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ANS 1

$$\begin{bmatrix} 1 & 103 & 3 & 0 & 5 \\ 0 & 1 & -10 \text{ LAST} & 0 & 7 \\ 0 & 0 & 1 & 0 & -6 \\ 0 & 0 & 0 & 1 & 103 \end{bmatrix}$$

Sol:-

ID = 15870

$$\begin{bmatrix} 1 & 8 & 3 & 0 & 5 \\ 0 & 1 & -3 & 0 & 7 \\ 0 & 0 & 1 & 0 & -6 \\ 0 & 0 & 0 & 1 & 8 \end{bmatrix}$$

Now Apply Row operation

$$\begin{bmatrix} 1 & 0 & 27 & 0 & -51 \\ 0 & 1 & -3 & 0 & 7 \\ 0 & 0 & 1 & 0 & -6 \\ 0 & 0 & 0 & 1 & 8 \end{bmatrix} \quad R_1 - 8R_4$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 & 111 \\ 0 & 1 & -3 & 0 & 9 \\ 0 & 0 & 1 & 0 & -6 \end{bmatrix} \quad R_1 - 27R_3$$

$$\sim \begin{bmatrix} -8 & 0 & 0 \\ -1 & 5 & 8 \\ 1 & -4 & 13 \end{bmatrix} \text{ interchange } R_1 \text{ and } R_3$$

$$\sim \begin{bmatrix} -8 & 0 & 0 \\ 0 & -2 & -17 \\ 1 & 5 & 8 \\ 1 & -4 & 13 \end{bmatrix} R_2 - 2R_1$$

$$\sim \begin{bmatrix} -8 & 0 & 0 \\ 0 & -2 & -17 \\ 0 & 40 & 64 \\ 1 & -4 & 13 \end{bmatrix} 8R_3 + R_1$$

$$\sim \begin{bmatrix} -8 & 0 & 0 \\ 0 & -2 & -17 \\ 0 & 0 & 64 \\ 1 & -4 & 13 \end{bmatrix} R_3 + 20R_2$$

$$\sim \begin{bmatrix} -8 & 0 & 0 \\ 0 & -2 & -17 \\ 0 & 0 & 64 \\ 1 & -4 & 13 \end{bmatrix}$$

Ans 2 Part A

$$\begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 2 & -5 & -1 \end{bmatrix} \quad \begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 0 & 3 & -5 \end{bmatrix}$$

$$A_2 \begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 2 & -5 & -1 \end{bmatrix}$$

$$A_2 \begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 0 & 3 & -5 \end{bmatrix} \quad R_3 - 2R_2$$

$$\underline{B} \begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 0 & 3 & -5 \end{bmatrix}$$

$$\underline{B} \begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 2 & -5 & -1 \end{bmatrix} \quad R_3 + 2R_2$$

Ans 2

Part (B)

$$\underline{B} = \begin{bmatrix} 1 & 0 & \pi \\ 0 & 1 & e \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

Sol:-

$$\begin{bmatrix} 1 & 0 & \pi \\ 0 & 1 & e \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} \textcircled{1} & 0 & \uparrow \\ 0 & \textcircled{1} & e \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

These are echelon form A matrix (A) is said to (i) The first non-zero element in each row is called its leading entry is 1.

Ans 3 Part A

- (i) It is in row echelon form
(ii) The leading entry in each row is a 1 (called a leading 1).

(iii)

Each column containing a leading 1 has zero in all its other.

For example:-

$$\begin{bmatrix} 1 & 0 & a_1 & 0 & b_1 \\ 0 & 1 & a_2 & 0 & b_2 \\ 0 & 0 & 0 & 1 & b_3 \end{bmatrix}$$

* Practical use of Reduced Row Echelon Form:-

Reduce row echelon form is a type of matrix used to solve systems of linear equation. It has four main required which

seems to be very inefficient
and an easy way to make
mistake.

Ans 3 Part (B)

(B)

$$\begin{bmatrix} 1 & 1D2 & 8 \\ 2 & 8 & -1 \\ -1D3 & 0 & 0 \\ 1 & -4 & 1D\text{-first last} \end{bmatrix}$$

(b) Sol:

$$\begin{bmatrix} 1 & 1D2 & 8 \\ 2 & 8 & -1 \end{bmatrix}$$

$$\begin{pmatrix} 1 & 0 & 0 & 7 & 0 \\ 0 & 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 4 & 0 \end{pmatrix}$$

linear equation -

Give one example.

Sol (A)

Difference b/w Row Echelon Form and reduced row echelon Form:-

The matrix in row echelon form meets the following requirements (i) The first non-zero number from the left is always to the right of the first non-zero number in the row above.

(ii) Rows consisting of all zero are at the bottom of the matrix.

For Example
$$\begin{bmatrix} 1 & a_0 & a_1 & a_2 & a_3 \\ 0 & 0 & 2 & a_4 & a_5 \\ 0 & 0 & 0 & 1 & a_6 \end{bmatrix}$$

1) But on the other hand reduced row echelon form meets different

ANS NO 2 Part NO B 4 parts

Part NO 1 A

$$\begin{bmatrix} e & 0 & 0 & 0 \\ 0 & \pi & 0 & 0 \\ 0 & 0 & -\pi & 0 \\ 0 & 0 & 0 & e \end{bmatrix}$$

Sol:-

$$\begin{bmatrix} e & 0 & 0 & 0 \\ 0 & \pi & 0 & 0 \\ 0 & 0 & -\pi & 0 \\ 0 & 0 & 0 & e \end{bmatrix} \text{ is in echelon form}$$

yes in echelon form because
no of zero increases as
we goes down row
by row before 1st non-
zero.

$$\sim \begin{bmatrix} 1 & 0 & 0 \\ 0 & 0.8 & 0.08 \\ 0 & 0 & 64 \\ 0 & 0 & 0.32 \end{bmatrix} \cdot 376R_2 + R_3$$

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AAns 2 Par(●) CPar C

$$C = \begin{bmatrix} 5 & 0 & 0 & 7 \\ 0 & 1 & 0 & 5 \\ 0 & 0 & 1 & 4 \end{bmatrix}$$

Sol:

$$\begin{bmatrix} 5 & 0 & 0 & 7 \\ 0 & 1 & 0 & 5 \\ 0 & 0 & 1 & 4 \end{bmatrix}$$

$$\begin{bmatrix} 5 & 0 & 0 & 7 \\ 0 & \textcircled{1} & 0 & 5 \\ 0 & 0 & \textcircled{1} & 4 \end{bmatrix}$$

Its in echelon form because it satisfies the 4th condition that is in a column that contains the leading entry of row all the other element are zero.

* Augmented Matrix converted into System of linear form :-

$$1x_1 = 111, \quad x_2 = -11$$

$$x_1 = 111$$

$$x_3 = -6, \quad x_4 = 8 \text{ Ans}$$

Ans 2 Part (A)

(A)

$$\begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 2 & -5 & -1 \end{bmatrix} \rightarrow$$

$$\begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 0 & 3 & -5 \end{bmatrix}$$