

**Ways to prevent the disease COVID-19**

1. Wash Your Hands For 20sec.
2. Cover Nose & Mouth When Sneezing.
3. Use hand sanitizer if soap and water are not available.
4. Avoid Crowded Places (Social Distancing)
5. Avoid Contact With Sick People
6. Stay At home
7. Don't visit outside unnecessarily

**Subject: Advanced Design of Reinforced concrete structures**

**Instructor:** Engr. Fawad Ahmad

**Total Marks:** 30

**Note:**

1. Attempt all questions. **R** is your class id.
2. ACI tables and values used in design must be referred while solving your design problem.
3. Use correct class Id R.

**Q.NO (01) (10)**

<b>A</b>	<p>Determine the values of <math>E_t</math>, <math>\phi</math> and <math>\phi M_n</math> for the sections shown below:</p> <div style="display: flex; justify-content: space-around; align-items: flex-start;"> <div style="text-align: center;"> <p>3 #11 bars 14 in. width 21 in. height 18 in. effective depth 3 in. clear cover <math>f_y = 75,000 \text{ psi}</math> <math>f'_c = 5,000 \text{ psi}</math></p> </div> <div style="text-align: center;"> <p>4 #10 bars 18 in. width 15 in. height 12 in. effective depth 3 in. clear cover <math>f_y = 60,000 \text{ psi}</math> <math>f'_c = 4,000 \text{ psi}</math></p> </div> </div> <p style="color: red; font-weight: bold;">Also discuss the strength analysis. Does the reinforcement is done according to design standard or not. Defend your design analysis.</p>	5
<b>B</b>	<p>Design a doubly reinforced beam for <math>M_D =</math> <b>[First three Digits of R]</b> ft-K and <math>M_L = 410</math> ft-K, if <math>f_c' = 4000</math> psi and <math>f_y = 6000</math>psi. Appropriate diagram is must in design.  <span style="color: red; font-weight: bold;">Assume the maximum permissible beam dimensions other than done in notes or Text book.</span></p>	5

**Q.NO (02) (10)**

<b>A</b>	<p>Design a short square column for the following conditions: <math>P_u =</math> <b>[First three Digits of R]</b> k, <math>M_u =</math> <b>[First two Digits of R]</b> ft-k, <math>f_c' = 4000</math> psi, and <math>f_y = 60,000</math> psi. Place the bars uniformly around all four faces of the column. Appropriate diagram is must in design.</p>	10
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**Q.NO (03) (10)**

<b>A</b>	<p>Design a square column footing for a 16 inch square tied interior column that supports a dead load <math>P_D =</math> <b>[First three Digits of R]</b>K and live load of <math>P_L = 160</math>K. The column is reinforced with #8 bars the base of the footing is 5feet below, the soil weight is 100 lf/ft<sup>3</sup>, <math>f_y = 60,00</math> psi and <math>f_c' = 3000</math>psi and <math>q_a =</math> <b>[First four Digits of R]</b>psf. Development length for main bars is also to be done in footing design. Appropriate diagram is must in design.</p>	10
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\*\*\*\*\* Best of Luck- Stay Safe\*\*\*\*\*

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ID :- 15629

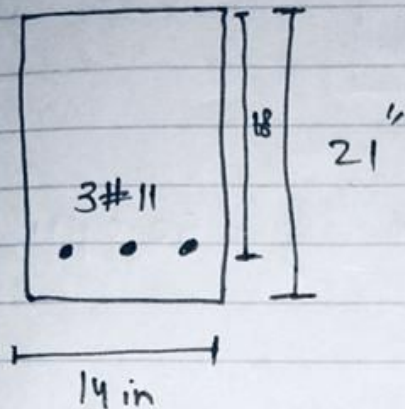
Subject :- Advanced Design of Reinforced  
concrete structure -

Instructor :- Engr. Fawad Ahmed -

IQRA National University  
Peshawar -



Q#(1)  
Determine the value of  $E_t$ ,  $\phi$  and  $\phi M_n$  for the Section -



