

Name : Salman Khan

ID no: 16208

Semester: 2nd

Dept.: Electrical.

Subject: Linear Circuit analysis

Assignment:

Ques - Solve the following questions from  
text book.

- (i) Chapter 4: 2, 10, 13, 19, 29, 32, 35, 46, 47  
(ii) Chapter 5: 10, 11, 13, 25, 29

### Chapter 4

Q<sup>2</sup>) Evaluate the following determinants.

$$(a) \begin{vmatrix} 2 & 1 \\ -4 & 3 \end{vmatrix} \quad \text{and} \quad \begin{vmatrix} 0 & 2 & 11 \\ 6 & 4 & 1 \\ 3 & -1 & 5 \end{vmatrix}$$

Soln

The first determinant is simply  
evaluated as.

$$\begin{vmatrix} 2 & 1 \\ -4 & 3 \end{vmatrix} = (2 \times 3) - (1 \times (-4))$$

$$= 6 - (-4)$$

$$= 6 + 4$$

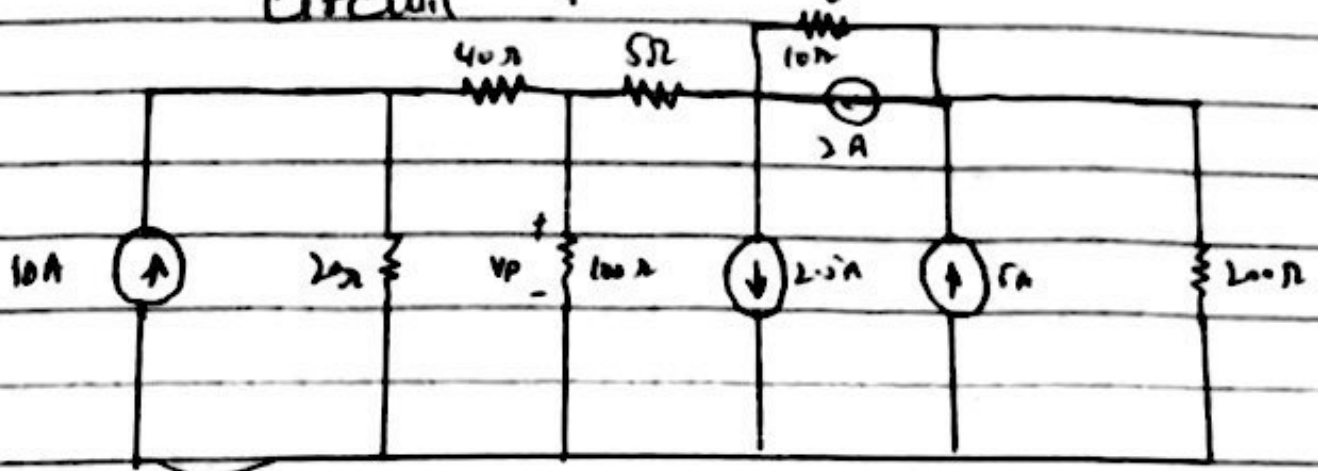
$$\boxed{\det(A) = 10}$$

b) evaluate determinant from the first column.

$$\begin{vmatrix} 0 & 2 & 11 \\ 6 & 4 & 1 \\ 3 & -1 & 5 \end{vmatrix} = 0 \begin{vmatrix} 4 & 1 \\ -1 & 5 \end{vmatrix} - 6 \begin{vmatrix} 2 & 11 \\ -1 & 5 \end{vmatrix} + \begin{vmatrix} 2 & 11 \\ 4 & 1 \end{vmatrix}$$

$$\begin{aligned}
 &= 0(4 \times 5 - 1 \times (-1)) - 6(2 \times 5 - 11 \times (-1)) + 3(2 \times 1 - 11 \times 4) \\
 &= 0(22) - 6(21) + 3(-42) \\
 &= 0 - 126 - 126 \\
 &= 0 - 252 \\
 &\boxed{\text{detc } (B) = -252}
 \end{aligned}$$

Q12 Use nodal analysis to find up in the circuit



Sol

Apply KCL to node  $V_1$  give

$$10 = \frac{V_1}{20} + \frac{V_1 - V_P}{40} \quad \text{--- (1)}$$

Apply KCL to node  $V_P$  give

$$0 = \frac{V_P - V_1}{40} + \frac{V_P}{100} + \frac{V_P - V_2}{50} \quad \text{--- (2)}$$

Apply KCL to node  $V_2$  give

$$2 - 2.5 = \frac{V_2 - V_P}{50} + \frac{V_2 - V_2}{10} \quad \text{--- (3)}$$

Apply KVL to node  $V_3$

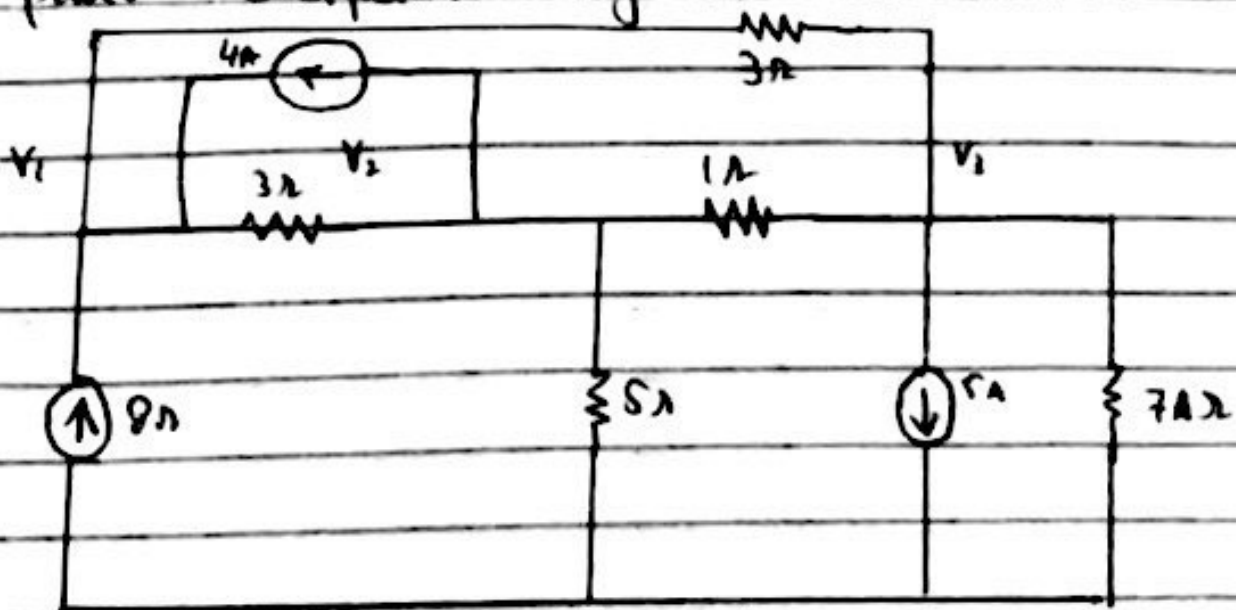
$$5 - 2 = \frac{V_3 - V_2}{10} + \frac{V_3}{20} \quad \text{--- (3)}$$

Solve the four equations:

of (1), (2), (3), and (4) to

$$V_p = 171.639 \text{ V}$$

(13) Using the bottom node as reference determine the voltage across the  $5\Omega$  resistor in the circuit of fig 4.31, and calculate the power dissipated by the  $7\Omega$  resistor.



Sol

The voltage across the  $9\text{A}$  current source to be  $V_1$ , while  $V_2$  denote the voltage across the  $5\Omega$  resistor, finally the voltage across the  $7\Omega$  resistor is labeled as  $V_3$ .

From the node  $V_1$

$$-8 - 4 + \frac{V_1 - V_2}{3} + \frac{V_1 - V_3}{3} = 0$$

$$\left(\frac{1}{3} + \frac{1}{3}\right)V_1 - \left(\frac{1}{3}\right)V_2 - \left(\frac{1}{3}\right)V_3 = 12$$

$$2V_1 - V_2 - V_3 = 36 \quad \text{--- (1)}$$

From node  $V_2$ :

$$4 + \frac{V_2 - V_1}{3} + \frac{V_2}{5} + \frac{V_2 - V_3}{1} = 0$$

$$-\left(\frac{1}{3}\right)V_1 + \left(\frac{1}{3} + \frac{1}{5} + \frac{1}{1}\right)V_2 - V_3 = -4$$

$$-5V_1 + 23V_2 - 15V_3 = -60 \quad \text{--- (2)}$$

From node  $V_3$

$$5 + \frac{V_3 - V_2}{1} + \frac{V_3 - V_1}{9} + \frac{V_3}{7} = 0$$

$$-\left(\frac{1}{3}\right)V_1 - V_2 + \left(1 + \frac{1}{9} + \frac{1}{7}\right)V_3 = -5$$

$$-7V_1 - 21V_2 + 31V_3 = -105 \quad \text{--- (3)}$$

Solve the three eq. (1), (2) and (3)

$$V_1 = 26.733V$$

$$V_2 = 8.833V$$

$$V_3 = 8.633V$$

Thus  $V_{SD} = V_2$

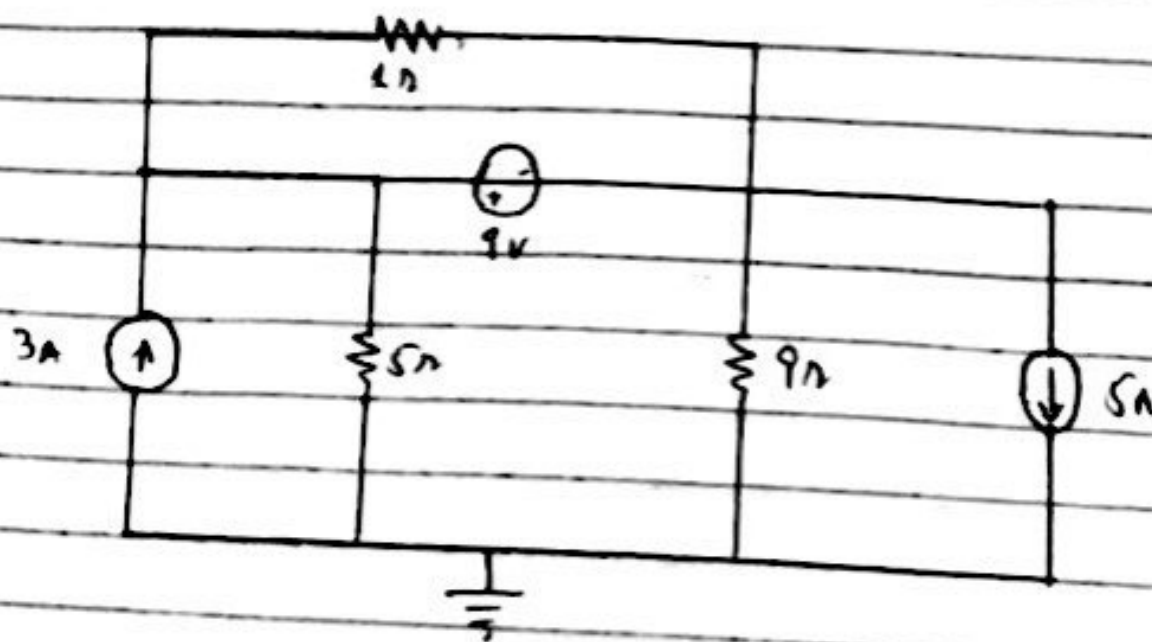
$$V_{SD} = 8.833V$$

Since the voltage across the  $7\Omega$  resistor is  $V_a$ . Therefore

$$\begin{aligned} P_{7\Omega} &= \frac{V_a^2}{7} \\ &= \frac{(8.633)^2}{7} \\ &= 74.528689 \end{aligned}$$

$$P_{7\Omega} = 10.646 \text{ W}$$

219) determine the numerical value for the voltage labeled  $V_1$



Soln:

