

Paper: Final

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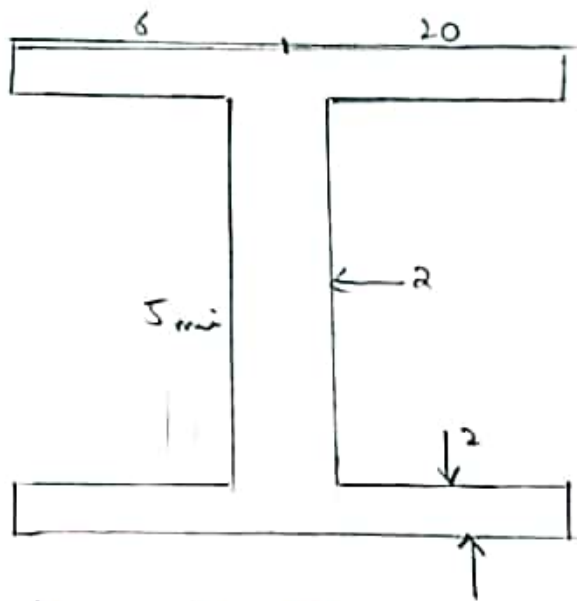
Sec: Sec "B"

Subject: MOSTII

Submitted To: Engg Saqib.

## Question 1

(a) Determine the location of the shear center for the beam having the cross sectional dimension - - - - -  
- - - - - center dimension.



Required:- location of shear center

Solution:-

As we know that

$$e = \frac{t_f b^2 h^2}{4I}$$

and

$$I = 2 \left( \frac{bh^3}{12} + Ay^2 \right) + \left[ \frac{bh^3}{12} + Ay^2 \right]$$

$$= 2 \left[ \frac{26(2)^3}{12} + (20 \times 2) \cdot (25)^2 \right]$$
$$+ \left[ \frac{2(50)^3}{12} + 0 \right]$$

$$I = 50034.66 + 20833$$

$$I = 70867.99 \text{ mm}^4$$

$$e = \frac{2(50)^2(25)^2}{4(70867.99)} = 11.02 \text{ mm}$$

So shear center  $e = 11.02 \text{ mm}$

Question: b

Determine the thickness of the walls of a water tank constructed from steel plates filled to a height of 26 ft - - - -  
- - - - - 62.4 lb/ft<sup>3</sup>

Data:

$$\Rightarrow H = 26 \text{ ft}$$

$\Rightarrow$  same diameter

$$D = 22 \text{ ft}$$

$\Rightarrow$  tangential stress = 6000 lb/ft

$\Rightarrow$  Specific weight of water tank = 62.4 lb/ft<sup>3</sup>

we have to find the thickness = ?

Solution:-

The pressure developed by water =

$$P = \gamma h$$

$$6t = \frac{PD}{2t}$$

$$6t = \frac{PD}{2t} \Rightarrow \frac{7hD}{2t}$$

$$2t \times 4 = 7hD$$

$$2t = \frac{\gamma h D}{\delta t}$$

$$t = \frac{\gamma h D}{\delta t \times 2}$$

$$t = \frac{\frac{(62.4)}{(12)^3} \times (26 \times 12) \times (22 \times 12)}{6000 \times 2}$$

$$t = 0.24''$$



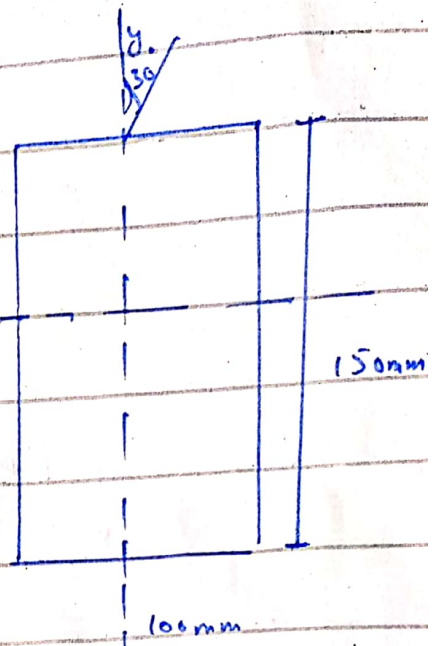
Q No: 2

Part (a)

Given, Data

$$w = 4 \text{ kN/m}$$

$$L = 3 \text{ m}$$



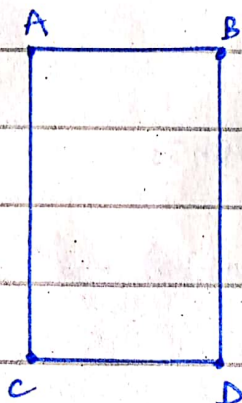
Required

Max Bending

$$\text{Stress} = ?$$

Sol:-

As the bending moment is maximum at extremes so we would find stresses at A, B, C & D as shown.