Given data:

$$f_y = 75,000 \text{ psi}$$

$$f_c' = 5,000 \text{ psi}$$

$$A_s = 4.88 \text{ (table A-4)}$$

SOL

We know that

$$E_t = \frac{d-c}{c} (0.003)$$

$$c = \frac{a}{B_1}$$

for this we have to find  $a$  and  $B_1$ ,

$$a = \frac{A_s f_y}{0.85 f_c b}$$

$$a = \frac{(4.68)(75)^2}{0.85 \times 5 \times 14}$$

$$a = 5.899 \text{ in}$$

$$B_1 = 0.80 \text{ for } f_c' = 5000 \text{ psi}$$

Now

$$c = \frac{a}{B_1}$$

$$c = \frac{5.899}{0.80}$$

$$c = 7.37 \text{ in}$$

$$\epsilon_t = \left( \frac{d-c}{c} \right) (0.003)$$

$$\epsilon_t = \left( \frac{18 - 7.37}{7.37} \right) (0.003)$$

$$\epsilon_t = 0.00432$$

$0.0042 < \epsilon_t < 0.005$   
transition zone-



$$\phi = 0.65 \left( \epsilon_t - 0.002 \right) \frac{250}{3}$$

$$\phi = 0.65 (0.00432 - 0.002) \left( \frac{250}{3} \right)$$

$$\phi = 0.836$$

$$\phi M_n = ?$$

$$\rho = \frac{A_s}{bd} = \frac{4.68}{14 \times 18} = 0.01857$$

$$\rho_{max} = 0.0028$$

$$\rho_{min} = 0.0194 \quad / \text{OK}$$

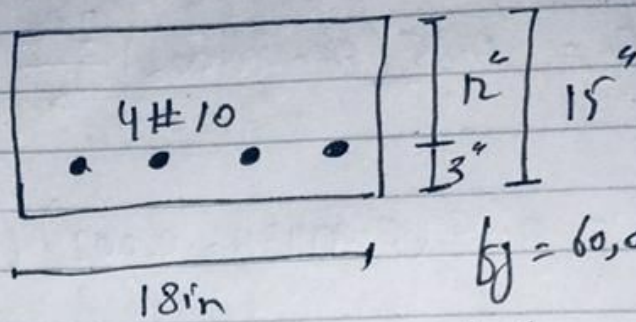
$$M_n = A_s f_y \left( d - \frac{a}{2} \right) = 4.68 \times 75 \left( 18 - \frac{5.89}{2} \right)$$