Consider  $V_1$  and  $V_2$  as a super node

Apply KCL on super node.

$$V_1 - V_2 = \frac{V_1}{1} + \frac{V_2 - V_1}{1} + \frac{V_2}{9} = 3 - 5$$

$$45V_1 - 45V_2 + 9V_1 + 45V_2 - 45V_1 + 9V_2 = 3 - 5$$

$$9V_1 + 9V_2 = 135 \quad \text{--- (1)}$$

So

$$V_1 - V_2 = 9 \quad \text{--- (2)}$$

Combining eq (1) and (2)

$$9V_1 + 9V_2 = 135$$

$$9V_1 - 9V_2 = 81$$

$$18V_1 = 216$$

$$V_1 = \frac{216}{18}$$

$$V_1 = 12 \text{ V}$$

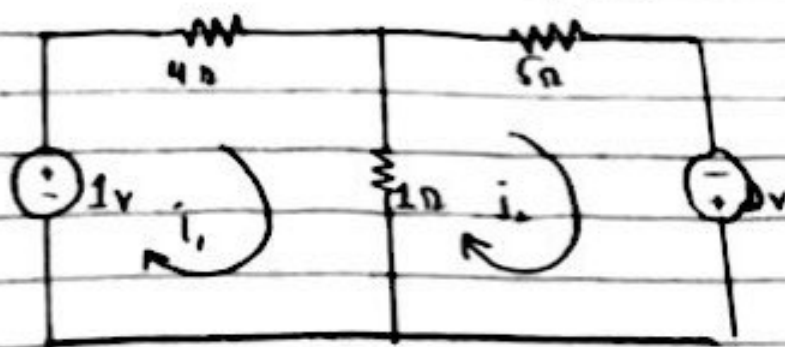
Put in eq - (2)

$$V_2 = V_1 - 9$$

$$V_2 = 12 - 9$$

$$V_2 = 3$$

Q29) Determine the current flowing out of the positive terminal of each voltage source in the circuit.



Solution:

Applying KCL on  $i_1$

$$4i_1 + 1(i_1 - i_2) = 1$$

$$5i_1 - i_2 = 1 \quad \text{--- (i)}$$

Applying KVL on  $i_2$

$$1(i_2 - i_1) + 5i_2 = 2$$

$$-i_1 + 6i_2 = 2 \quad \text{--- (ii)}$$

Multiply (ii) with eq (i)

So adding with eq (i)

$$5i_1 - i_2 = 1$$

$$-5i_1 + 30i_2 = 10$$

$$\hline 29i_2 = 11$$

$$i_2 = \frac{11}{29}$$



$$i_2 = 0.379$$

Putting in eq ①

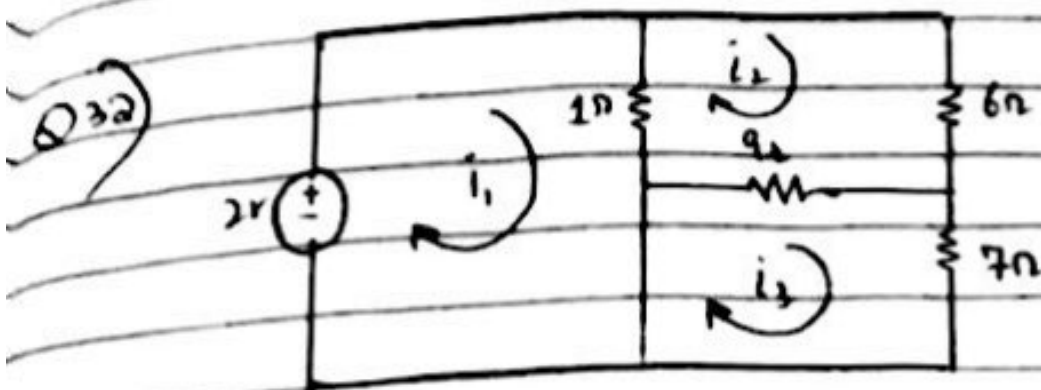
$$5i_1 = 1 + 0.379$$

$$i_1 = 0.275 \text{ A}$$

Result

$$i_1 = 0.275 \text{ A}$$

$$i_2 = 0.379 \text{ A}$$



Soln.

write the equation.

$$-2 + 1(i_1 - i_2) - 3 + 5(i_1 - i_3) = 0$$

$$6i_1 - i_2 - 5i_3 = 5 \quad \text{--- ①}$$

write the 2<sup>nd</sup> eq.

$$1(i_2 - i_1) + 6i_2 + 9(i_2 - i_3) = 0$$

$$-i_1 + 16i_2 - 9i_3 = 0 \quad \text{--- ②}$$

write 3<sup>rd</sup> eq.

$$5(i_3 - i_1) + 3 + 9(i_3 - i_2) + 7i_3 = 0$$

$$-5i_1 - 9i_2 + 21i_3 = -3 \quad \text{--- ③}$$

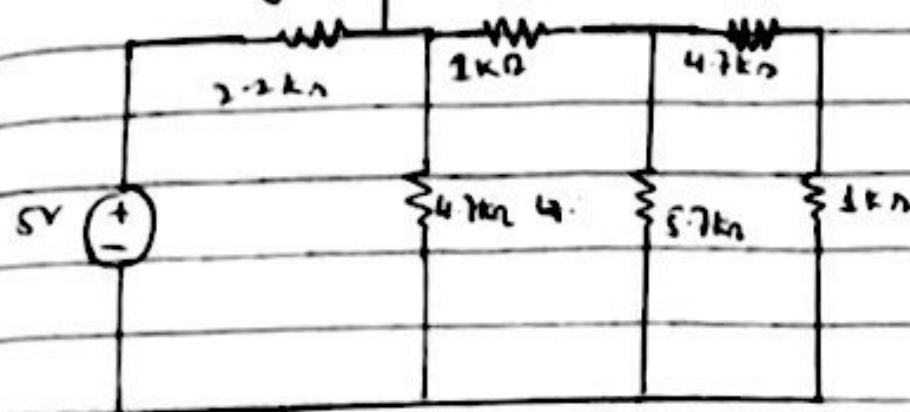
Solve the three eq (1), (2) and (3)

$$i_1 = 989.205 \text{ mA}$$

$$i_2 = 150.147 \text{ mA}$$

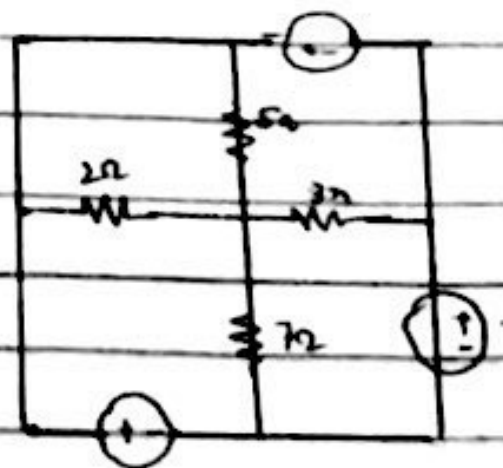
$$i_3 = 157.017 \text{ mA}$$

Q.25) Choose nonzero value of the three Voltages. Source of figure so that current flows through ~~any~~ any resistor in the circuit.



Soln-

Let name the sources  $V_1, V_2$  and  $V_3$  from top to bottom.



And the current  $i_1, i_2, i_3$  and  $i_4$

form the currents in resistors to be equal to zero.

$$i_1 - i_2 = 0$$

$$i_2 - i_4 = 0$$

$$i_1 - i_3 = 0$$

$$i_2 = i_4 = 0$$

② Now we will apply KVL on each of the four loops

$$2 \cdot (i_1 - i_3) + 5 (i_1 - i_2) = 0$$

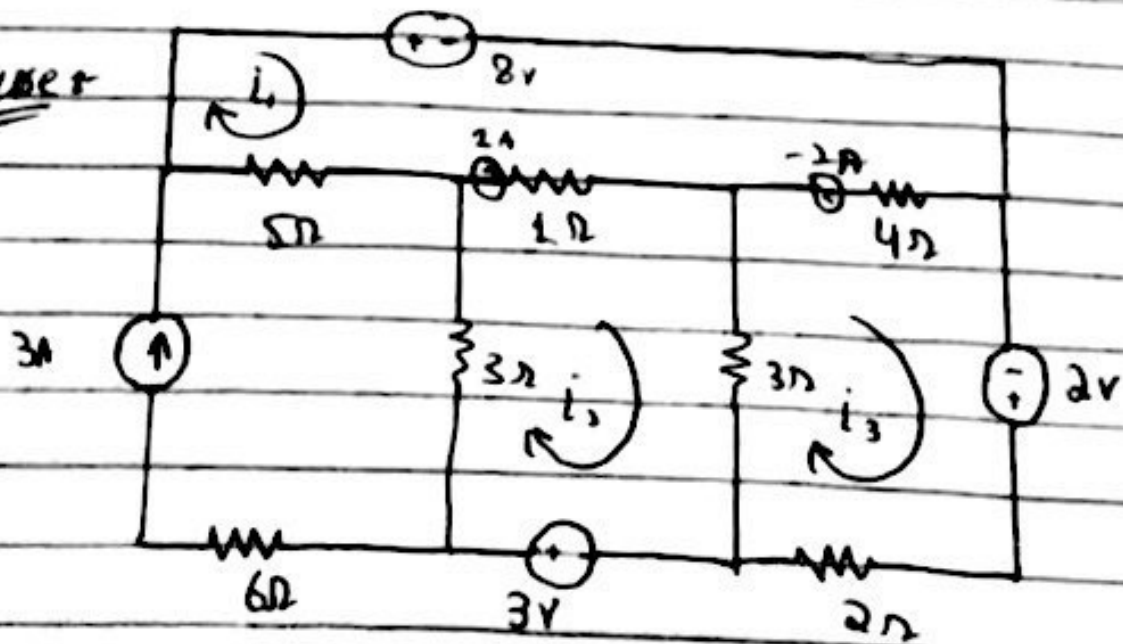
$$3 \cdot (i_1 - i_4) + 5 (i_2 - i_1) = -V_1$$

