

Mid term paper

Name

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ID

2807

Section

A'

Subject

PRLD - I

Submitted to

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(1)

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Section: A7

Q:1 Given data :-

$$\text{Live load (L-L)} = 2.47 \text{ kips/ft}$$

$$\text{Dead load (D.L)} = 1.05 \text{ kips/ft.}$$

$$\text{height (h)} = 20''$$

$$\text{width (b)} = 10''$$

$$\text{full span} = 18'$$

$$f'_c = 4000 \text{ psi} = 4 \text{ ksi}$$

$$f_y = 60000 \text{ psi} = 60 \text{ ksi}$$

Solution :-

⇒ Step # 01 :-

$$\begin{aligned} \text{Effective depth} &= d = h - 3 \\ &= 20 - 3 = 17'' \end{aligned}$$

$$\text{Effective cover} = d' = 2.5''$$

$$\begin{aligned} \rho_{\max} &= 0.85 \times \beta \times \frac{f'_c}{f_y} \times \left(\frac{\epsilon_u}{\epsilon_u + \epsilon_y} \right) \\ &= 0.85 \times 0.85 \times \frac{4}{60} \times \left(\frac{0.003}{0.003 + 0.005} \right) \end{aligned}$$

(2)

Name: Rizwan ullah khan

ID # 7807

Section: A

$$\rho_{max} = 0.0180$$

⇒ Step #02 :-

Find the area of steel :-

$$\rho_{max} = \frac{A_{st}}{b \times d} \Rightarrow A_{st} = \rho_{max} \times (b \times d)$$

$$A_{st} = 0.0180 \times (10 \times 17)$$

$$A_{st} = 3.06 \text{ in}^2$$

⇒ Step #03 :-

Design moment:

$$M_{u2} = \phi \times A_{st} \times f_y \times (d - a/2)$$

$$a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b} = \frac{3.06 \times 60}{0.85 \times 40 \times 10} = 5.4''$$

$$M_{u2} = 0.90 \times 3.06 \times 60 \times (17 - 5.4/2)$$

$$M_{u2} = 2362.9 \text{ kip-inch}$$

(3)

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ID # 7807

Section:- A'

Moment produced by given load.

$$\text{Self weight of beam} = \frac{10}{12} \times \frac{20}{12} \times 150$$

$$= 208.3 \text{ lb/ft}$$

$$\text{Factored load} = 1.2(1050 + 208.3) + 1.6(2470)$$

$$= 5.46 \text{ kips/ft.}$$

$$\text{Ultimate factored load} = \frac{wL^2}{8}$$

$$= \frac{5.46 \times (18)^2}{8} \times 12$$

$$M_u = 2653.5$$

As

$$M_u < M_v$$

$$2362.9 < 2653.5$$

↓
Required double Reinforcement.

(4)

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Section: A'

⇒ Step # 04

$$M_u = 2653.56 - 2362.9$$

$$= 290.64 \text{ kip-inch}$$

⇒ Step # 05

Steel Area in Compression:

$$M_u = \phi \times A'_{st} \times f_y \times (d - d')$$

$$A'_{st} = \frac{M_u}{\phi \times f_y \times (d - d')}$$

$$= \frac{290.64}{0.90 \times 60 \times (17 - 2.5)}$$

$$\boxed{A'_{st} = 0.37 \text{ in}^2}$$

⇒ Step # 06

$$A_s = A_{st} + A'_{st}$$

$$A_s = 3.06 + 0.37$$

$$\boxed{A_s = 3.43 \text{ in}^2}$$

(5)

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Section: A

⇒ Step #07:-

As we use #8 bar which dia is 1"

$$\text{Area} = 0.785 \text{ in}^2$$

Calculate No. of bars:-

$$\begin{aligned} \text{No. of bars} &= \frac{A_{st}}{\text{Area of 1 bar}} \\ &= \frac{3.43}{0.785} = 4.36 \end{aligned}$$

No. of bars = 5 bars → Tensile zone.

For Compression:-

use #6 bar ⇒ dia 0.75"

$$\text{Area} = 0.44 \text{ in}^2$$

$$\text{No. of bars} = \frac{A'_{st}}{\text{Area of 1 bar}} = \frac{0.37}{0.44} = 0.84$$

No. of bars = 1 bar → Compression zone.

