

Date: _____

Day: M T W T F S S

ID: 7379

Name:-

FAHAD M. IRSHAD.

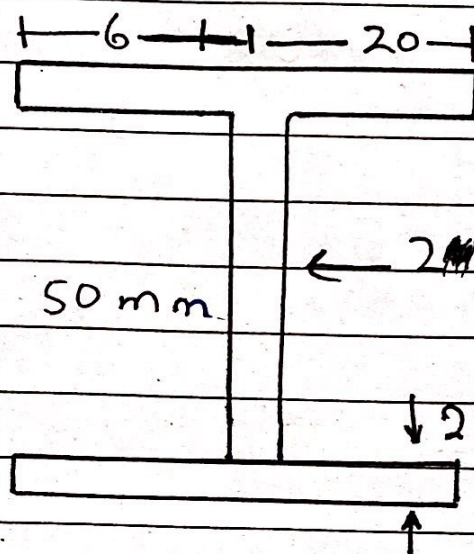
SUBJECT:-

MOS-II

Department:-

BE(Civil)

Q1 (a) :- Determine the location of the shear center for the beam having the cross section ----- calculations should be based on the centerline dimensions.



Required :- location of shear centre.

Sol :-

As we know

$$e = \frac{I_y h^2 b^2}{4I}$$

and :-

$$I = 2 \left(\frac{bh^3}{12} + Ay^2 \right) \left[\frac{bh^3}{12} + Ay^2 \right]$$

$$= 2 \left[\frac{26(2)^3}{12} + (20 \times 2)(25)^2 \right] + \left[\frac{2(50)^3}{12} + 0 \right]$$

$$I = 50034.66 + 20833$$

$$I = 70867.99 \text{ mm}^4$$

$$e = \frac{2(50)^2(25)^2}{4(70867.99)} = 11.02 \text{ mm}$$

So shear centre $e = 11.02 \text{ mm}$

Q. (b) :- Determine the thickness of the wall

 the specific weight of water is 62.4 lb/ft^3 .

Data :-

$$\Rightarrow H = 26 \text{ ft}$$

assume diameter =

$$D = 22 \text{ ft}$$

$$\Rightarrow \text{tangential stress} = 600 \text{ lb/ft}^2$$

\Rightarrow specific weight of water

$$\text{tank} = 62.4 \text{ lb/ft}^3$$

we have to find the thickness = ?

Solution :-

The pressure developed by water = $P = rh$

$$b_t = \frac{PD}{2t}$$

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$$6t = \frac{PD}{2t} = \frac{rhd}{2t}$$

$$2t \times 6t = rhd$$

$$2t = \frac{rhd}{6t}$$

$$t = \frac{rhd}{6t \times 2}$$

$$t = \frac{(62.4) \times (26 \times 12) \times (22 \times 12)}{(12)^3 \times 6000 \times 2}$$

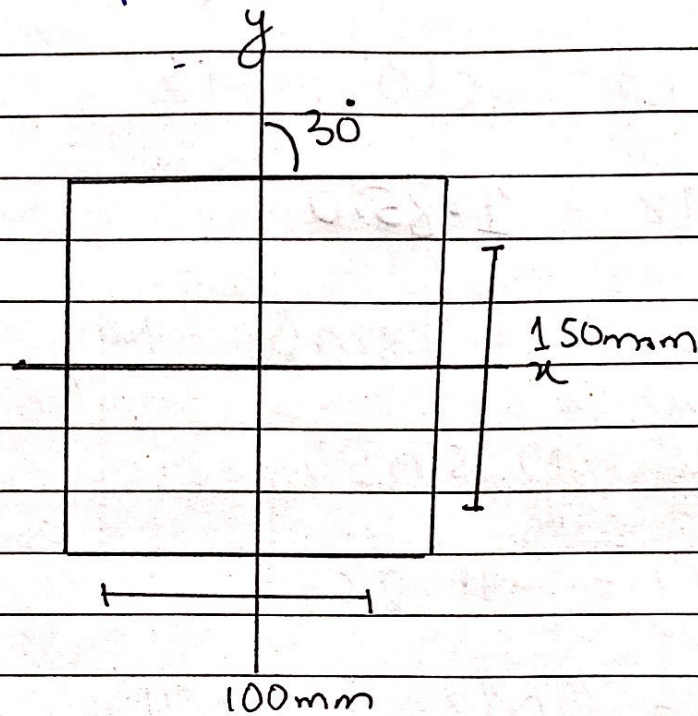
$$t = 0.24''$$

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Q2(a) :- The 100 by 150mm wooden beam shown in figure 2

.....
- - - - - Neglect the weight of the beam.