$$7 \cdot (i_2 - i_4) + 2 \cdot (i_2 - i_3) = V_1$$

$$3 \cdot (i_4 - i_2) + 7 \cdot (i_4 - i_3) = V_3$$

③  $V_1 = V_2 = V_3 = 0$

④ figure



Soln

$$i_4 = 3A$$

Mesh analysis  $i_1 - i_2 - i_3$  super node given us

$$8 + 5(i_1 - 3) + 3(i_2 - 3)$$

$$-3 + 2i_3 - 2 = 0$$

By apply KVL on the lower left Super node

and the upper right node we get

$$i_1 - i_2 - 1 = 0$$

$$2 + i_1 - i_2 = 0$$

After solving these three eq we get

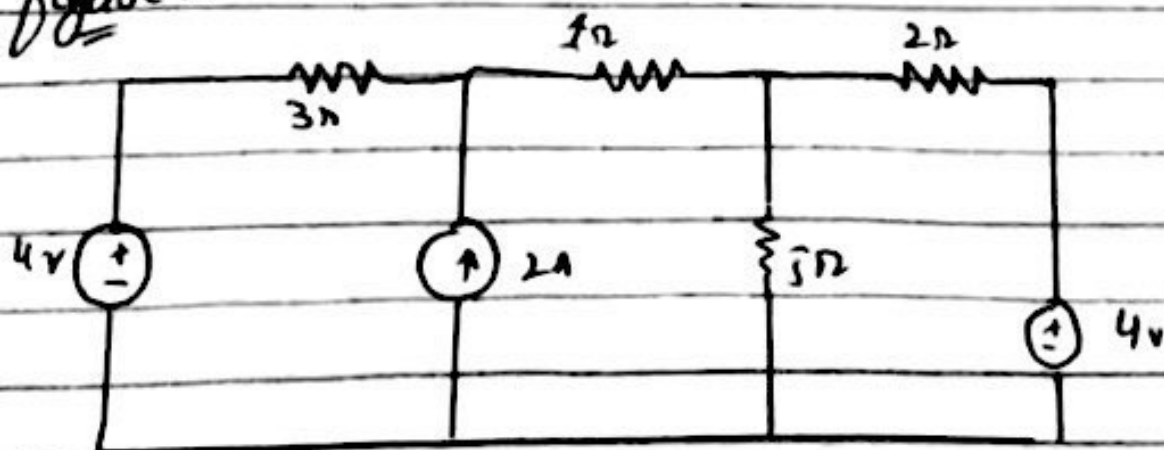
$$i_1 = 1.4 \text{ A}$$

$$i_2 = 2.4 \text{ A}$$

$$i_3 = 3.4 \text{ A}$$

## Question No (5)

(10) Figure:-



Solution

there are three sources.

$$V_x = V_1 + V_2 + V_3$$

where  $V_1$ ,  $V_2$  and  $V_3$  are the contribution due to the left 4V voltage source, 2A current source and the right 4V voltage source respectively.

Sources respectively,

To obtain  $v_1$  we set the 2A and the right 4V source to zero as shown below apply mesh analysis to the two meshes 1 and 2 we obtain the following matrix equation:

$$\begin{bmatrix} 3+1 & -1 \\ -1 & 5+2 \end{bmatrix} \begin{bmatrix} i_1 \\ i_2 \end{bmatrix} = \begin{bmatrix} 4 \\ 0 \end{bmatrix}$$

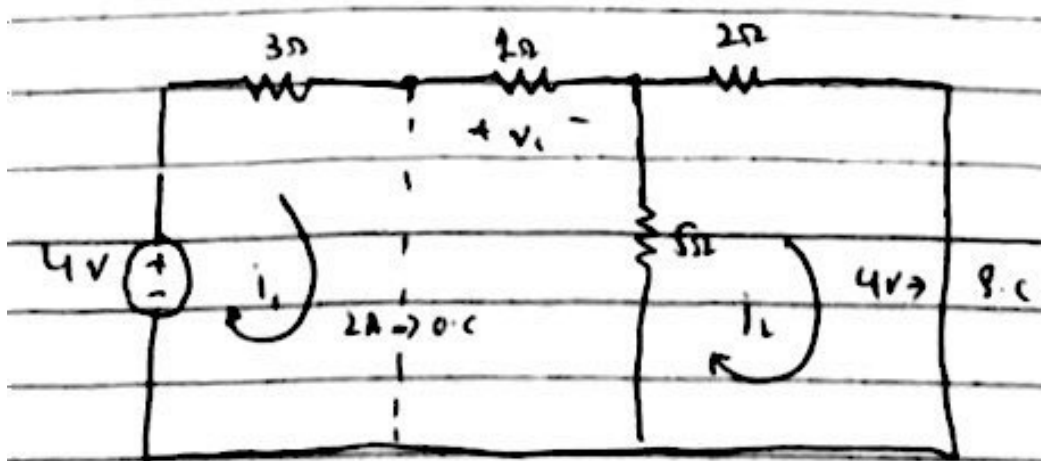
we find:

$$i_1 = \frac{14}{19} \text{ A}$$

For 1  $\Omega$  resistor, ohm's law given

$$V_1 = 1 \cdot i_1 = \frac{14}{19} \text{ V}$$

$$= 736.84 \text{ mV}$$



To obtain  $v_2$  we set the two 4V source to zero as shown below, Apply nodal analysis to the two nodes  $V_a$  and  $V_b$  we obtain the following matrix equation:

$$\begin{bmatrix} \frac{1}{3} + 1 & -1 \\ -1 & 1 + \frac{1}{3} + \frac{1}{2} \end{bmatrix} \begin{bmatrix} V_a \\ V_b \end{bmatrix} = \begin{bmatrix} 2 \\ 0 \end{bmatrix}$$

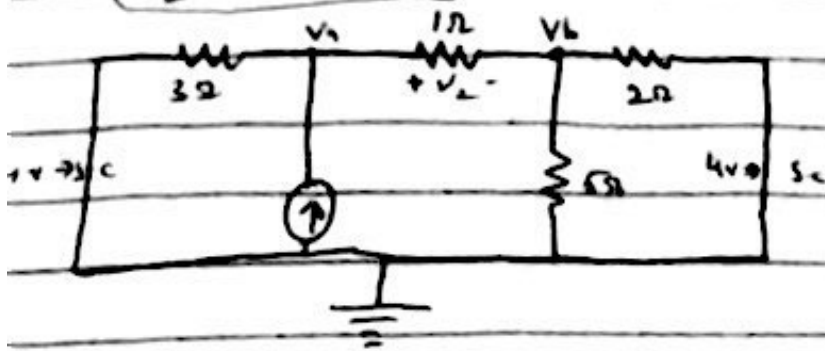
matrix of we find

$$V_a = \frac{51}{19} \text{ V} \quad \text{and} \quad V_b = \frac{30}{19} \text{ V}$$

By inspection, it is clear that:

$$V_2 = V_a - V_b = \frac{51}{19} - \frac{30}{19} = \frac{21}{19}$$

$$V_2 = 1.105 \text{ V}$$



To obtain  $V_3$  we set the 2A and left 4V source to zero as shown below

Apply mesh analysis to the two meshes 1 and 2 we obtain the following matrix equation:

$$\begin{bmatrix} 3+1+5 & -5 \\ -5 & 5+2 \end{bmatrix} \begin{bmatrix} i_1 \\ i_2 \end{bmatrix} = \begin{bmatrix} 0 \\ -4 \end{bmatrix}$$

the matrix eq we find:

$$i_1 = \frac{-10}{19} \text{ A}$$

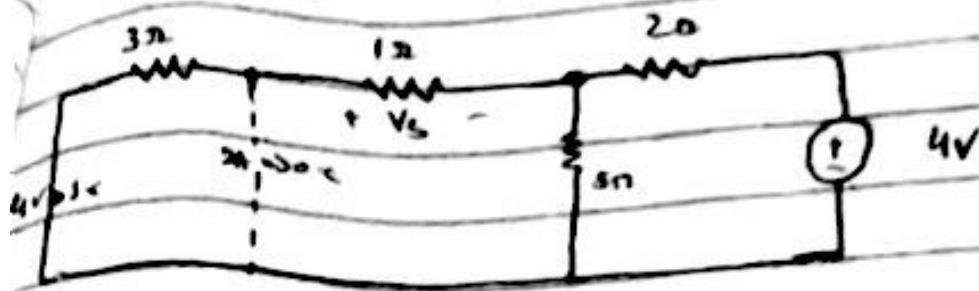
the 1Ω resistor, ohm's law gives:

$$V_3 = 1 \cdot i_1 = -\frac{10}{19} \text{ V}$$

$$V_3 = -526.32 \text{ mV}$$

therefore

$$V_x = V_1 + V_2 + V_3$$
$$V_x = 736.84 \text{ mV} + 1.105 \text{ V} - 526.32 \text{ mV}$$
$$V_x = 1.316 \text{ V}$$



It is required to evaluate the value of the current sources that result in reducing the  $V_x$  values by 10%. Let the new values of  $V_x$  is  $V'_x$  the current sources values affect only its contribution which is  $V_2$ , let the new value of  $V_2$  is  $V'_2$  thus

$$V'_x = 0.9V_x = 0.9 \cdot 1.316 \text{ V}$$
$$V'_x = 1.1844 \text{ V}$$

2nd

$$V'_2 = V'_x - (V_1 + V_3) = 1.1844 \text{ V} - (736.84 \text{ mV} - 526.32 \text{ mV})$$
$$= 973.88 \text{ mV}$$

Apply nodal analysis to the two nodes  $V_a$  and  $V_b$  in the circuit show below gives.

