

# "Assignment"

Course Title      Signal and System

Module              4th

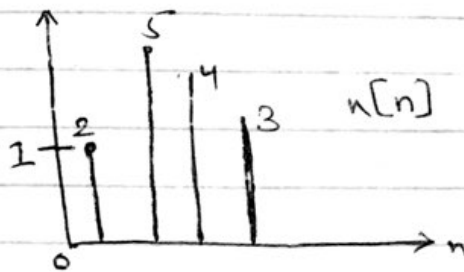
Instructor         Sir Mujtaba

Name                Farhan Ali

ID                    14873

Signature             
The signature is a stylized cursive script that reads "Farhan Ali". It features a large, sweeping initial 'F' and 'A'.

Q1:- Evaluate the even and odd components for the given function.

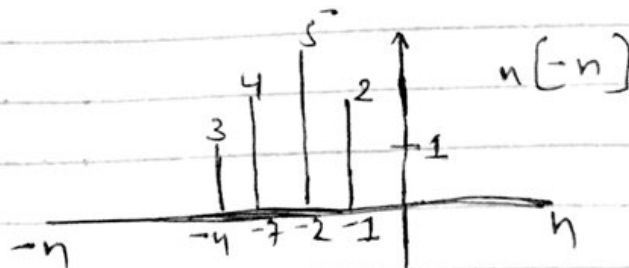


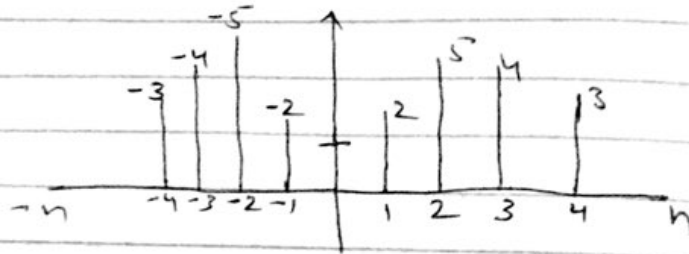
Sol:-

As we know that the even components of a function can be written as

$$x_e[n] = \frac{x[n] + x[-n]}{2}$$

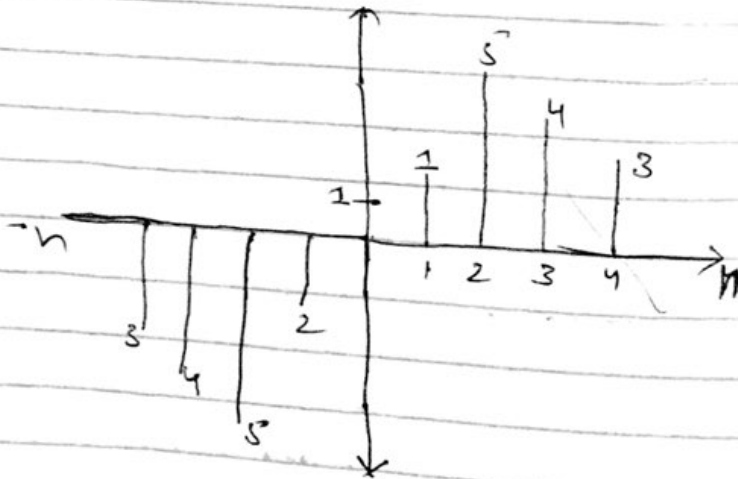
Reflect  $x[n]$  to get  $x[-n]$



$n_e[n]$ 

Odd Components of a function be written as

$$n_o[n] = \frac{n[n] - n[-n]}{2}$$

 $n_o[n]$ 

Q3

Part (ii) :-

Suppose an analog signal has a highest frequency of 60 Hz. outline the steps that will ensure that no aliasing occurs.

$f = 60 \text{ Hz}$  ensure that there is no aliasing occurs.

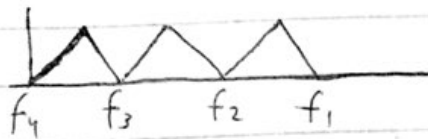
$$f = 60 \text{ Hz}$$

From Nyquist Criteria.

$$f_s \geq 2f_m$$

$$f_s \geq 2 \times 60$$

$$f_s \geq 120$$



if  $f_s = 120 \text{ Hz}$  there will be no aliasing occurs as Nyquist criteria proved it.

Q3 Part (i) :-

Discuss the procedure of converting an analogue signal into a digital signal.

Ans:-

Analogue signal is converted to a digital using a two step process.

\* Sampling

\* Quantization

The device used to do this is called as ADC (Analog to Digital Converter)

Step 1:-

Sampling converts a continuous time continuous amplitude (real valued) signal to discrete time continuous amplitude (Real value) signal.

Remember only time axis is discretized and not the amplitude axis.

Step 2:-

Quantization converts the discrete time continuous amplitude signal to discrete time and discrete valued.

(From a set of finite values so that it can be represented by finite bits and can be stored on a computer.)

Q49-

Show that:

$$x[n] * [h_1[n] * h_2[n]] \\ = [x[n] * h_1[n]] * h_2[n]$$

Consider

$$y[n] = [x[n] * h_1[n]] * h_2[n] \\ x[n] * h_1[n] = w_1[n]$$

Now

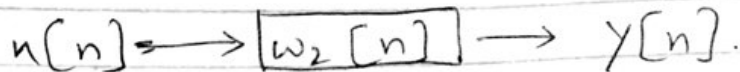
$$y[n] = [x[n] * h_1[n]] * h_2[n] \\ y[n] = w_1[n] * h_2[n]$$



Now consider that:-

$$w_2[n] = h_1[n] * h_2[n] \\ y[n] = x[n] * [h_1[n] * h_2[n]]$$

$$y[n] = x[n] * w_2[n]$$



As both block diagrams  
given the same response  
So:

$$L.H.S = R.H.S$$

Q 28-

Calculate the inverse Laplace transform of the given equation.

$$X(s) = \frac{s+4}{s^2+4s-12}$$

Soln-

$$\frac{s+4}{s^2+4s-12}$$

$$= \frac{s+4}{s^2+6s-2s-12}$$

$$= \frac{s+4}{s(s+6)-2(s+6)}$$

$$= \frac{s+4}{(s+6)(s-2)}$$

$$\frac{s+4}{(s+6)(s-2)} = \frac{A}{s+6} + \frac{B}{s-2}$$

$$s+4 = A(s-2) + B(s+6) \quad \text{--- (i)}$$



Page = 8

Let  $s = 2$  in eq ①

$$2+4 = A(2-2) + B(2+2)$$

$$2+4 = A(0) + B(4)$$

$$2+4 = B(4)$$

$$6 = B(4)$$

$$\frac{6}{4} = \frac{B(4)}{4}$$

$$\frac{3}{2} = B$$

Now let  $s = -2$

$$-2+4 = A(-2-2) + B(-2+2)$$

$$2 = A(-4) + B(0)$$

$$\frac{2}{-4} = \frac{A(-4)}{-4}$$

$$A = \frac{2}{-4} = \frac{1}{-2}$$

$$A = \frac{1}{-2}$$

Now put them back

Page = 9

$$= \frac{1}{-2} + \frac{3}{2} \frac{1}{s-2}$$

$$= \frac{1}{-2} \left[ \frac{1}{s+6} + \frac{3}{2} \left( \frac{1}{s-2} \right) \right]$$

$$= \frac{1}{-2} e^{-6t} + \frac{3}{2} e^{-2t}$$

✓