Moment of inertia

$$I_z = \frac{bh^3}{12} = \frac{0.1(0.15)^3}{12} = I_z = 2.8125 \times 10^{-5}$$

Now

$$I_y = \frac{hb^3}{12} = \frac{0.15(0.1)^3}{12}$$

$$I_y = 1.25 \times 10^{-5}$$

$$\sigma = \frac{Mzy}{I_z} + \frac{Myz}{I_y}$$

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$$\sigma = \frac{M \cos \theta}{I_z} + \frac{M \sin \theta}{I_y}$$

$$M \cos \theta = P \cos \theta = M_z$$

$$= 12 \cos 30^\circ = M_z$$

$$M_z = 10.8510$$

$$M \sin \theta = P \sin \theta = M_y$$

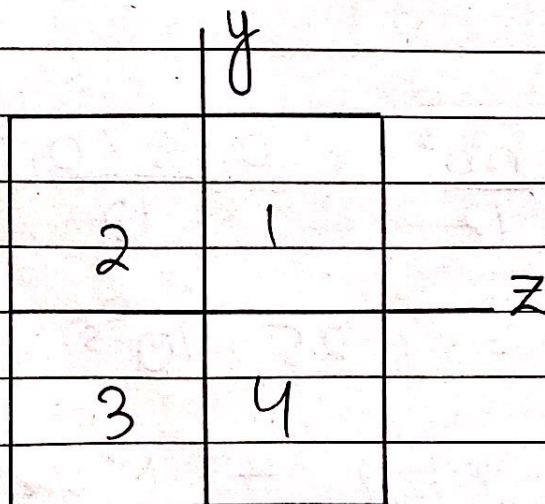
$$M_y = 12 \sin 30^\circ$$

$$M_y = -11.8563$$

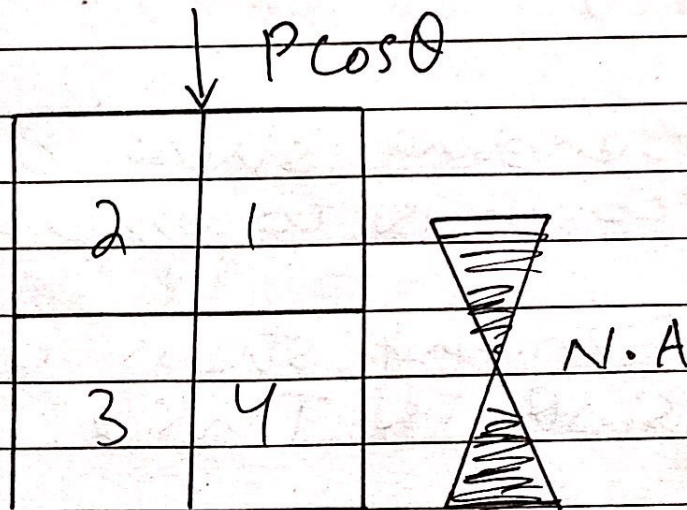
$$\sigma = \left(\frac{M_z}{I_z} \right) + \left(\frac{M_y}{I_y} \right)$$

$$\sigma = \frac{1.851}{2.812 \times 10^{-5}} + \frac{(-11.8563)}{1.25 \times 10^{-5}} = -882628 \text{ Nm}^2$$

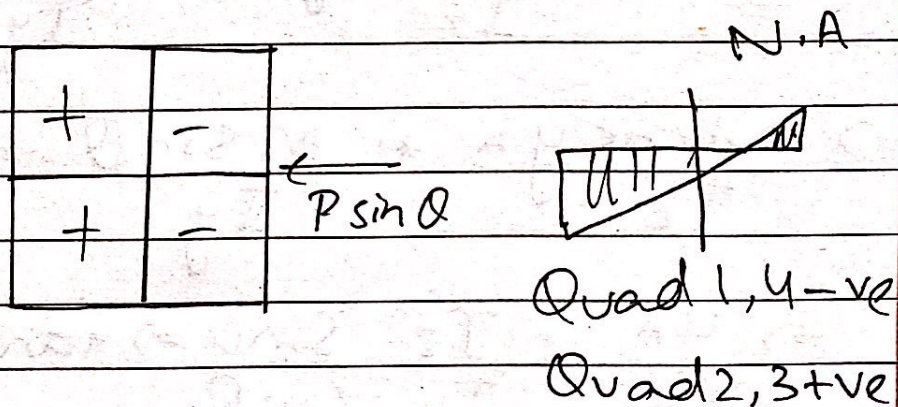
Sign Convention.



If we take compression as negative and tension as positive and the beam is a simply supported.



Quadrant 1, 2 -ve.
Quadrant 3, 4 +ve



Quad 1, 4 -ve
Quad 2, 3 +ve

In case of an symmetrical loading the neutral axis lies at an angle of α° . The Principal axis and the algebraic sum of stress at N.A. is zero.