$$I_{cs} = \left(1 + \frac{1}{2}\right) V_a - V_b - \text{①}$$

$$0 = -V_a + \left(1 + \frac{1}{5} + \frac{1}{2}\right) V_b - \text{②}$$

We have:

$$V_a - V_b = V_x = 973.88 \text{ mV} - \text{③}$$

Solving the three eq. ①, ② and ③ we

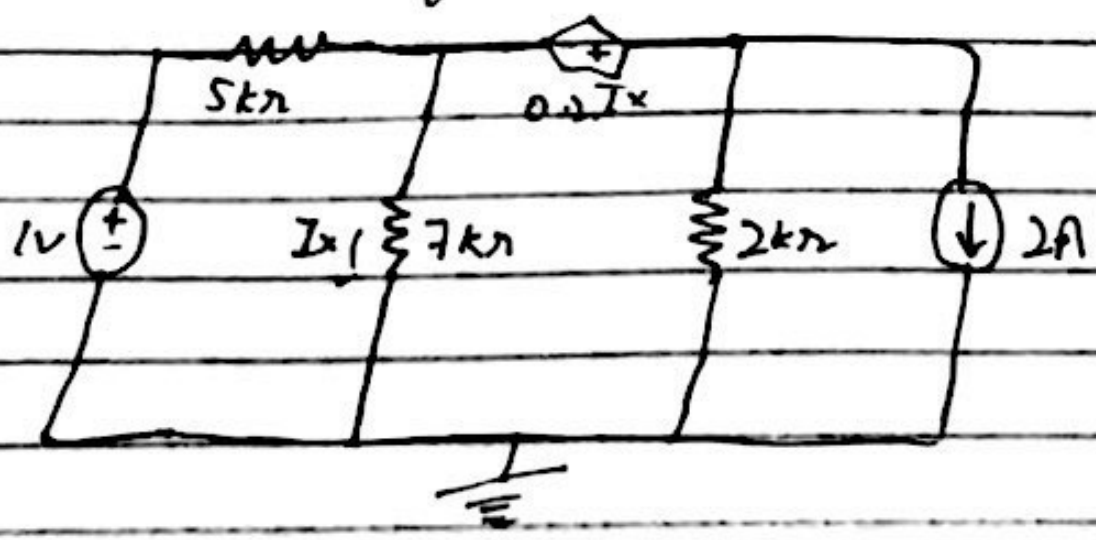
$$I_{cs} = 1.7623 \text{ A}$$

We verify our result in part (a) using pspice as shown below we obtain.

$$V_x = 6.053 - 4.737$$

$$V_x = 1.316 \text{ V}$$

11. u Employ Superposition principles to obtain a value from the current  $I_x$  labeled



Soln

Since there are two independent source let.



Where  $I_{x1}$  and  $I_{x2}$  are the contributions due to the  $1\text{V}$  voltage source and  $2\text{A}$  current source, respectively.

To obtain  $I_{x1}$ , we set the  $2\text{A}$  current source to zero (replacing it with an open circuit) as shown below.

Apply KCL to the supernode  $x$  and  $y$ .

$$\frac{V_1 - 1}{5000} + \frac{V_1}{7000} + \frac{V_2}{2000} = 0$$

But  $V_2 = V_1 + 0.2 I_{x1}$  hence.

$$\frac{V_1 - 1}{5000} + \frac{V_1}{7000} + \frac{V_1 + 0.2 I_{x1}}{2000} = 0$$

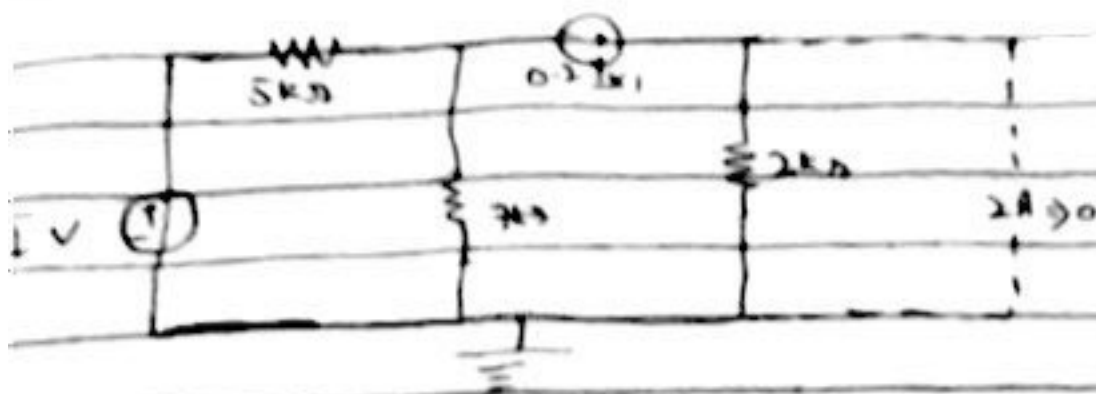
But  $V_1 = 7000 I_{x1}$ , hence.

$$\frac{7000 I_{x1} - 1}{5000} + \frac{7000 I_{x1}}{7000}$$

$$\frac{7000 I_{x1} + 0.2 I_{x1}}{2000} = 0$$

Then

$$I_{x1} = 33.9 \mu\text{A}$$



To obtain  $I_x$  we set the 1V voltage source to zero (replacing it with a short circuit) as shown below.

Apply KCL to the supernode  $\gamma$  given

$$\frac{V_1}{5000} + \frac{V_1}{7000} + \frac{V_2}{2000} = -2$$

But

$$V_1 = 7000 I_{x2} \quad ; \quad \text{then}$$

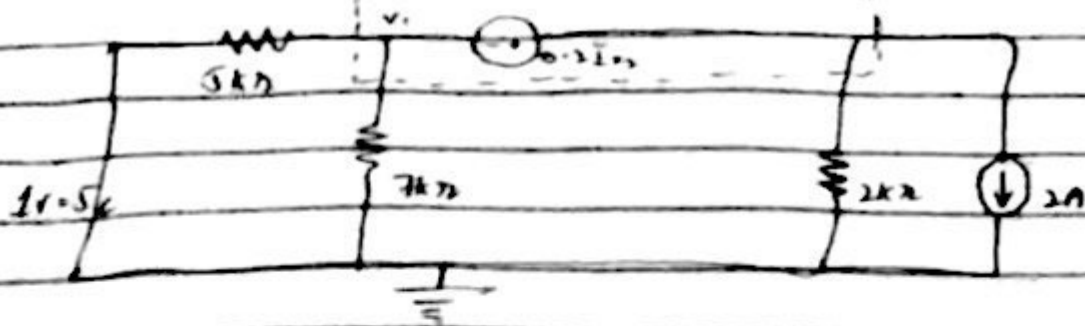
$$\frac{7000 I_{x2}}{5000} + \frac{7000 I_{x2}}{7000} + \frac{7000 I_{x2} + 0.2 I_{x2}}{2000} = -2$$

Thus

$$I_{x2} = -338.38 \text{ mA}$$

Therefore:  $I_x = I_{V_1} + I_{x2}$   
 $= 338.98 \text{ mA} + (-338.98 \text{ mA})$

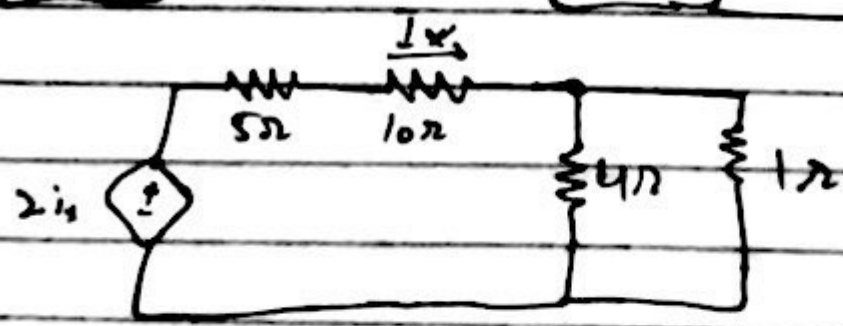
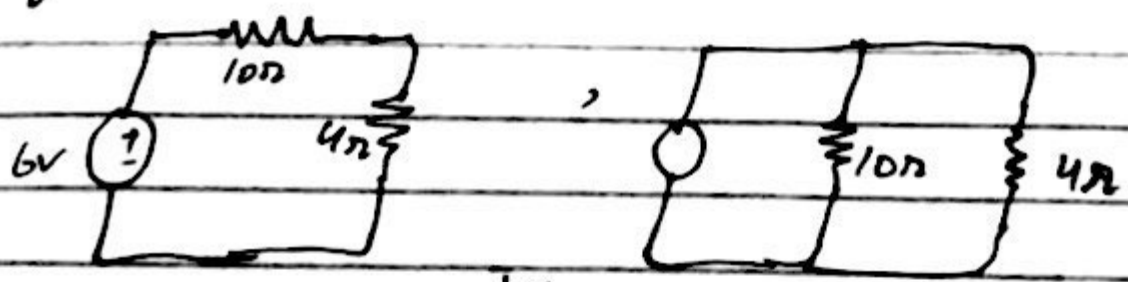
$$I_x = -338.98 \text{ mA}$$



Result

$$I_x = -338.95 \text{ mA}$$

3) Perform and appropriate source transformation on each of the circuit depicted in 5.58 taking care to retain the 4r resistor in each final circuit.