$$M_n = 5282.72 \text{ in-k}$$

$$M_n = 440.2 \text{ ft-k}$$

$$\phi M_n = 0.836 \times 440.2$$

$$\phi M_n = 368.028$$



$$f_y = 60,000 \text{ psi}$$

$$f_c' = 4000 \text{ psi}$$

find

$$\epsilon_t = ?$$

$$\phi = ?$$

$$\phi M_n = ?$$

Sol 2

$$A_s = 5.06 \text{ (table)}$$

$$\epsilon_t = \left( \frac{d - c}{c} \right) (0.003)$$

$$c = \frac{q}{B_1}$$

$$q = \frac{A_s f_y}{0.85 f_c' b}$$

$$q = \frac{5.06 \times 60}{0.85 \times 4 \times 18}$$



5

$$g = 4.96 \text{ in}$$

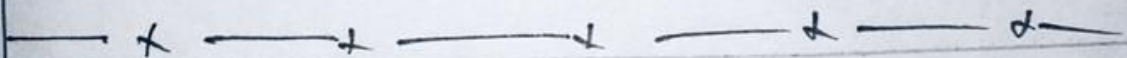
$$B_1 = 0.85$$

$$C = \frac{g}{B_1} = \frac{4.96 \text{ in}}{0.85} = 5.835$$

$$\epsilon_t = \left( \frac{12 - 5.835}{5.835} \right) (0.003)$$

$$\epsilon_t = 0.003 < 0.004.$$

Section is Not ductile and  
can not be used As per ACI  
Code -

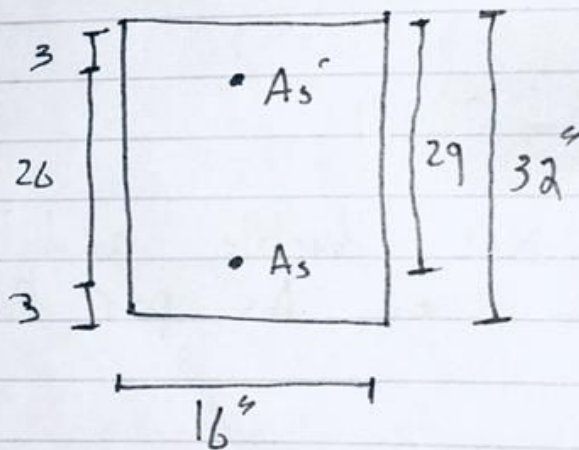


Q#(1) part(B)

Design a doubly reinforced beam  
 for  $M_D = 156 \text{ ft-k}$  and  $M_L = 418 \text{ ft-k}$   
 $f_c = 4000 \text{ psi}$  and  $f_y = 60,000 \text{ psi}$

Sol:

Assuming the Maximum dimension  
 for the beam is -



③ factored load:-

$$M_u = 1.2 M_D + 1.6 M_L$$

$$M_u = 1.2(156) + 1.6(418)$$

$$M_u = 843.6 \text{ ft-k}$$



② Nominal Moment ( $M_n$ )

$$M_n = \frac{M_u}{\phi}$$

$$M_n = \frac{843.2}{0.90}$$

$$M_n = 936.88$$

Now

$$A_s = \rho_{max} b d$$

$$\because \rho_{max} = 0.018$$

(table A-7)

$$A_s = 0.018 \times 16 \times 29$$

$$A_s = 8.352 \text{ in}^2$$

by

$$\rho_{max} = 0.0181 \quad \frac{M_u}{\phi b d^2} = 912 \quad (\text{table} = \text{A-13})$$

$$M_{u1} = 912 \times \phi b d^2$$

$$M_{u1} = 912 \times 0.90 \times 16 (29)^2$$

$$M_{u1} = 920.3 \text{ ft-k.}$$

$$M_{n1} = \frac{M_{u1}}{\phi}$$

$$M_{n1} = \frac{920.3}{0.90}$$

$$M_{n1} = 1022.65 \text{ ft-k.}$$

$$M_{n2} = M_n - M_{n1}$$

$$M_{n2} = 936.8 - 1022.65$$

$$M_{n2} = -85.8$$

I am taking this value positive  
it because of MD = is less -

$$M_{n2} = 85.8 \text{ ft-k.}$$

As' Required.

