## Assignment

Problem 1: A construction company will replace an excavator after 5 years. A new one costs $\$ 250,000$. How much is the end-of-year annual uniform payment the company has to put into a bank in order to save enough money in five years' time for purchasing the equipment if the bank is offering an interest rate of $4 \%$ per annum?

## Solution 1:

Principal amount $=S=\$ 250,000 \quad$ Number of periods $=\mathrm{n}=5$
Interest rate in \% per period (nominal or apparent rate) $=\mathrm{i}=4 \%=0.04$
Annual uniform payment = A =?
Inflation free assumption is made for the solution


Fig. 1. - Sum of $\$ 250000$ accumulated by five uniform periodic (annual) payments.

## Using Formula:

$S=A x\left[\left\{(1+i)^{\wedge}-1\right\} / i\right]$
$A=S \times\left[i /\left\{(1+i)^{\wedge}-1\right\}\right]$
$250000=\mathrm{Ax}\left[\left\{(1+0.04)^{\wedge}-1\right\} / 0.04\right]$
$250000=\mathrm{A} \times[\{1.21665-1\} / 0.04]$
$250000=\mathrm{A} \times[0.21665 / 0.04]$
$250000=$ A x 5.4163
$\mathrm{A}=250000 / 5.4163$
$\mathrm{A}=46156.78$
A = \$ 46157
Therefore Annual uniform payment is $\mathbf{\$} 46157$.

Problem 2: A construction material company makes and sells window panels. The selling price per panel is $\$ 900$. The variable cost for making the window panels is $\$ 500$ per unit. The fixed cost is $\$ 8,000,000$. Find the BEP (break-even point)?

## Solution 2:

Selling Price per unit $=p=\$ 900$
Variable cost per unit $=\mathrm{v}=\$ 500$
Fixed Cost $=\mathrm{FC}=\$ 8,000,000$
Break-even point $=\mathrm{BEP}=$ ?
Number of units $=x$

## Using Formula:

TR $=\mathrm{a}+\mathrm{b}+\mathrm{c}+$ Profit
Total Cost (TC) $=$ Variable Cost (VC) + Fixed Cost (FC)
Where as
$\mathrm{TR}=$ total revenue
a =Direct cost (material, labour, equipment, etc)
$\mathrm{b}=$ Cost of administering the company
$\mathrm{c}=$ Costs of marketing/advertisements
At break-even point (BEP)
TR $=\mathrm{a}+\mathrm{b}+\mathrm{c}$
$\mathrm{TR}=\mathrm{TC}$
TR = px
TC = VC +FC
TC $=v x+F C$
So
Px = vx $+F C$
Hence, at BEP, $x=F C /(p-v)$

## Mathematical Presentation:

$\mathrm{x}=8000000 /(900-500)$
$\mathrm{x}=8000000 / 400$
$x=20000$ units
Therefore Break-even point (BEP) $=20000$ units
Let $\mathrm{x}=18000,20000$ and 22000

The above problem can be solved using the following table:

| Cost-volume-profit analysis (or Break-even analysis |  |  |  |  |
| :---: | :---: | :---: | :---: | :---: |
| Volume | $\mathrm{x}=18000$ | $\mathrm{x}=20000$ | $\mathrm{x}=22000$ | $\mathrm{x}=25000$ |
| Total Revenue | 16200000 | 18000000 | 19800000 | 22500000 |
| Variable Cost | 9000000 | 10000000 | 11000000 | 12500000 |
| Fixed Cost | 8000000 | 8000000 | 8000000 | 8000000 |
| Total Cost | 17000000 | 18000000 | 19000000 | 20500000 |
| Net Income | -800000 | 0 | 800000 | 2000000 |
|  | Loss | BEP | Profit |  |

By putting different values of $x$, we observe that the break-even occurs when volume $x$ is 20000 units. If the production of the company is less than 20000 units then the company is in loss and if production is greater than 20000 the company is making profit.

If the maximum capacity of the company is assumed 25000 units then the company's maximum profit is $\$ 2,000,000$.

BEP \% = [BEP/Maximum Capacity] x 100
ВЕР $\%=(20000 / 25000) \times 100$
BEP \% = 80\%

## Graphical presentation - Break-even chart:

The Break-even is a graphical presentation of TR, VC, FC and TC. The Fig. 2 below shows the break-even chart of problem 2.


Fig. 2. - The break-even chart for problem 2.