As we know that

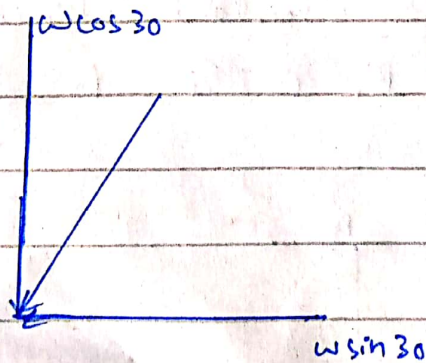
$$\sigma = \frac{M_x y}{I_x} + \frac{M_y x}{I_y}$$

We know have to find  
 $M_x$  &  $M_y$

As for simply supported  
we have

$$M_{ed} = \frac{w l^2}{8} \quad \dots (1)$$

Find the component of  $w$   
in  $x$  and  $y$  direction.



$$\text{So } M_x = \frac{(w \cos 30) \times l^2}{8}$$

$$M_x = \frac{(4 \times \cos 30) 3^2}{8}$$

$$M_x = 3.9 \text{ kN}\cdot\text{m}$$

Now

$$M_y = \frac{(4 \times \sin 30) \times 3^2}{8}$$

$$M_y = 2.25 \text{ kN}$$

$M_x$  is causing compression at A and B and tension at C and D.

$M_y$  is causing compression at B and D and tension at A and C.

Now  $I_x$  &  $I_y$

$$I_x = \frac{bh^3}{12} = \frac{0.1 \times 0.15^3}{12} = 2.815 \times 10^{-5}$$

$$I_y = \frac{hb^3}{12} = \frac{0.15 \times 0.1^3}{12} = 1.25 \times 10^{-8} \text{ m}^4$$

Now stress at External Fiber.

$$\sigma_x = \frac{M_y}{I_x} = \frac{3.9 \times 0.075}{2.815 \times 10^{-5}}$$



$$\sigma_x = 10390.7 \text{ kN/m}^2$$

$$\sigma_y = \frac{2.25 \times 0.05}{1.25 \times 10^{-5}}$$

$$\sigma_y = 9000 \text{ kN/m}^2$$

Now

Taking tension + ↑

$$\text{stress at A} = \frac{M_{xy}}{I_x} + \frac{M_{yx}}{I_y}$$

$$= -10390.7 + 9000$$

$$= -1390.7 \text{ kN/m}^2 (\text{comp})$$

$$\text{at B} = \frac{M_{xy}}{I_x} + \frac{M_{yx}}{I_y}$$

$$= -10390.7 - 9000$$

$$\sigma \text{ at B} = -19390.7 \text{ kN/m}^2 (\text{comp})$$

Now

$$\text{Stress at C} = \frac{M_{xy}}{I_x} + \frac{M_{yx}}{I_y}$$

$$= 10390.7 + 9000$$

$$= 19390.7 \text{ kN/m}^2 \text{ (Tension.)}$$

$$\text{Stress at D} = \frac{My}{I_x} + \frac{My}{I_y}$$

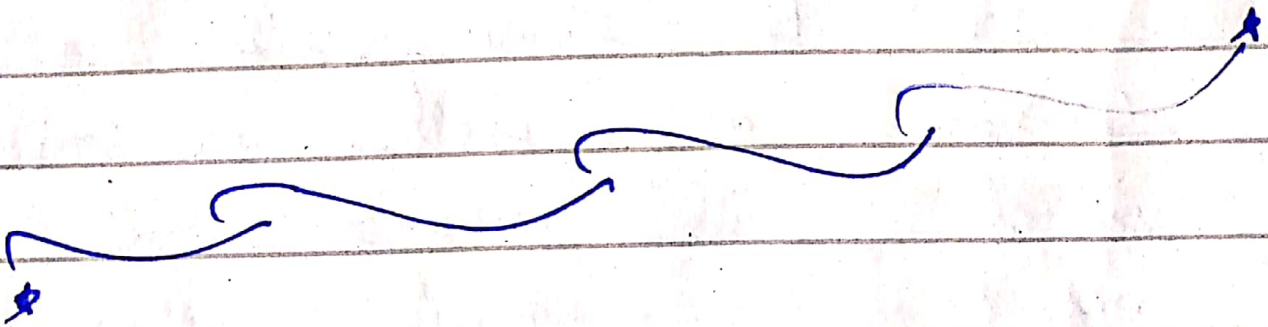
$$= 10390.7 - 9000$$

$$= 1390.7 \text{ kN/m (Tension)}$$

so the maximum stress are on

B and C

⇒ B is under compression  
of 19390.7 & C is  
under tension of the same  
value.





