

Name

M. Afnan

ID

2895

Section

"A"

Semister

4th

Dept

Civil engineering

Subject

Differential equations

Submitted

to

Mam Shomaila

Quiz

Ans :-

A yarn merchants 3 brands
A, B and C of yarn,
each of which is blend
Pakistan, Egyptian and American
cotton in ratio,

1 : 2 : 1 , 2 : 1 : 1 and
2 : 0 : 2 .

If cost/kg of A, B and C
is Rs 40, 50 and 60
respectively.

find the cost/kg of cotton
of each country

40	
P	E
A	E
A	

50	
P	P
A	E
B	

60	
P	P
A	A
C	

Let x , y and z be the
cost/kg of Pakistan, Egyptian
and American cotton respec-
tively. Then according to
the given condition

$$\left. \begin{aligned} \frac{1}{4}x + \frac{2}{4}y + \frac{1}{4}z &= 40 \\ \frac{2}{4}x + \frac{1}{4}y + \frac{1}{4}z &= 50 \\ \frac{2}{4}x + \frac{2}{4}z &= 60 \end{aligned} \right\} \rightarrow (5)$$

$$\left. \begin{aligned} 1x + 2y + 1z &= 160 \\ 2x + 1y + 1z &= 200 \\ 1x + 1z &= 120 \end{aligned} \right\} \rightarrow (5)$$

In matrix form we can write it as.

$$\begin{bmatrix} 1 & 2 & 1 \\ 2 & 1 & 1 \\ 1 & 0 & 1 \end{bmatrix} \begin{bmatrix} x \\ y \\ z \end{bmatrix} = \begin{bmatrix} 160 \\ 200 \\ 120 \end{bmatrix}$$

$$A = \begin{bmatrix} 1 & 2 & 1 \\ 2 & 1 & 1 \\ 1 & 0 & 1 \end{bmatrix}, \quad X = \begin{bmatrix} x \\ y \\ z \end{bmatrix}, \quad b = \begin{bmatrix} 160 \\ 200 \\ 120 \end{bmatrix}$$

$$AX = b$$

$$A = \begin{bmatrix} 1 & 2 & 1 \\ 2 & 1 & 1 \\ 1 & 0 & 1 \end{bmatrix}$$

$$A_1 = \begin{bmatrix} 160 & 2 & 1 \\ 200 & 1 & 1 \\ 120 & 0 & 1 \end{bmatrix}$$

$$A_2 = \begin{bmatrix} 1 & 160 & 1 \\ 2 & 200 & 1 \\ 1 & 120 & 1 \end{bmatrix}$$

$$A_3 = \begin{bmatrix} 1 & 2 & 160 \\ 2 & 1 & 200 \\ 1 & 0 & 120 \end{bmatrix}$$

$$|A| = -2 \quad \left| \begin{array}{l} |A_1| = \begin{vmatrix} 1 & 2 & 1 \\ 2 & 1 & 1 \\ 1 & 0 & 1 \end{vmatrix} = 1(1 \times 1 - 0 \times 1) - 2(2 \times 1 - 1 \times 1) \\ \quad \quad \quad + 1(2 \times 1 - 1 \times 1) \\ |A_2| = \begin{vmatrix} 160 & 2 & 1 \\ 200 & 1 & 1 \\ 120 & 0 & 1 \end{vmatrix} = 160(1 \times 1 - 0 \times 1) - 2(200 \times 1 \\ \quad \quad \quad - 120 \times 1) + (200 \times 1 - 120 \times 1) \\ |A_3| = \begin{vmatrix} 1 & 160 & 1 \\ 2 & 200 & 1 \\ 1 & 120 & 1 \end{vmatrix} = 1(200 \times 1 - 120 \times 1) - 160(2 \times 1 \\ \quad \quad \quad - 1 \times 1) + 1(2 \times 1 - 1 \times 200) \\ |A_4| = \begin{vmatrix} 1 & 2 & 160 \\ 2 & 1 & 200 \\ 1 & 0 & 120 \end{vmatrix} = 1(1 \times 120 - 0 \times 200) - 2 \\ \quad \quad \quad (2 \times 120 - 1 \times 200) + 160 \\ \quad \quad \quad (2 \times 120 - 1 \times 1) \end{array} \right.$$

$$|A| = -2$$

$$|A_1| = -120, |A_2| = -40, |A_3| = -120$$

According to Cramer's rule

$$x = \frac{|A_1|}{|A|} = \frac{-120}{-2} = 60$$

$$y = \frac{|A_2|}{|A|} = \frac{-40}{-2} = 20$$

$$z = \frac{|A_3|}{|A|} = \frac{-120}{-2} = 60$$

$$(x, y, z) = (60, 20, 60)$$