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$$b = \frac{M \cos \theta}{I_z} y + \frac{M \sin \theta}{I_y} z$$

Let consider a point "A" on N.A lies in Quadrant 2, where

- Bending stress due to $P \cos \theta$ is compressive.
- Bending stress due to $P \sin \theta$ is Tensile.

$$\text{eq (1)} \Rightarrow 0 = -\frac{M \cos \theta y_A}{I_z} + \frac{M \sin \theta z_A}{I_y}$$

$$\Rightarrow 0 = -\frac{M \cos \theta y_A}{I_z} + \frac{M \sin \theta z_A}{I_y}$$

$$\Rightarrow \frac{M \cos \theta y_A}{I_z} + \frac{M \sin \theta z_A}{I_y}$$

$$\Rightarrow \frac{y_A}{z_A} = \frac{I_z \sin \theta}{I_y \cos \theta} \Rightarrow \tan \alpha = \frac{I_z \tan \theta}{I_y}$$

eq (2)

Now put values of I_z , I_y and θ in eq - (2)

$$\tan \alpha = \frac{I_z \tan 30}{I_y}$$

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$$\Rightarrow \tan \alpha = \frac{2.8125 \times 10^{-5} (\tan 30^\circ)}{1.25 \times 10^{-5}}$$

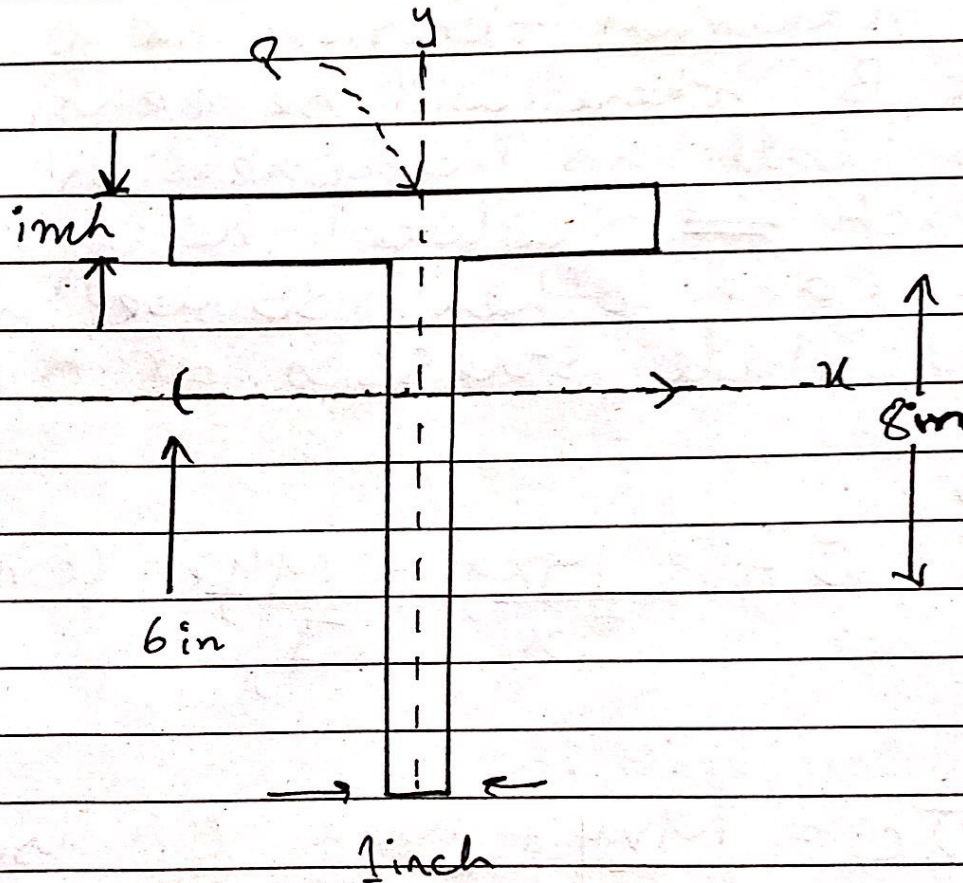
$$\tan \alpha = -14.4129$$

$$\alpha = \tan^{-1} (-14.4129)$$

$$\alpha = 1.5^\circ$$

$$\alpha = 1^\circ 30' 5''.$$

Q2 (b) :- The T section shown in figure 3 is the cross section of a simply supported beam. What is the maximum load that will not overstress the beam?