(6)

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ID # 7807

Section: 'A'

Step # 08:-

Minimum width of beam:-

$$b_{min} = 2(1.5) + 2\left(\frac{3}{8}\right) + 5(1) + 4(1)$$

$$= 12.75 > 10'' \Rightarrow \text{Multiple Layers.}$$

$$\text{Effective depth } (d) = 20 - 1.5 - \frac{3}{8} - \frac{3}{8} - \frac{1}{2}\left(\frac{6}{8}\right)$$

$$\boxed{d = 16.62}$$

$$\text{Effective Cover} = (d') = 1.5 + \frac{3}{8} + \frac{1}{2}\left(\frac{6}{8}\right)$$

$$\boxed{d' = 2.25''}$$

Moment of design is given by,

$$M_d = \phi \times \left[A_{st}' \times f_y \times (d - d') + (A_{st} - A_{st}') \times f_y \times (d - \frac{a}{2}) \right]$$

$$a = \frac{(A_{st} - A_{st}') \times f_y}{0.85 \times f_c' \times b}$$

$$= \frac{(5 \times 0.785 - 1 \times 0.44) \times 60}{0.85 \times 4 \times 10} = 6.15''$$

(7)

Name: Rizwan Allah Khan ID # 7807

Section: 'A'

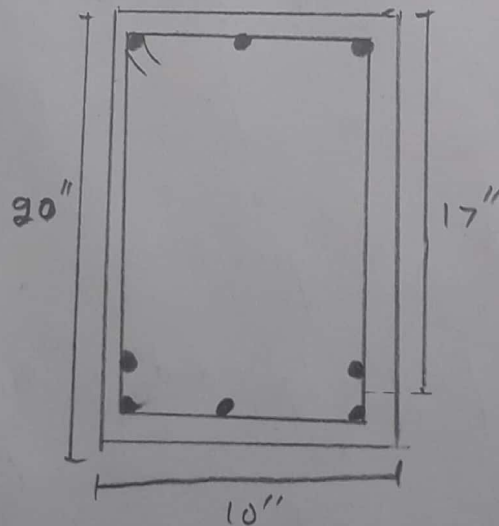
$$M_d = 0.90 \times \left[(1 \times 0.44) \times 60 \times (16.62 - 2.25) + (5 \times 0.785 - 1 \times 0.44) \times 60 \times \left(16.62 - \frac{6.15}{2}\right) \right]$$

$$M_d = 2890.46$$

So

$$M_d = 2890.46 > 2653.56$$

and design is correct.



⑧

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ID # 7807

Section: 'A'

Q:- 2/

A) Bond stress:-

The stress which is acting on the outer interface of steel to the surrounding concrete is called Bond stress.

OR

Bond stress is the result of the bonding between the concrete surface and reinforcement steel. Bond stress resist any force that tries to pull out the rods from the concrete.

Development length:-

Development length can be defined as the length of the bar required for transferring the stress into the concrete.

OR

The quantity of the rebar length ~~is~~ that ~~quantity~~ is actually required to be enclosed into the concrete to make desired bond strength between two materials.

(9)

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Section: 'A'

Q:- 2/ b)

Condition for using doubly reinforced beam:-

Conditions:-

- When the cross section of the beam is fixed.
- When moment to be carried by the beam is more than the balanced moment.
- ⇒ In case of a continuous beam.
- ⇒ The portion of the beam over middle support in continuous T beams has to be designed as doubly reinforced section.
- ⇒ When dimensions of the beam are restricted for architectural or structural purposes.

(10)

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Section: 'A'

Q: 2/ part (c)

T-beam:-

⇒ T-beam is more economical than rectangular beam.

⇒ In case of T-beam slab & beam are connected with one another and act as a one member.

⇒ It consist of T-shaped structure.

⇒ Analysis is required when

$$a > h_f.$$

a = depth

h_f = Slab thickness.

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Section: 'A'

Rectangular beam:-

- ⇒ Rectangular beam is less economically than T-beam.
- ⇒ In case of rectangular beam slab has been placed on the beam and there is no connection b/w slab & beams.
- ⇒ It is generally used as compression in top fiber and tension in bottom fibre.
- ⇒ It is most commonly used in office/commercial buildings.
- ⇒ Analysis is required when

$$a \leq h_f$$

a = depth

h_f = height of flange.

(12)

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Q: 21 Part - d

Effect of Strength Reduction Factor
in flexural strength:-

In design of flexural strength the strength reduction factor decrease from tension ~~test~~ controlled section to compression controlled section to increase safety.

Basically it represent the uncertainty in determine the member behavior to the type of stresses to which it is subjected.

