

(i)

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Subject:- Linear Algebra

Q1 :- 
$$\begin{bmatrix} 1 & 103 & 3 & 0 & 5 \\ 0 & 1 & -103 & 0 & 7 \\ 0 & 0 & 1 & 0 & -6 \\ 0 & 0 & 0 & 0 & 10 \end{bmatrix}$$

$$A = \begin{bmatrix} 1 & 0 & 3 & 0 & 5 \\ 0 & 1 & -3 & 0 & 7 \\ 0 & 0 & 1 & 0 & -6 \\ 0 & 0 & 0 & 1 & 0 \end{bmatrix}$$

The matrix is already in row  
reduced echelon form. As it  
satisfies all the rules.

HQAI

$$A = \begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 2 & -5 & -1 \end{bmatrix} \quad B = \begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 0 & 3 & -5 \end{bmatrix}$$

Elementary row operation that transform first matrix into second and reverse row operation that transform the second matrix into first.

$$\Rightarrow A = \begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 2 & -6 & -1 \end{bmatrix} \begin{array}{l} \rightarrow \text{row (i)} \\ \rightarrow \text{row (ii)} \\ \rightarrow \text{row (iii)} \end{array}$$

Multiply Row(2) with "2" and subtract it from row (3)

$$A = \begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 - (0 \times 2) & 2 - (1 \times 2) & -5 - (-4 \times 2) & -1 - (2 \times 2) \end{bmatrix}$$

$$A = \begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 0 & 3 & -5 \end{bmatrix}$$

$$A = \begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 0 & 3 & -5 \end{bmatrix}$$

Now  $A=B$  (the row operation used  $(2R_2 - R_3)$ )

1, D = 13835

Page (3)

Now let B (Reverse Row Operation)

$$B = \begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 0 & 3 & 5 \end{bmatrix} \begin{array}{l} \rightarrow \text{Row 1} \\ \rightarrow \text{Row 2} \\ \rightarrow \text{Row 3} \end{array}$$

multiply Row 2 with "2" and add it to Row 3

$$B = \begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0+(0 \times 2) & 0+(1 \times 2) & 3+(-4+2) & -5+4 \end{bmatrix}$$

$$B = \begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 2 & 3-8 & -5+4 \end{bmatrix}$$

$$B = \begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 2 & -5 & -1 \end{bmatrix}$$

So (B=A)

The row operation used was  $2R_2 + R_3$ .

consist of all zero, the leading "1" of the lower row is right to the leading row of the higher row.

(4)

Q3

(ii) 
$$\begin{bmatrix} 1 & 0 & \pi \\ 0 & 1 & e \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$
 is an echelon form

The matrix is in echelon form because it fulfil all the rules

- It have all the zeros row of bottom
- The leading one of the non-zero same row is right to the leading 1 of the upper row.

(iii) 
$$\begin{bmatrix} 5 & 0 & 0 & 7 \\ 0 & 1 & 0 & 5 \\ 0 & 0 & 1 & 4 \end{bmatrix}$$
 is an reduced echelon form

The matrix is an row reduced echelon form because it fulfil all the rules in reduced row echelon form. The row which consist of all zero entries should be at the bottom part. The matrix does not have the zero's row in the bottom therefore is not in the row reduced echelon form.

(1)

(5)

Q3(A) Reduce Row Echelon form

- A matrix is said to be in reduced row echelon form when it satisfies following condition.
- The matrix satisfies condition for row echelon form.
- The leading entry in each row is the only non-zero in its row.

For example,

$$\begin{bmatrix} 1 & 0 & 0 & 0 \\ 0 & 1 & 0 & 0 \\ 0 & 0 & 1 & 0 \\ 0 & 0 & 0 & 1 \end{bmatrix}$$

Q3(B) find an echelon form for the below matrix using row operation.

$$\begin{bmatrix} 1 & 5 & 2 \\ 2 & 8 & -1 \\ -7 & 0 & 0 \\ 1 & -4 & 14 \end{bmatrix} \quad R_3 + 7R_4$$

$$\begin{bmatrix} 1 & 5 & 2 \\ 2 & 8 & -1 \\ 0 & 0 & 0 \\ 1 & -4 & 14 \end{bmatrix} \quad R_3 \leftrightarrow R_4$$

Page (6)

$$\begin{bmatrix} 1 & 5 & 8 \\ 2 & 8 & -1 \\ 1 & -4 & 14 \\ 0 & 0 & 0 \end{bmatrix}$$

$R_2 - 2R_3$

$$\begin{bmatrix} 1 & 5 & 8 \\ 0 & 0 & -29 \\ 1 & -4 & 14 \\ 0 & 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 5 & 8 \\ 0 & 0 & -29 \\ 0 & -9 & 6 \\ 0 & 0 & 0 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 5 & 8 \\ 0 & -9 & 6 \\ 0 & 0 & -29 \\ 0 & 0 & 0 \end{bmatrix}$$

$\rightarrow$  Echelon form

3  
5  
2