$$A_s' = \frac{M_{n2}}{f_y (d - d')}$$

$$A_s' = \frac{85.8 \times 12}{60 (29 - 3)}$$



$0.66 \text{ in}^2$

by 3#5  $A_s' = 0.91 \text{ in}^2$

$A_s' f_c' = A_{s2} f_y$

$A_{s2} = \frac{A_s' f_c'}{f_y}$

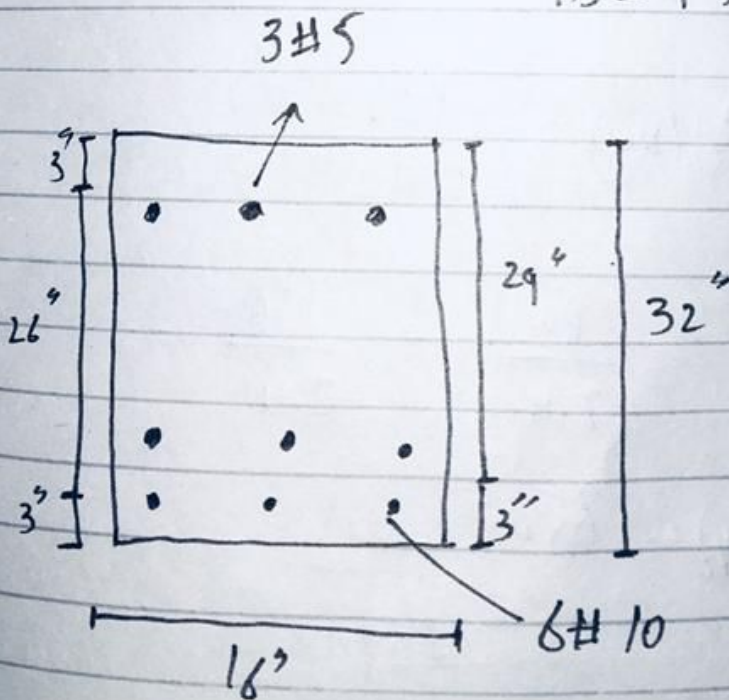
$A_{s2} = \frac{0.91 \times 60}{60} = 0.91 \text{ in}^2$

$A_s = A_s + A_{s2}$

$A_s = 8.35 + 0.91 \text{ in}$

$A_s = 7.515$

by 6#10  
 $A_s = 7.59$



Q#(2)

→ Design a short square column for the following condition -

$$P_u = 156 \text{ k}$$

$$M_u = 15 \text{ ft-k}$$

$$f_c' = 4000 \text{ psi}$$

$$f_y = 60,000 \text{ psi}$$

Place the bars uniformly around all four faces of the column -

Sol:-

Assuming the column will have compression stress about

$$0.6 f_c' = 2400 \text{ psi}$$

$$= 2.4 \text{ ksi}$$

Now

$$A_g(\text{Req}) = \frac{P_u}{2.4}$$

$$= \frac{156}{2.4} = \frac{156}{2.4}$$

$$A_g(\text{Req}) = 65 \text{ in}^2$$



So we try

9 x 9 in column -

$$A_g = 81 \text{ in}^2$$

$$e = \frac{M_u}{P_u} = \frac{15 \times 12}{156}$$

$$= 1.15 \text{ in}$$

$$P_n = \frac{P_u}{\phi} = \frac{156}{0.65}$$

$$P_n = 240 \text{ k}$$

$$k_n = \frac{P_n}{f_c' \times A_g}$$

$$= \frac{240}{4 \times 81}$$

$$k_n = 0.74$$

$$R_n = \frac{P_n \times e}{f_c' \times A_g \times h}$$

$$R_n = \frac{240 \times 1.15}{4 \times 81 \times 9}$$

$$R_n = 0.946$$

$$y = \frac{9 \cdot 2.5 - 2.5}{9}$$

$$y = \frac{4}{9}$$

$$y = 0.44 \text{ (not in the table)}$$

So let Assume the ( $y = 0.7$ )

Now by the intersection diagram take the  $\int$  value with the help of  $R_n$  and  $K_m$  value - which is

wh:

$$\int = 0.012 \text{ - table intersection from diagram}$$

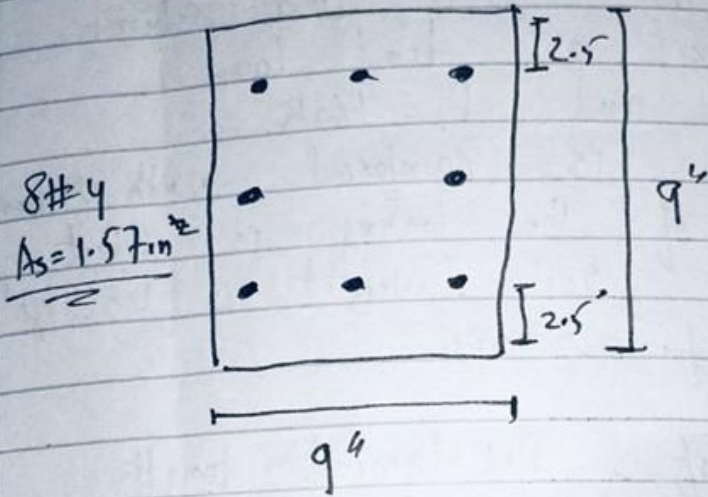
$$A_s = \int b h$$

$$A_s = 0.012 \times 9 \times 9$$

$$A_s = 0.972 \text{ in}^2$$



Use  $8\#4$   
 $A_s = 1.57 \text{ in}^2$



Q# (3)

→ Design a square column footing for a 16in square tied column that support a dead load

$$P_D = 156k \quad \text{and} \quad P_L = 160k$$

The column is reinforced with 8 bars the base of the footing is 5 feet below, the soil weight is  $100 \text{ lb/ft}^3$

$$f_y = 60,000, \quad f_c' = 3000 \text{ psi}$$

$q_a = 1562 \text{ psf}$  - Development length  
Appropriate diagram is must -

Sol<sup>n</sup>

Given data.

$$P_D = 156k$$

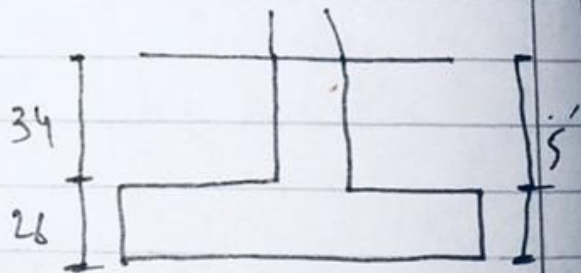
$$P_L = 160k$$

$$\gamma_s = 100 \text{ lb/ft}^3$$

$$f_y = 60,000 \text{ psi}$$

$$f_c' = 3000 \text{ psi}$$

$$q_a = \frac{156k}{100} \text{ psf}$$



Assumed data

$$\gamma_c = 150 \text{ lb/ft}^3$$

$$h_c = 26 \quad d = 22.5$$

$$h_s = 34$$



Sol:-

① effective Soil pressure -

$$q_e = q_a - h_c \times \gamma_c - H_s' \times \gamma_s$$

$$q_e = 1562 - \left( \frac{26}{12} \times 150 \right) - \left( \frac{34}{12} \times 100 \right)$$

$$q_e = 1562 - 325 - 283.3$$

$$q_e = 953.7$$

$$q_e = 0.953 \text{ ksf}.$$

② Area of footing -  $= \frac{P_D + P_L}{q_e}$ 

$$= \frac{156 + 160}{0.953}$$

$$= 331.34$$

use

$$\text{Area} = 324 \text{ } 18' \times 18' \text{ footing}$$

③ Ultimate bearing capacity -

$$q_u = \frac{1.2 P_D + 1.6 P_L}{\text{Area of footing}}$$

$$q_u = \frac{1.2(156) + 1.6(160)}{324}$$

$$q_u = 1.36 \text{ Ksf}$$

④ Depth required for two way or punching shear -

The depth required for two-way shear is the largest value obtained from the following -

$$\textcircled{1} \quad d = \frac{V_{u2}}{\phi 4 \sqrt{f_c'} b_o}$$

$$\alpha_s = 40$$

$$\textcircled{2} \quad d = \frac{V_{u2}}{\phi \left( \frac{\alpha_s d}{b_o} + 2 \right) \sqrt{f_c'} b_o}$$