Strength Reduction factor is denoted by " ϕ "

Q: 21 Part 'E'

Designing method:-

Two methods are used to design concrete & different structures.

(13)

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Section: 7A'

1- ASD Method (Allowable stress design)

2- USD Method (Ultimate strength design)

1- ASD Method:

It is also known as working stress design method.

⇒ In this method, all loads are taken as service loads and no factors is applied to increase the service load.

⇒ It is based on principle that stress developed in structural members should not exceed a certain limit of elastic limit.

2- USD Methods:

This method is best for designing different structural members. because of following reasons.

(14)

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ID # 7807

Section: 'A'

*- USD method result in more economical designed for a building with fewer special needs for customized area.

* - The ultimate strength of material is considered we can get much slender section for column and beam compared to other method.

⇒ This method is also known as load factor method.

Q: 31 Given data:

height of flange = $h_f = 6''$

C/C distance b/w beams = $10'$

width of web = $14''$

Span = $32'$

Total depth = $28''$

D.L = 50 p.s.f

L.L = 225 p.s.f

$f_y = 60,000 \text{ psi}$

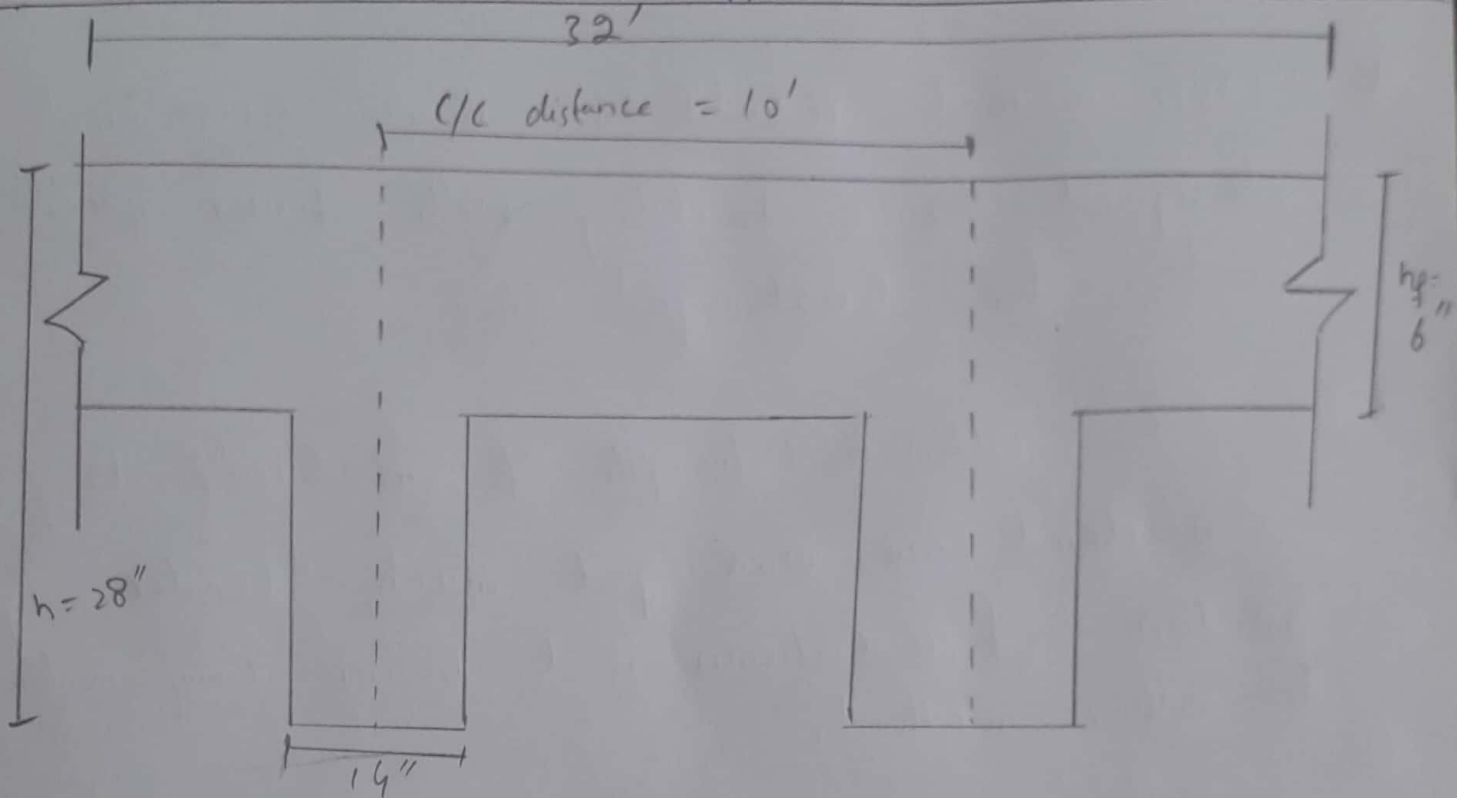
$f'_c = 4,000 \text{ psi}$

(18)