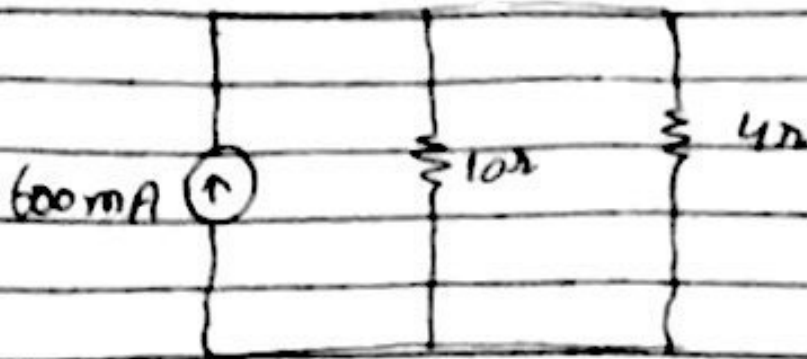


Soln The value of the new source we get  
 $I = \frac{V}{R}$

$$I = \frac{6}{10}$$

$$I = 0.6 \text{ A}$$

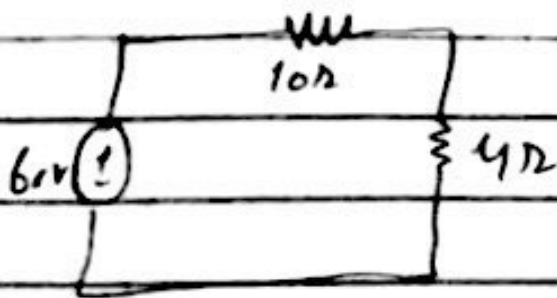
And we can draw the circuit as



The new voltage source will have the value of

$$V = 10 \cdot 6$$
$$\boxed{V = 60V}$$

And we draw it as

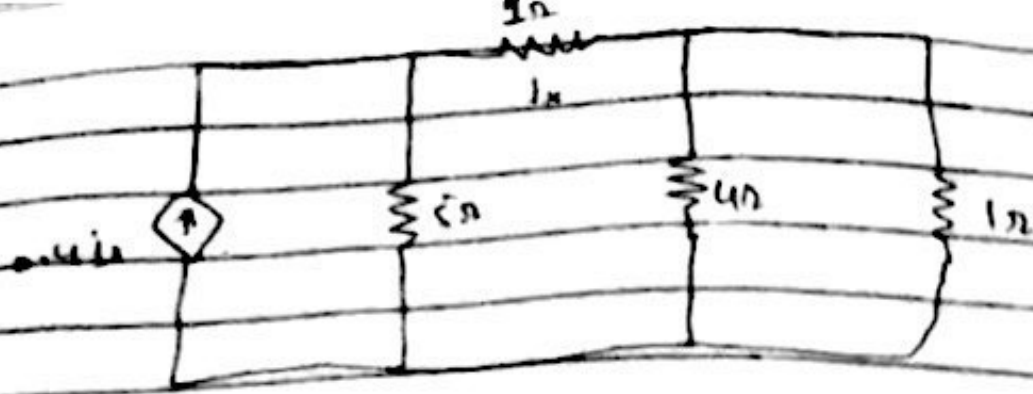


To get the value of the new current source we use

$$I = \frac{V}{R}$$

$$I = \frac{60}{4}$$

And we draw it as



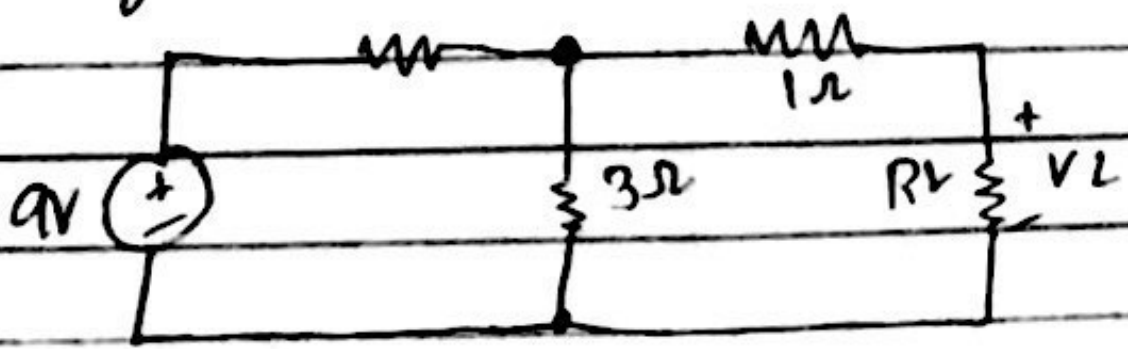
Result

(a) we replace the  $10\Omega$  resistor and the voltage source with a  $600\text{ mA}$  current source in parallel with a  $10\Omega$  resistor.

(b) we replace  $10\Omega$  resistor and the current source with a  $60\text{ V}$  voltage source in series with a  $10\Omega$  resistor.

(c) we replace the  $5\Omega$  resistor and dependent voltage source with a dependent current source labeled  $0.4i_x$  in parallel with a  $5\Omega$  resistor.

Q5:- Determine the thevenin equivalent of the network connected to  $R_L$  (b) determine  $V_L$  for  $R_L = 1\Omega, 3.5\Omega, 6.25\Omega$  and  $9\Omega$ .



Solution:-

To get  $V_{TH}$  we disconnect  $R_L$  and find the voltage between the two disconnected point. As we can see this voltage is the one on the  $3\Omega$  resistor.

$$V_{TH} = 9V \cdot \frac{3}{5}$$

$$V_{TH} = 5.4V$$

We can calculate  $R_{TH}$  as:

$$R_{TH} = 1+3\parallel 2$$

$$R_{TH} = 2.2\Omega$$

Then we calculate  $V_L$  as:

$$V_L = V_{TH} \cdot \frac{R_L}{R_L + R_{TH}}$$

for the each value of  $R_L$  we get:

$$R_L = 1\Omega \Rightarrow V_L = 1.688V$$

$$R_L = 3.5\Omega \Rightarrow V_L = 3.316V$$

$$R_L = 6.25\Omega \Rightarrow V_L = 3.995V$$

$$R_L = 9.8\Omega \Rightarrow V_L = 4.41V$$

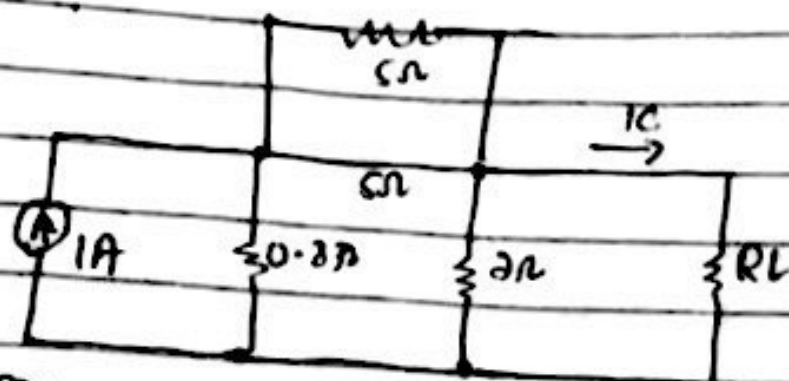
Result :-

$$V_{TH} = 5.4V, R_{TH} = 2.2\Omega$$

$$V_L = 1.688V, 3.316V, 3.995V, 4.41V$$

27:

- (a) obtain the norton equivalent of the network connected to  $R_L$
- (b) obtain the evenin equivalent of the same network.
- (c) use either to calculate  $i_o$  for  $R_L = 0\Omega, 1\Omega, 4.923\Omega$  and  $8.107\Omega$ .



Solution:-

(a) we calculate  $R_N$  as:

$$R_N = (0.8 + 5) \parallel 2$$

$$R_N = 3.3 \parallel 2$$

$$R_N = 1.245\Omega$$

for  $i_N$  we have:

$$i_N = \frac{0.8}{0.8 + 2.5}$$

$$i_N = 0.242A$$

(b) now we can  $V_{th}$  as

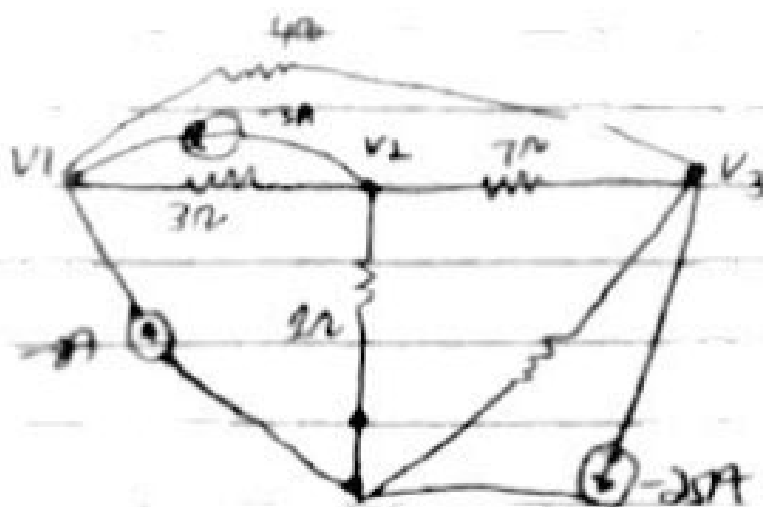
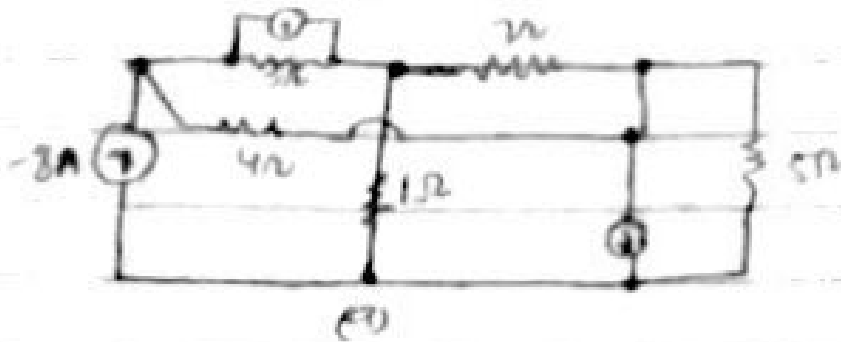
$$V_{th} = i_N \cdot R_N$$

$$R_N \times i_N = 1.245\Omega \times 0.242A$$

$$\Rightarrow 0.301V \text{ ANSWER}$$

### Example 4.2

Determine the nodal voltages for the circuit of 4.4a, as reference to the bottom node



Reference node (b)

### Solution:

We have three nodes in the circuit  $v_1$ ,  $v_2$  and  $v_3$ .

Applying KCL on node 1

$$-3 - \frac{v_2 - v_1}{3} + \frac{v_2 - v_3}{4}$$

Try LCM



$$-11 = 4V_1 + 4V_2 + 3V_3 - 3V_2$$

$$-11 = \frac{7V_1}{12} - \frac{4V_2}{12} - \frac{V_3}{12}$$

$$-11 = 0.5833V_1 - 0.3333V_2 - 0.0833V_3$$

Applying KCL At node 2

$$3 = \frac{V_1 - V_2}{3} + \frac{V_2 - V_3}{7}$$

$$3 = \frac{7V_1 - 7V_2 + 3V_2 - 3V_3}{21}$$

$$3 = \frac{7V_1}{21} + \frac{3V_2}{21} - \frac{3V_3}{21}$$

$$3 = 0.3333V_1 + 0.1429V_2 - 0.1429V_3$$

Applying KCL At node 3

$$25 = \frac{V_3}{15} + \frac{V_2 - V_3}{7} + \frac{V_3 - V_1}{4}$$

Taking LCM

$$25 = \frac{28V_2 + 20V_3 - 28V_3 + 35V_3 - 35V_1}{140}$$

$$25 = \frac{-35V_1}{140} - \frac{8V_2}{140} + \frac{83V_3}{140}$$

$$25 = 0.25V_1 - 0.0571V_2 + 0.5929V_3$$

simplifying further by grammer rule

$$\begin{bmatrix} 0.5833 & -0.3333 & -0.2500 \\ -0.3333 & 1.4762 & -0.1429 \\ 0.2500 & -0.1429 & 0.5929 \end{bmatrix} \begin{bmatrix} v_1 \\ v_2 \\ v_3 \end{bmatrix}$$

let det of A =  $\Delta x$

$$\Delta x \begin{bmatrix} 0.5833 & 0.3333 & -0.2500 \\ -0.3333 & 1.4762 & -0.1429 \\ 0.2500 & -0.1429 & 0.5929 \end{bmatrix}$$

$$\Delta x = 0.5833 \begin{bmatrix} 1.4762 & -0.1429 \\ 0.1429 & 0.5929 \end{bmatrix}$$