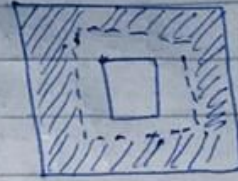
$b_o$  = perimeter around the punching area -



$$b_o = 4(a+d)$$

$$b_o = 4(16+22.5)$$

$$b_o = 154$$



$$16+22.5 = 38.5$$

$$V_{u2} [A - (a+d)] \leq V_u$$

$$V_{u2} = 324 - \left( \frac{16+22.5}{12} \right) \times 1.367$$

$$V_{u2} = (324 - 3.20) \times 1.367$$

$$V_{u2} = 438.53 \times 1000$$

$$V_{u2} = 438533$$

$$\textcircled{1} d = \frac{V_{u2}}{\phi \eta \sqrt{f_c} b_o}$$

$$= \frac{438533.6}{0.75(4) \sqrt{3000} \times 154}$$

$$= 17.33 < 22.5 \quad \text{OK}$$

$$\textcircled{2} \quad d = \frac{V_u^2}{\phi \left( \frac{\alpha_s d}{b_o} + 2 \right) \sqrt{f_c} b_o}$$

$$= \frac{438533.6}{0.75 \left( \frac{40 \times 22.5}{154} + 2 \right) \sqrt{3000} \times 154}$$

$$= \frac{438533.6}{0.75 (2.40) \sqrt{3000} \times 154}$$

$$= 12.75 > 22.5 \text{ /ok.}$$

\textcircled{5} depth required for one way shear -

$$V_{u1} = (18 \times 6.48) \times q_u$$

$$V_{u1} = 18 \times 6.48 \times 1.367$$

$$V_{u1} = 159.44$$

$$V_{u1} = 159.44 \times 6.816$$

$$\frac{l}{2} - \frac{a}{2} - d$$

$$\frac{18}{2} - \frac{1.3}{2} - 1.87$$

$$= 6.48$$



$$d = \frac{159446.8}{0.75 \times 2 \times \sqrt{3000} \times (18 \times 12)}$$

$$d = 8.98 < 22.5 \text{ /OK.}$$

Use height = 26"

Moment -

$$M_u = 8.335 \times 18 \times 1.36 \times \frac{8.335}{2}$$

$$M_u = 920.5$$

Now

$$\frac{M_u}{\phi b d^2} = \frac{920.5 \times 1000 \times 12}{0.90 \times (18 \times 12) (22.5)^2}$$

$$= 112.17$$

Now from table (A.12)

$$\rho = 0.0020$$

Use graph value ①  $\frac{200}{60,000} = 0.003$

②  $\frac{3\sqrt{3000}}{60,000} = 0.002$

So

$$\rho = 0.0033$$

Area of steel:-

$$A_s = \rho b d$$

$$A_s = 0.003 \times (18 + 12) \times 22.5$$

$$A_s = 16 \text{ in}^2$$

Use 8#14 (from table)

$$A_s = 18 \text{ in}^2$$

→ Development length.

$$\psi_t = \psi_e = \psi_s = \lambda = 1$$

$$\frac{d_b}{db} = \frac{3}{40} \frac{b_d}{b_c} \frac{\psi_t \psi_e \psi_s}{\psi_b} \quad \text{Ⓢ}$$

$\psi_t$  = Reinforcement location factor

$\psi_e$  = coating factor

$\psi_s$  = Reinforcement size factor

$\lambda$  = concrete modification factor -

$$\text{if } \frac{c_b}{d_b} > 2.5$$

then we use  
2.5



$$C_b = \text{Side cover} = 3.5$$

$$d_b = \text{dia of bar} = 1.69 \text{ (14 bar} = 1.69)$$

$$\frac{C_b}{d_b} = \frac{3.5}{1.69} = 2$$

So use 2  
using eq (1)

$$\frac{l_b}{d_b} = \frac{3}{40} \frac{60,000}{1 \sqrt{3000}} \times \frac{1+1+1}{2}$$

$$\frac{l_b}{d_b} = 31.875$$

$$\frac{l_b}{d_b} \times \frac{A_s(\text{Req})}{A_s(\text{select})}$$

$$= 31.87 \times \frac{16 \text{ m}^2}{18 \text{ m}^2}$$

$$= 28.32$$

$$l_d = 28.32 \times d_b$$

$$l_d = 28.32 \times 1.69$$

$$l_d = 47.87$$