -\sin \theta \\ 0 & 1 & 0 \\ \sin \theta & 0 & \cos \theta\end{array}\right]\left[\begin{array}{ccc}\cos \theta & 0 & \sin \theta \\ 0 & 1 & 0 \\ -\sin \theta & 0 & \cos \theta\end{array}\right]$

$$
=\left[\begin{array}{lll}
1 & 0 & 0 \\
0 & 1 & 0 \\
0 & 0 & 1
\end{array}\right]
$$

$$
=\left[\begin{array}{lll}
\cos ^{2} \theta+0+\sin ^{2} \theta & 0+0+0 & \cos ^{2} \theta \sin \theta+0 \\
0+0+0 & 0+1+0 & 0+0+0 \\
0+0 \sin \alpha \\
\sin \theta \cos \theta+0-\cos \theta \sin \theta & 0+0+0 & \sin ^{2} \theta+0 \\
& +\cos ^{2} \theta
\end{array}\right]
$$

$=\left[\begin{array}{lll}1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1\end{array}\right]$ Ans
$Q_{9} .00 \mathrm{am} \quad A=\left[\begin{array}{cc}2 & -2 \sqrt{2} \\ \sqrt{2} & 2\end{array}\right] \quad B=\left[\begin{array}{cc}2 & 2 \sqrt{2} \\ -\sqrt{2} & 2\end{array}\right]$
$A$ \& $B$ commute.

$$
A B=B A
$$

10.00

$$
A B=\left[\begin{array}{cc}
2 & -2 \sqrt{2} \\
\sqrt{2} & 2
\end{array}\right]\left[\begin{array}{cc}
2 & 2 \sqrt{2} \\
-\sqrt{2} & 2
\end{array}\right]
$$

11.00

$$
=\left[\begin{array}{ll}
4+2(\sqrt{2})^{2} & 4 \sqrt{2}-4 \sqrt{2} \\
2 \sqrt{2}-2 \sqrt{2} & 2(\sqrt{2})^{2}+4
\end{array}\right]
$$

$1.00=\left[\begin{array}{ll}8 & 0 \\ 0 & 8\end{array}\right]$

$$
\begin{aligned}
B A & =\left[\begin{array}{cc}
2 & 2 \sqrt{2} \\
-\sqrt{2} & 2
\end{array}\right]\left[\begin{array}{cc}
2 & -2 \sqrt{2} \\
\sqrt{2} & 2
\end{array}\right] \\
& =\left[\begin{array}{cc}
4+2(\sqrt{2})^{2} & -4 \sqrt{2}+4 \sqrt{2} \\
-2 \sqrt{2}+2 \sqrt{2} & 2(\sqrt{2})^{2}+4
\end{array}\right] \\
& =\left[\begin{array}{cc}
8 & 0 \\
0 & 8
\end{array}\right]
\end{aligned}
$$

${ }_{7.00}$ So

$$
A B=B A
$$

Herce comuta.
8.00 pm