$$- (0.3333) \begin{bmatrix} -0.3333 & -0.1429 \\ 0.2500 & 0.5929 \end{bmatrix} - 0.2500$$

$$\Delta x = 0.5833 (0.875 - 0.020)$$

$$0.3333 (0.1976 - 0.00357) - 0.2500 (0.0476 - 0.3690)$$

$$\Delta x = 0.498600 - 0.0777 + 0.079$$

Now

$$v_1 = \frac{1}{\Delta x} \begin{bmatrix} -1 & -0.33 & -0.250 \\ -3 & 1.476 & -0.142 \\ 25 & -0.142 & 0.592 \end{bmatrix}$$

$$= -1 \begin{bmatrix} 1.476 & -0.142 \\ 0.142 & 0.592 \end{bmatrix} - 3 \begin{bmatrix} 0.33 & 0.250 \\ -0.142 & 0.392 \end{bmatrix}$$

$$25 \begin{bmatrix} 0.33 & -0.250 \\ 1.476 & -0.142 \end{bmatrix}$$

$$= 11 \begin{bmatrix} 1.479 & -0.142 \\ 0.142 & 0.59 \end{bmatrix}$$

$$= 11(0.275 - 0.010) - 3(0.197 - 0.035) + 25(0.047 + 0.36)$$

$$V_1 = 1.714 = 5.412V$$

$$0.3167$$

$$V = \frac{1}{\Delta x} \begin{bmatrix} 0.523 & -11 & -0.250 \\ -0.333 & 3 & -0.142 \\ -0.250 & 25 & 0.592 \end{bmatrix}$$

$$= 0.523 \begin{bmatrix} 3 & -0.142 \\ 25 & 0.592 \end{bmatrix} + 11 \begin{bmatrix} 0.333 & -0.142 \\ -0.250 & 0.592 \end{bmatrix}$$

$$= 0.250 \begin{bmatrix} 0.333 & 3 \\ 0.250 & 25 \end{bmatrix}$$

$$= 0.53(1.778 + 3.572) + 11(0.2197 + 0.035)$$

$$= -0.25(8.332 + 0.7)$$

$$= 2.45$$

so

$$V_1 = \frac{24}{0.3161} = 77.3V$$

Now

$$V_2 = \frac{1}{\Delta X} \begin{bmatrix} 0.5833 & -0.333 & -11 \\ 0.33 & 1.476 & 3 \\ 0.250 & -0.142 & 25 \end{bmatrix}$$

$$0.483 \begin{bmatrix} 0.333 & 11 \\ 0.333 & 476 & 3 \end{bmatrix} 0.33 \begin{bmatrix} 0.33 & 3 \\ 0.25 & 25 \end{bmatrix}$$

$$-11 \begin{bmatrix} 0.333 & 1.476 \\ 0.250 & -0.142 \end{bmatrix}$$

$$= 0.583(15.238) + 0.333(9.0825) - 11(0.107) = 14.67$$

$$\text{so } V_3 = \frac{14.67}{0.316} = 46.32V$$

so

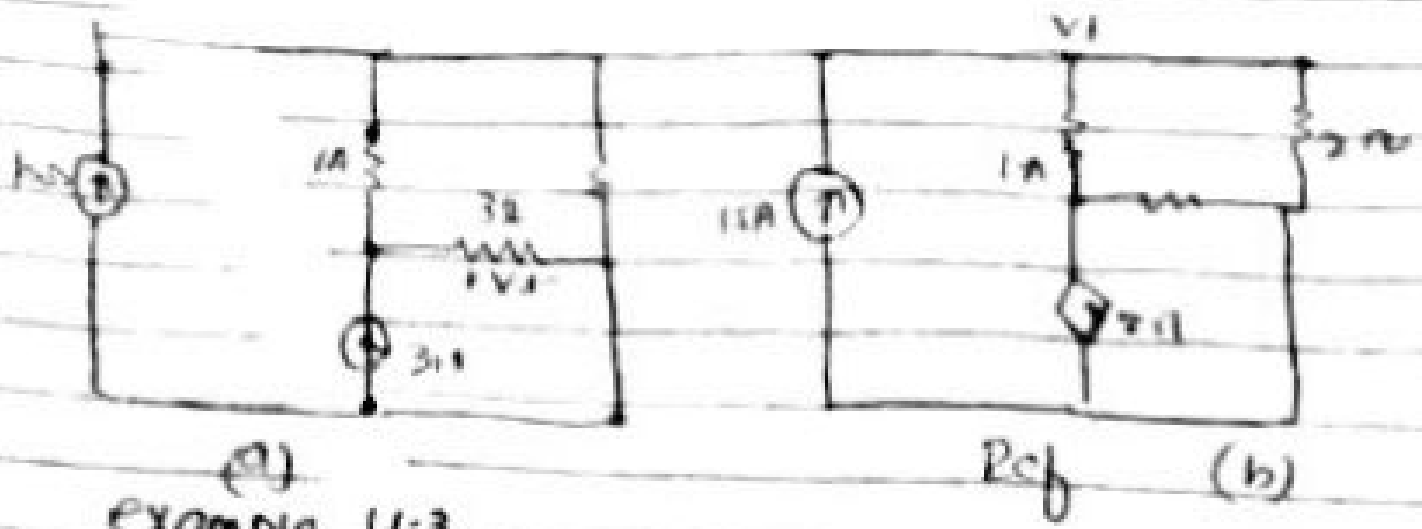
$$V_1 = 5.412V$$

$$V_2 = 77.3V$$

$$V_3 = 46.32V$$

Example 4.3

Determine the power supplied by the dependant source of figure.



(a)  
 Example 4-3  
 Solution

Applying KCL - on  $v_2$   
 $15 = v_1 - v_2 = v_1/2$

$$15 = \frac{2v_1 - 2v_2 + 15}{2}$$

$$30 = 2v_1 - 2v_2 \quad (1)$$

Applying KCL on  $v_1$

$$3i_1 = v_2 - v_1 + v_3/3$$

$$3i_1 = 3v_2 - 3v_1 + 15 = - \quad (2)$$

$i_1$  is flowing across

$$v_1/30 \quad \text{or} \quad v_1/2$$

$$\therefore i_1 = v_1/2$$

Put eq (2)

$$3V_1 = 3V_2 - 3V_1 + 2V_2$$

$$6V_1 = 6V_2 - 6V_1 + 4V_2$$

$$8V_2 + 15V_1 = 6$$

$$-15V_1 + 8V_2 = 0 \quad \text{--- (3)}$$

Bring (5) with eq (2) by  
subtraction from eq (3)

$$15V_1 - 7V_2 = 0$$

$$-15V_1 + 10V_2 = 30$$

$$3V_2 = -30$$

$$V_2 = -10$$

Bring 5 with eq (1)

$$\text{or } 3V_1 = 2V_2 - 30$$

$$\Rightarrow 15V_1 - 10V_2 = 150$$

Combining eq (1) and eq (3)

$$15V_1 - 10V_2 = 150$$

$$-15V_1 + 18V_2 = 0$$

$$-2V_2 = 150$$

$$v_2 = 75$$

putting in eq 3

$$15v_1 + 8(-75) = 0$$

$$v_1 = 40$$

Now

$$i_2 = \frac{v_1}{2} = \frac{40}{2} = 20A$$

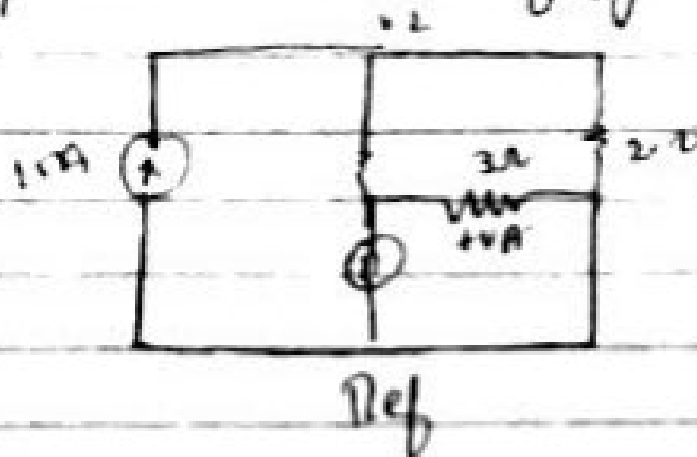
your power,  $P = iv$

$$P = (3i_2)(v_2) = 3(20)(75)$$

$$P = 4.5 \text{ kW}$$

Example 4.4

Determine the power supplied by the dependent source of figure.



Applying KCL on the  $v_2$ .

$$15 = v_1 - v_2 + \frac{v_1}{2}$$

$$30 - v_1 - v_2 + \frac{v_2}{2}$$

$$30 - 2v_1 - 2v_2 + v_2$$

$$30 = 3v_1 - 2v_2 \quad \dots \quad (1)$$

Applying KCL at  $v_2$

$$3v_2 = v_1 + v_2 + \frac{v_2}{3}$$

$$v_2 = \frac{v_1}{3}$$

$$\frac{2v_2}{3} = 3v_1 - \frac{3v_1 + v_2}{3}$$

$$-3v_1 + v_2 = 0 \quad \dots \quad (2)$$

combine eq(1) and (2)

$$3v_1 - 2v_2 = 30$$

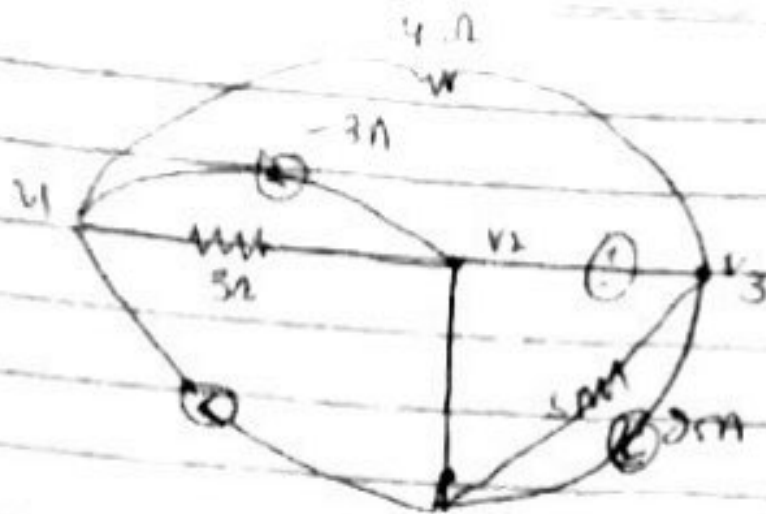
$$-3v_1 + v_2 = 0$$

$$v_2 = 30$$

Example 4.5:

Determine the value of unknown node voltage in the circuit of figure.