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10 # 7807

Section: A-A'

Soln

$$\text{Effective depth } (d) = h - 3$$

$$= 28 - 3$$

$$d = 25''$$

Step # 01 :-

we know that

$$M_D = \frac{wL^2}{8}$$

Find 'w'

(16)

Name: Rizwan ullah khan

ID# 2807

Section 'A'

$$W_t = b \times t \times r_c$$

$$= \frac{14}{12} \times \frac{28}{12} \times 150$$

$$W_t = 408.34 \text{ lb/ft}$$

Total Factor Load:-

$$= 1.2 \text{ DL} + 1.6 \text{ L-L}$$

$$= 1.2(50 + 408.34) + 1.6(225)$$

$$= 910.1 \text{ lb/ft}$$

$$= 0.9101 \text{ kip/ft}$$

Total Factored moment:-

$$M_u = \frac{wL^2}{8} = \frac{0.910 \times (32)^2}{8} \times 12$$

$$M_u = 1397.76 \text{ kip-inch}$$

Step # 02:-

Analysis for T-beam or rectangular:

(17)

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Section 'A'

$$\Rightarrow a = h_f = 6''$$

Area of steel

$$A_{st} = \frac{M_u}{\phi \times f_y \times (d - a/2)}$$

$$= \frac{1397.76}{0.90 \times 60 \times (25 - 6/2)} = 1.17 \text{ in}^2$$

\Rightarrow By formula of 'a'

$$a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b} = \frac{1.17 \times 60}{0.85 \times 4 \times 96} = 0.226''$$

if a is less than height of flange
So we have to design Rectangular beam.

$$A_{st} = \frac{M_u}{\phi \times f_y \times (d - a/2)} = \frac{1397.76}{0.90 \times 60 \times (25 - \frac{0.2}{2})}$$

$$\boxed{A_{st} = 1.03 \text{ in}^2}$$

(18)

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ID # 7807

Section: 'A'

⇒ now

$$a = \frac{A_{st} \times f_y}{0.85 \times f_c \times b} = \frac{1.03 \times 60}{0.85 \times 4 \times 96} = 0.19''$$

So

$$A_{st} = \frac{M_u}{\phi \times f_y \times (d - a/2)} = \frac{1397.6}{0.90 \times 60 \times (25 - \frac{0.19}{2})}$$

$$\boxed{A_{st} = 1.03 \text{ in}^2}$$

So Area of steel of both is same.

Step # 03:

Reinforcement Ratio:-

$$\Rightarrow \rho_{max} = 0.85 \times \beta \times \frac{f_c'}{f_y} \times \left(\frac{\epsilon_u}{\epsilon_u + \epsilon_y} \right)$$

$$= 0.85 \times 0.85 \times \frac{4}{60} \times \left(\frac{0.003}{0.003 + 0.005} \right)$$

$$\boxed{\rho_{max} = 0.018}$$

$$\Rightarrow \rho_{min} = \frac{200}{f_y} = \frac{200}{60,000}$$

$$\boxed{\rho_{min} = 0.003}$$

(19)

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ID# 7807

Section: A'

$$\Rightarrow \rho = \frac{A_{st}}{b \times d} = \frac{1.03}{14 \times 25} = 0.002$$

$$\boxed{\rho = 0.002}$$

Check the order

$$\rho_{min} < \rho < \rho_{max}$$

$$0.003 < 0.002 < 0.018$$

if ρ is less than ρ_{min} , so find A_{st} on ρ_{min} then

$$\rho_{min} = \frac{A_{st}}{b \times d} \Rightarrow A_{st} = \rho_{min} \times b \times d$$

$$A_{st} = 0.003 \times 14 \times 25$$

$$\boxed{A_{st} = 1.05 \text{ in}^2}$$

Step # 04

No: of Bar required:

We use # 8 bar, Dia = (8/8) = 1"

$$\text{Area} = \frac{\pi}{4} \left(\frac{8}{8} \right)^2 = 0.785 \text{ in}^2$$

(20)