Q No: 2

Part (b)

Given Data

$L = 16 \text{ ft}$

$I_x = 112.6 \text{ in}^4$

$I_y = 18.7 \text{ in}^4$

$\sigma_c = 12000 \text{ psi}$

$\sigma_T = 5000 \text{ psi}$

Sol:

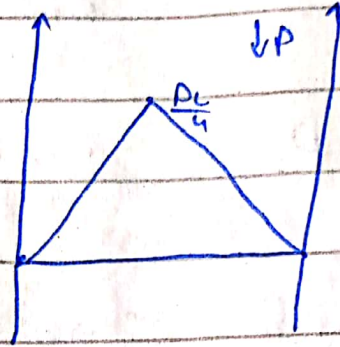
By looking to the figure to we can judge that Max compression would occur on A & C and Max Tension at B. There will be tension as well as compression which will reduced that effects of each other calculate stress at A & C.

So

$$\sigma_A = \frac{M y_x}{I_x} + \frac{M y_y}{I_y} \text{ (Comp)}$$

$$\sigma_c = \frac{M_{xy}}{I_{xx}} + \frac{M_{yx}}{I_{yy}} \quad (\text{Tension})$$

Now  $M_x$  &  $M_y$



$$\text{So } M_x = \frac{P \cos 60^\circ \times (16 \times 12)}{4}$$

$$M_x = 48P \cos 60^\circ$$

$$M_y = \frac{P \sin 60^\circ (16 \times 12)}{4}$$

$$M_y = 48P \sin 60^\circ$$

Now

$$\sigma_A = \frac{M_{xy}}{I_{xx}} + \frac{M_{yx}}{I_{yy}}$$

$$1200 = \frac{48P \cos 60^\circ \times 30.027}{112.6}$$

$$= \frac{48P \sin 60^\circ \times 3}{18.7}$$

Solving the equation.

$$\text{Now } = \frac{M_{xy}}{I_{yy}} + \frac{M_{yx}}{I_{xx}}$$



$$5000 = \frac{48 P \cos 60 \times 5.93 + 48 P \sin 60 \times 0.15}{112.6 - 18.7}$$

Solving the equation

$$P = 2104.9 \text{ lb}$$

So the maximum load "P" applied should be 1638.6 lb.

Q No: 3

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Given Data:

Length,  $L = 10 \text{ ft}$

Breadth,  $b = 0.75 \text{ in}$

height,  $h = 2 \text{ in}$

Factor of Safety = 2

$E = 10.3 \times 10^6$

Required:

Safe load,  $P_{\text{safe}} = ?$

SOL:-

CASE I:

Strut column act as a hinged column about an axis perpendicular to the 2 in dimension then.

$$I = I_r = \left( \frac{3}{4} \right) (2)^3 = 0.5 \text{ in}^4$$

21 19  
 $l_e = L$  For Hinged ended column

$$P_{cr} = \frac{n^2 EI \pi^2}{l_e^2}$$

$$P_{cr} = \frac{1^2 (10.3 \times 10^6) (0.5) (3.14)^2}{(10 \times 12)^2}$$

$$P_{cr} = 3526.17$$

$$P_{safe} = \frac{P_{cr}}{\text{factor of safety}}$$

$$P_{safe} = \frac{3526.17}{2} = 1763.08$$

$$P_{safe} = 1763.08$$

CASE 2 :-

Column act as a fixed end about axis parallel to z-axis i.e. y-axis

$$I = I_y = \frac{2 \times (0.75)^3}{12}$$



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$$I_y = 0.07 \text{ m}^4$$

Now For fixed ended  $l_e = \frac{L}{2}$

$$P_{cr} = \frac{(1.1)^2 (10.3 \times 10^6) (0.07) (3.14)^2}{120/2}$$

$$P_{cr} = 1974.65 \text{ lb}$$

For  $P_{safe}$

$$P_{safe} = \frac{P_{cr}}{\text{Factor of Safety}}$$

$$P_{safe} = \frac{1974.65}{2}$$

$$P_{safe} = 987.32 \text{ lb}$$

In both case we take smaller value of safe.

$$P_{safe} = 987.32 < 1763.07$$