Solution

Reference node

Applying KCL on  $v_1$

$$-8 - 3 = \frac{v_1 - v_2}{3} + \frac{v_1 - v_2}{4}$$

$$-11 = \frac{4v_1 + v_2 + 3v_1 - 3v_2}{12}$$

$$(-11)(12) = 7v_1 - 4v_2 - 3v_3$$

$$-(132) = 7v_1 - 4v_2 - 3v_3 \quad (1)$$

Applying KCL on node  $v_2$

$v_2$  and  $v_3$

$$3 + 2 = \frac{v_2 - v_1}{3} + \frac{v_3 - v_2}{4} + \frac{v_3 - v_2}{5}$$

$$28 = \frac{20v_2 + 20v_3 + 15v_3 + 10v_2}{60}$$

$$(28)(60) = -35v_1 + 100v_2 + 27v_3$$

$$1680 = -35v_1 + 100v_2 + 27v_3 \quad (2)$$

Multiply eq (1)

$$3v_1 - 20v_2 - 15v_3 = -660 \quad (3)$$

combining eq 2 and 3

$$-3v_1 + 80v_2 + 27v_3 = 1680$$

$$3v_1 - 20v_2 - 15v_3 = -660$$

$$60v_2 + 12v_3 = 1020 \quad (4)$$

we know that from super node

$$v_1 + 2v_2 = v_3 \quad (5)$$

putting eq 5 in eq 4

$$60v_2 + v_2 + 2v_2 = 1020$$

$$61v_2 = 998$$

Dividing both side by 61

$$\frac{61v_2}{61} = \frac{998}{61}$$

$$v_2 = \frac{998}{61}$$

$$v_2 = 16.4$$

putting in eq (1)

$$16 + 4(16.4) = v_3$$

$$v_3 = 84$$

putting  $v_2$  and  $v_3$  in eq (1)

$$-132 = 7V_1 - 4(16.4) - 3(38.4)$$

$$-132 - 7V_1 = 65.6 - 115.2$$

$$-132 - 7V_1 = -180.8$$

$$180.8 - 132 = 7V_1$$

$$48.8 = 7V_1$$

Divided both side by 7

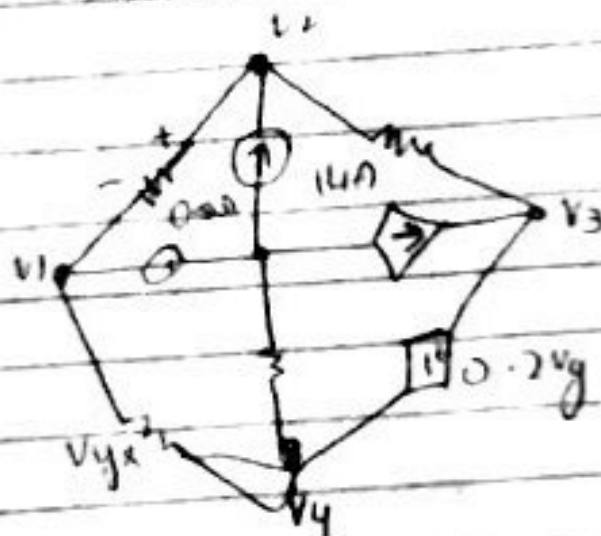
$$\frac{48.8}{7} = \frac{7V_1}{7}$$

$$48.8 = 7V_1$$

$$V_1 = 6.971$$

Example 4.6

Determine the node to reference voltage in the circuit.



Solution

$$\text{As } V_1 = -12V$$

Applying KCL on  $V_2$

$$V_2 \frac{1}{0.5} + V_2 \frac{1}{5} - V_3 = 14$$

$$2v_1 + 0.5v_2 = 0.5v_3 - 14$$

$$-1v_1 + 0.5v_2 = -0.5v_3 + 14 \quad \text{--- (1)}$$

Applying KCL on upper node  
i.e.  $v_3$  node

$$0.5v_1 = \frac{v_3 - v_2}{2} + \frac{v_3 - v_4}{2}$$

$$0.5v_1 = \frac{v_3 - v_2 + v_3 - v_4}{2}$$

We know that

$$0.5v_1 = 0.5(v_2 - v_1)$$

$$0.5v_1 = 0.5(v_2 - v_1)$$

$$0.5v_1 - 0.5v_1 = 0.5v_2 - 0.5v_1 - 4v_2 + 4v_4$$

$$0.5v_2 - 0.5v_1 = v_1 - 4v_2 + 4v_4$$

$$7.5v_1 - 7.5 + 2.5v_2 = 0 \quad \text{--- (2)}$$

put the values of equation

$v_1$  and  $v_3$  in eq (2)

we will get value of  $v_3$

$$-2v_1 + 2.5v_2 - 0.5v_3 = 14$$

$$[-12] + 2.5(-4) - 0.5v_3 = 14$$

$$12 - 10 - 0.5v_3 = 14$$

$$0.5v_3 = 12$$

$$v_3 = \frac{12}{0.5}$$

$$v_3 = 24$$

put in eq (9)

$$7.5(-12) - 7(-4) + 2.5 + 2v_4 = 0$$

$$2v_4 - 2 = 0$$

$$v_4 = 1$$

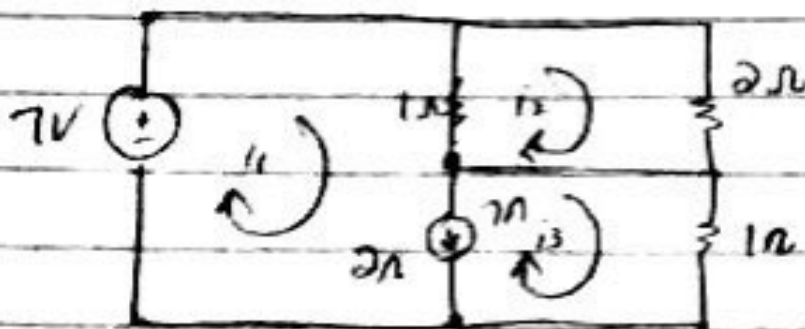
$$v_4 = 1$$

Result

$$v_1 = -12, v_2 = -4, v_3 = 24, v_4 = 1$$

Example 4.11

Determine the three mesh current



Solution

we know that there is independent sources b/w node 2 and node 3 which this a super node

Apply KVL on super mesh

$$1(i_1 - i_2) + 3(i_3 - i_2) + 2i_3 = 7$$

$$i_1 - i_2 + 3i_3 - 3i_2 + 2i_3 = 7$$

$$i_1 - 4i_2 + 5i_3 = 7 \quad \text{--- } \textcircled{1}$$

Applying KVL on mesh 2

$$(u \ i) \begin{pmatrix} 12 & 13 \\ 12 & 13 \end{pmatrix} = 0$$

$$-12 + 6i2 + 13 = 0 \quad (3)$$

Apply KVL on a node on which independent source is entering.

$$2 + 13 - i2$$

$$= 13 - i2$$

Apply cramer's rule

$$\begin{bmatrix} 1 & -4 & 4 \\ -1 & 6 & -3 \\ 1 & 6 & -1 \end{bmatrix} \begin{bmatrix} i_1 \\ i_2 \\ i_3 \end{bmatrix} = \begin{bmatrix} 1 \\ 0 \\ 7 \end{bmatrix}$$

$$|A| = \begin{vmatrix} 1 & -4 & 4 \\ -1 & 6 & -3 \\ 1 & 6 & -1 \end{vmatrix}$$

$$= 1(6 + 4(6+3))(-4)$$

$$= -6 + 16 - 24$$

$$|A| = -14$$

$$|A \ x| = \begin{vmatrix} 7 & -4 & 4 \\ 0 & 6 & -3 \\ 7 & 6 & -1 \end{vmatrix}$$

$$= 7(-6) + 7(12 \ 24)$$

$$= -42 + 7(-12)$$

$$= -42 - 84$$

$$\boxed{|Ax| = -126}$$

$$Bx = \begin{vmatrix} 1 & 7 & 4 \\ -1 & 0 & -3 \\ 0 & 7 & -1 \end{vmatrix}$$

$$= 1 \begin{vmatrix} 0 & -3 \\ 7 & -1 \end{vmatrix} - 1 \begin{vmatrix} 7 & 4 \\ 7 & -1 \end{vmatrix} + 0$$

$$= 1(21) - 1(-7 - 28)$$

$$= 21 + 35$$

$$\boxed{|Bx| = 56}$$

$$Cx = \begin{vmatrix} 1 & -4 & 7 \\ -1 & 6 & 0 \\ 0 & 0 & 7 \end{vmatrix}$$

$$= 1 \begin{vmatrix} 6 & 0 \\ 0 & 7 \end{vmatrix} + 1 \begin{vmatrix} -4 & 7 \\ 0 & 7 \end{vmatrix} + 0$$

$$= 1(42) + 1(28)$$

$$= 42 + 28$$

$$\boxed{|CX| = 70}$$

$$|CX| = \begin{vmatrix} 1 & -4 & 7 \\ -1 & 6 & 0 \\ 1 & 0 & 7 \end{vmatrix}$$

$$= 1 \begin{vmatrix} 6 & 0 \\ 0 & 7 \end{vmatrix} + 4 \begin{vmatrix} -1 & 0 \\ 1 & 7 \end{vmatrix} + 7 \begin{vmatrix} -1 & 6 \\ 1 & 0 \end{vmatrix}$$

$$= 1(42) + 4(-7) + 7(-6)$$

$$= 42 - 28 - 42$$

$$= -28$$

now

$$i_1 |AY| = \frac{-26}{-14} = 9A$$

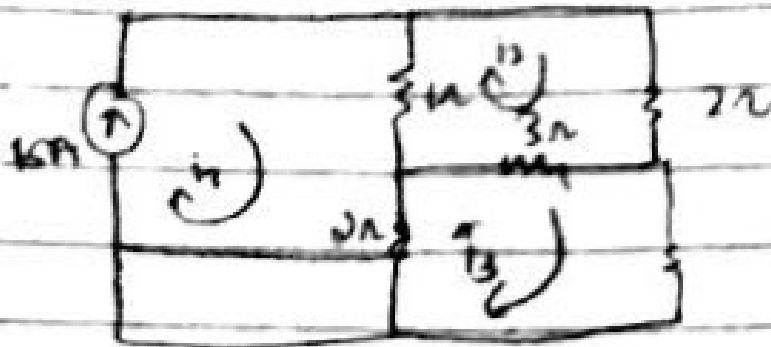
$$i_2 = \frac{|2X|}{|A|} = \frac{-56}{-14} = 2.5A$$

$$i_3 = \frac{|CX|}{|A|} = \frac{-28}{-14} = 2A$$



### Example 4-12

Evaluate the three known currents in the circuit.