Given :-

$$L = 16 \text{ ft}$$

$$I_x = 112.6 \text{ in}^4$$

$$I_y = 18.7 \text{ in}^4$$

$$\sigma_c = 12000 \text{ psi}$$

$$\sigma_t = 5000 \text{ psi}$$

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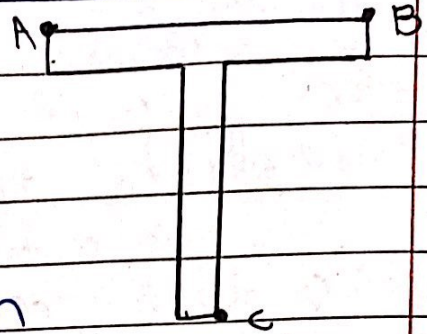
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Solution :-

By looking to the figure, we can judge that maximum compression would occur on A

& maximum tension at C.

at B there will be tension as well as compression, which ~~are~~ reduce the effects of each other. So we will calculate stresses at A & C.

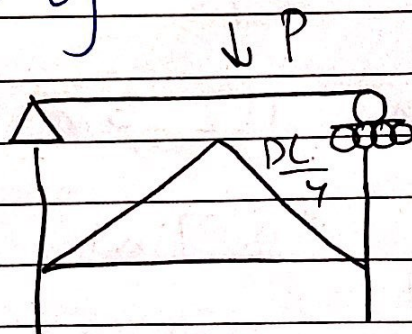


So,

$$\sigma_A = \frac{Mx_y}{I_x} + \frac{My_x}{I_y} \text{ (comp)}$$

$$\sigma_C = \frac{Mx_y}{I_x} + \frac{My_x}{I_y} \text{ (Tension)}$$

Now M_x & M_y



So

$$M_x = P \cos 60^\circ \times (16 \times 12)$$

4

$$M_x = 48P \cos 60^\circ$$

$$M_y = \frac{P \sin 60 (16 \times 12)}{4}$$

$$M_y = 48P \sin 60$$

Now

$$\sigma_A = \frac{M_{xy}}{I_x} + \frac{M_{yx}}{I_y}$$

$$\Rightarrow 12000 = \frac{48P \cos 60^\circ \times 3.07}{112.6} +$$

$$\frac{48P \sin 60^\circ \times 3}{18.7}$$

Solving the equation.

$$\Rightarrow \boxed{P = 1638.6 \text{ lb}}$$

Now

$$\sigma_C = \frac{M_{xy}}{I_x} + \frac{M_{yx}}{I_y}$$

$$5000 = \frac{48P \cos 60^\circ \times (5.93)}{112.6} + \frac{48 \sin 60^\circ \times 0.5}{18.7}$$

Solving the equation.

$$\boxed{P = 2104.9 \text{ lb}}$$

So the maximum load P
applied should be 1638.6 lb

Q3: A 10ft long strut braced in the middle has a rectangular Determine the safe load P about using a factor of safety of 2 and $E = 10.3 \times 10^6$

Given data :-

$$\text{length "L"} = 10 \text{ ft}$$

As both sides are hinged
So

$$l_e = L$$

$$E = 10.3 \times 10^6$$

$$\text{Factor of safety} = 2$$

$$b = 0.75 \text{ inch}$$

$$h = 2 \text{ inch}$$

Required data :-

Determine safe load?

Solution :- As

$$P_{cr} = \frac{\pi^2 EI}{l_e^2}$$

As we know that $I = Ar^2$

$$I = A r^2$$

$$r = \sqrt{\frac{I}{A}}$$

$$r = \sqrt{\frac{hb^3}{12bh}} \Rightarrow \sqrt{\frac{b^2}{12}}$$

$$r = \frac{b}{2\sqrt{3}} \Rightarrow \frac{0.75}{2\sqrt{3}}$$

$$r = 0.216 \text{ inch}$$

$$P_{cr} = \frac{\pi^2 EA}{(L/r)^2}$$

$$\Rightarrow \frac{(3.14)^2 (10.3 \times 10^6) (1.5)}{\left(\frac{10}{0.216}\right)^2}$$

$$P_{cr} = 853.8343$$

Safe load = $\frac{\text{Crushing load}}{\text{factor of safety}}$

$$\Rightarrow \frac{853.8343}{2}$$

$$\text{Safe load} \Rightarrow 426.917$$

★ for fixed ended column

$$L_e = \frac{L}{2} = \frac{10}{2}$$

$$L_e = 5 \text{ ft}$$

$$P_{cr} = \frac{\pi^2 EA}{\left(\frac{L_e}{r}\right)^2} \Rightarrow \frac{(3.14)^2 \times (10.3 \times 10^6)}{\left(\frac{10}{0.216}\right)^2} (1.5)$$

$$P_{cr} = 1974.207$$

$$\text{Safe Load} = \frac{P_{cr}}{\text{Factor of Safety}}$$

$$= \frac{1974.207}{2}$$

$$= \boxed{987.103} \quad \text{Ans.}$$