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ID # 7807

Section "A"

$$\text{No. of Bars} = \frac{\text{Area of Steel}}{\text{Area of Single Bar}} = \frac{1.05}{0.785} = 1.3$$

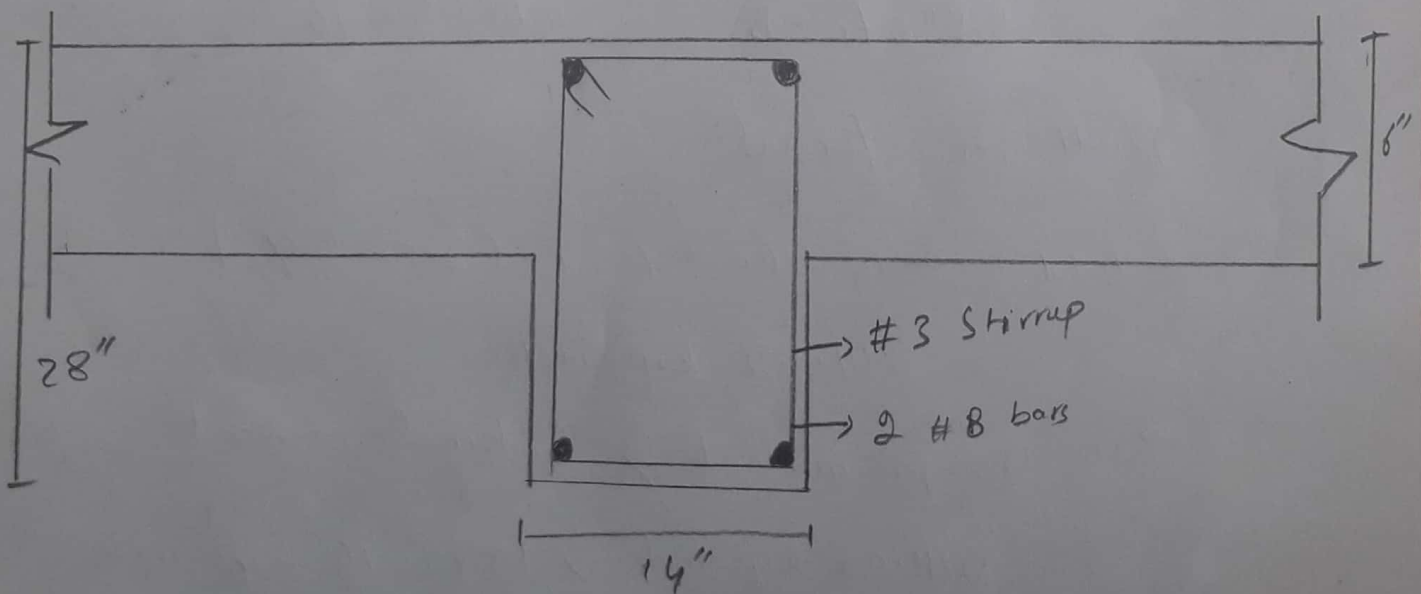
$$\boxed{\text{No. of Bars} = 2} \Rightarrow \#8 \text{ bars}$$

Step #05

width of Accomodation of Bars:

$$b_{min} = 2(1.5) + 2\left(\frac{3}{8}\right) + 2\left(\frac{0}{2}\right) + 1\left(\frac{0}{2}\right)$$

$$= 6.75" < 14" \Rightarrow \text{we will used Single Layer of bar.}$$



(21)

Name: Rizwan Ullah Khan

ID # 7807

Section: 'A'

Step # 6 :-

Moment Design:

$$M_d = \phi \times f_y \times A_{st} \times (d - a/2)$$

$$\text{No. of bars} = \frac{\text{Area of steel}}{\text{Area of single bars}}$$

$$A_{st} = \text{No. of bars} \times \text{Area of ~~steel~~ single bar.}$$

$$A_{st} = 2 \times 0.785$$

$$A_{st} = 1.57 \text{ in}^2$$

Now

$$a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b} = \frac{1.57 \times 60}{0.85 \times 4 \times 96} = 0.24$$

Put in formula

$$M_d = 0.90 \times 60 \times 1.57 \times (25 - 0.24/2)$$
$$= 2111.09 \text{ kip-inch}$$

So Design moment > External moment

$$2111.09 \text{ kip-inch} > 1397.76 \text{ kip-inch}$$

Design is correct.