Solution

We have one dependent current and one independent source

Now we have the  $6A$

We have to find two unknown source

Apply KCL on a node

Unsource is entering

$$i_1 + \frac{1}{9} 6A = i_3$$

$$\frac{v_x}{9} = i_3 - i_1$$

$v_x = 3(i_3 - i_1)$  from figure  
putting in equation

$$\frac{3}{9}(i_3 - i_1) = i_3 - i_1$$

$$\frac{1}{3} i_3 - \frac{1}{3} i_2 - i_3 - i_3$$

$$-i_3 - i_3 - \frac{1}{3} i_2 + i_3 - i_2$$

$$-i_3 + i_3 + \frac{1}{3} i_2 - \frac{1}{3} i_2$$

$$-i_3 + \frac{1}{3} i_2 + \frac{2}{3} i_3 = 0$$

$$i_2 = 15$$

$$-15 + \frac{1}{3} i_2 + \frac{2}{3} i_3 = 0$$

$$\frac{1}{3} i_2 + \frac{2}{3} i_3 = 15 \quad \text{--- (A)}$$

$$i_2 + 2i_3 = 45 \quad \text{--- (1)}$$

Apply KVL on mesh 2-

$$1(i_1 - i_2) + 2i_2 + 3(i_2 - i_3) = 0$$

$$i_2 - i_1 + 2i_1 + 3i_2 - 3i_3 = 0$$

$$-i_2 + 6i_2 - 3i_3 = 0$$

$$\boxed{i_1 = 15}$$

$$-15 + 6i_2 - 3i_3 = 0$$

$$6i_2 - 3i_3 = 15 \quad \text{--- (1)}$$

combining eq (1) and (2)

$$\begin{array}{r} 6i_2 + 12i_3 = 270 \\ -6i_2 - 3i_3 = -15 \\ \hline 9i_3 = 285 \end{array}$$

$$\Rightarrow i_3 = \frac{285}{9}$$

$$\Rightarrow 28.33 \text{ A and}$$

$$\Rightarrow i_2 = 11 \text{ A}$$

$$v_3 - v_1 + 2v_3 = -8$$

10

$$-v_1 + 3v_3 = -80 \quad (3)$$

Taking eq (1)

$$4v_1 = 100$$

$$v_1 = 25 \quad (a)$$

Taking eq (2)

$$v_3 + 3v_3 = -80$$

$$v_3 = \frac{-80}{4} = -20 \quad (b)$$

putting eq (a) and (b) and eq (3)

$$-30(0.57v_1 + 14.28) + 3v_2 - 3(0.33v_2 - 28.07) = 480$$

$$-17.1v_2 - 428.4 + 3v_2 - 0.99v_2 + 84.21 = 480$$

$$34.91v_2 = 822.39$$

$$v_2 = 20.31$$

putting in eq (a)

$$v_2 = 4(20.31) + (100) = 181.24$$

$$i_x = \frac{v_1 - v_2}{2} = \frac{25 - 181.24}{2}$$

$$i_x = -77.12 \text{ A}$$

Solving the mesh analysis



Applying KVL on loop 1

$$8i_1 + 4(i_1 - i_2) = 100$$

$$8i_1 + 4i_1 - 4i_2 = 100$$

$$13i_1 - 4i_2 = 100 \quad \text{--- (1)}$$

Applying KVL on loop 2

$$2i_2 + 4(i_2 - i_1) + 3(i_3 - i_2) = 0$$

$$2i_2 + 4i_2 - 4i_1 + 3i_3 - 3i_2 = 0$$

$$-4i_1 + 9i_2 - 3i_3 = 0 \quad \text{--- (2)}$$

Applying KVL on loop 3

$$3(i_3 - i_2) + 10(i_3 - i_4) + 5i_3 = 0$$

$$3i_3 - 3i_2 + 10i_3 - 10i_4 + 5i_3 = 0$$
$$i_4 = 8$$

$$-3i_2 + 18i_3 = 80 \quad (3)$$

Taking eq (1)

$$i_1 = \frac{4i_2 - 100}{12} \quad (4)$$

taking eq (2)

$$-3i_2 + 18i_3 = 80$$

$$i_3 = \frac{-3i_2 + 80}{18} \quad (5)$$

Putting eq 4 by b in eq (2)

$$-4(0.33i_2 - 8.33) + 9i_2 - 3(0.16i_2 + 4.44) = 0$$

$$-1 = 3.3i_2 + 33.32 + 9i_2 - 0.48i_2 - 13.32 = 0$$

$$7.8i_2 = -20 \quad \Rightarrow \quad \frac{-20}{7.8}$$

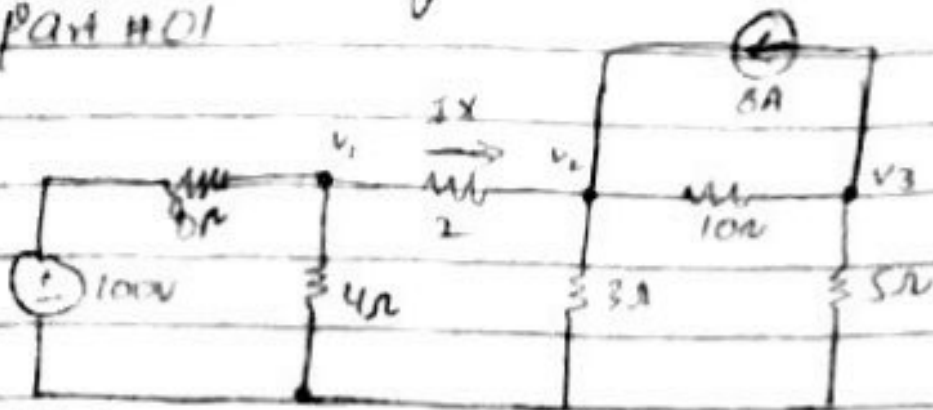
$$i_2 = -2.79 \text{ A}$$

$$i_2 = i_x$$

$$\boxed{i_x = -2.77 \text{ A}}$$

### Q3 - Node analysis

part 401



Solution -

Apply KCL on node 1 :-

$$\frac{v_1 - 100}{8} + \frac{v_1}{4} + \frac{v_1 - v_2}{2} = 0$$

$$v_1 - 100 + 2v_1 + 4v_1 - 4v_2 = 0$$

$$7v_1 - 4v_2 = 100 \quad \text{--- (1)}$$

Apply KCL on node 2 -

$$\frac{v_2 - v_1}{2} + \frac{v_3}{3} + \frac{v_2 - v_3}{10} = 8$$

$$50v_2 - 30v_1 + 20v_2 + 3v_2 - 3v_3 = 80$$

$$-30v_1 + 58v_2 - 3v_3 = 480 \quad \text{--- (2)}$$

Apply KCL on node 3

$$\frac{v_3 - v_2}{10} + \frac{v_3}{5} = -8$$

$$-2v_2 + 2v_3 = -80$$

10

$$-V_1 + 3V_3 = -80 \quad \text{--- (3)}$$

Taking eq (1)

$$7V_1 - 4V_2 = 100$$

$$V_1 = \frac{4V_2 + 100}{7} \quad \text{--- (a)}$$

Taking eq (2)

$$-V_2 + 3V_3 = -80$$

$$V_3 = \frac{V_2 - 80}{3} \quad \text{--- (b)}$$

Putting eq (a) and (b) in eq (3)

$$-30 \left( \frac{0.57V_2 + 14.28}{3} \right) + 53V_2 - 3 \left( \frac{0.33V_2 - 26.67}{3} \right) = 4$$

$$-17.1V_2 - 428.4 + 53V_2 - 0.99V_2 + 200.01 = 420$$

$$34.91V_2 = 828.39$$

$$V_2 = \frac{828.39}{34.91}$$

$$V_2 = 20.31$$

Putting in eq (a)

$$V_1 = \frac{4(20.31) + 100}{7}$$

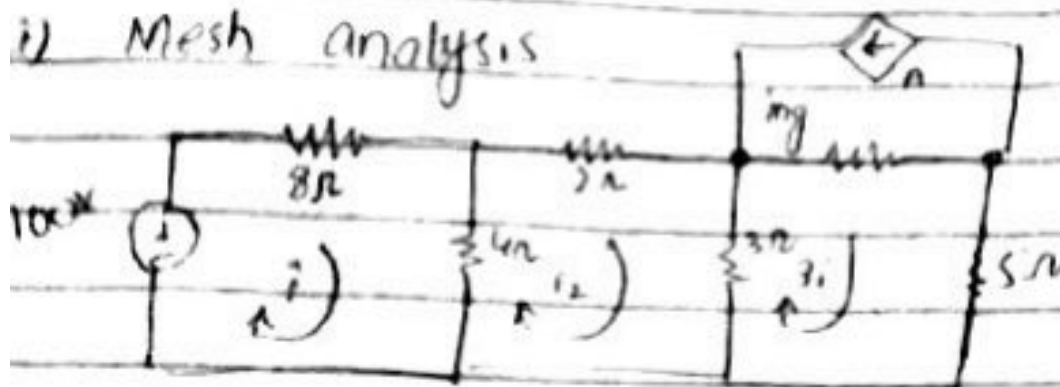
$$V_1 = 25.89$$

$$i_x = \frac{V_1 - V_2}{2} = \frac{25.89 - 20.31}{2}$$



$$r = 279A$$

i) Mesh analysis



Applying KVL on loop 1

$$8i_1 + 4(i_1 - i_2) = 100$$

$$8i_1 + 4i_1 - 4i_2 = 100$$

$$12i_1 - 4i_2 = 100 \quad \text{--- (1)}$$

Applying KVL on loop 2

$$2i_2 + 4(i_2 - i_1) + 3(i_3 - i_2) = 0$$

$$2i_2 + 4i_2 - 4i_1 + 3i_3 - 3i_2 = 0$$

$$-4i_1 + 9i_2 - 3i_3 = 0 \quad \text{--- (2)}$$

Applying KVL on loop 3

$$3(i_3 - i_2) + 10(i_3 - i_4) + 5i_3 = 0$$

$$3i_3 - 3i_2 + 10i_3 - 10i_4 + 5i_3 = 0$$

$$3i_2 + 19i_3 = +80 \quad \text{--- (3)}$$

taking eq (1)

$$i_2 = 4i_3 - 100 \quad \text{--- (4)}$$

taking eq (1) and (2)

$$-3i_2 + 19i_3 = -80$$

$$i_3 = \frac{-3i_2 + 80}{18} \quad \text{--- (5)}$$

Putting eq (4) and (5) on eq (2)

$$-1 \cdot 3i_2 + 33 \cdot 3i_2 + 9i_2 - 0 \cdot 0 \cdot 48i_2 - 13 \cdot 3i_2 = 0$$

$$i_2 = 20/72$$

$$i_1 = 2.79A$$

$$i_2 = A$$

$$i_3 = 2.79A$$