

Name M. Shawal Khan

ID 7813

Section A

Semester 6th.

Subject PRC 1

Q 1

Pg 1

Given Data:-

Clear span between supports = 15 ft.

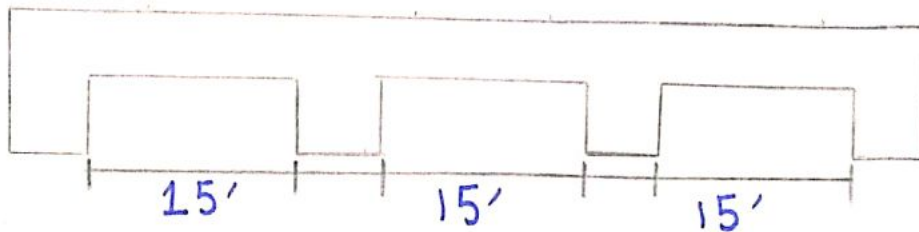
3 equal spans concrete slab.

Factored live load = 160 lb/ft^2

Service Floor finish load = 20 lb/ft^2

$f_c' = 4000 \text{ psi}$

$f_y = 40 \text{ ksi}$



Step 1 (Minimum Thickness)

Using formula

$$\begin{aligned} t_{\min} &= L/28 \\ &= 15/28 \\ &= 6.4 \approx 6.5' \end{aligned}$$

As $f_y \rightarrow 40 \text{ ksi}$

We have to multiply a factor with this thickness.

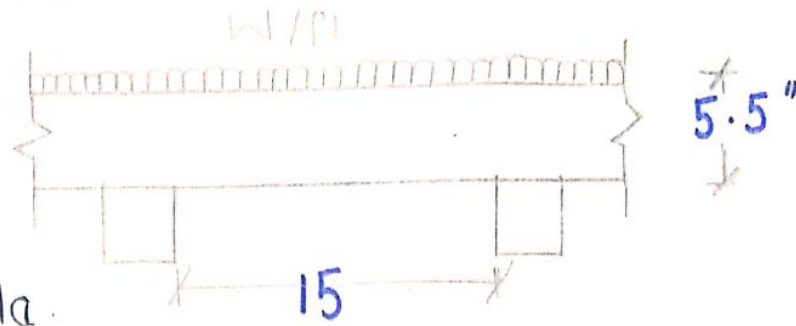
$$\begin{aligned} \text{Factor} &= \left(0.4 + \frac{f_y}{100} \right) \\ &= \left(0.4 + \frac{40}{100} \right) = 0.8. \end{aligned}$$

The minimum thickness will be

$$\begin{aligned} &6.5 \times 0.8 \\ t_{\min} &= 5.2 \approx 5.5'' \end{aligned}$$

Step 2 (Effective Depth)

Pg 2



Using formula.

$$\begin{aligned}d &= t - \text{clear cover} - \frac{1}{2} (\text{dia of main bars}) \\ &= 5.5 - 0.75 - \frac{1}{2} (5/8) \\ &= 4.5''\end{aligned}$$

Step 3 (Self weight of slab)

Using formula.

$$\frac{t}{12} + \gamma_{\text{concrete}}$$

$$\frac{5.5}{12} \times 150 = 68.75 \text{ lb/ft}^2.$$

Step 4 (Total Factored Load)

Factored live load = 160 lb/ft².

So factored dead load will be.

$$\begin{aligned}\text{Dead load} &= 1.2(20 + 68.75) \\ &= 106.5 \text{ lb/ft}^2.\end{aligned}$$

Now

$$\begin{aligned}\text{Total Factored load} &= D \cdot L + L \cdot L \\ &= 106.5 + 160 \\ &= 266.5 \text{ lb/ft}^2 \\ &= 0.2665 \text{ k/ft}^2.\end{aligned}$$

Step 5 (Ultimate Moment)

Using formula.

$$\begin{aligned}M_u &= \frac{W_u \times L^2}{8} = \frac{0.2665 \times (15)^2 \times 12}{8} \\ &= 89.94 \text{ kips-inch.}\end{aligned}$$

Step 6 Area of steel for main bars by trial Pg 3
and repeat method.

Trial : 1

Let depth of compression block.

$$a = 0.2 \times t \\ = 0.2 \times 5.5 = 1.1''$$

$$A_{st} = \frac{M_u}{\phi \times f_y \times (d - a/2)} = \frac{89.94}{0.90 \times 40 \times (4.5 - \frac{1.1}{2})}$$

$$A_{st} = 0.63 \text{ in}^2.$$

Trial 2

$$a = \frac{A_{st} \times f_y}{0.55 \times f_c' \times b} = \frac{0.63 \times 40}{0.85 \times 4 \times 12} = 0.62 \text{ in}^2$$

$$A_{st} = \frac{M_u}{\phi \times f_y (d - a/2)} = \frac{89.94}{0.90 \times 40 \times (4.5 - \frac{0.6}{2})}$$

$$A_{st} = 0.59 \text{ in}^2.$$

Trial 3

$$a = \frac{0.59 \times 40}{0.85 \times 4 \times 12} = 0.57''$$

$$A_{st} = \frac{89.94}{0.90 \times 40 \times (4.5 - \frac{0.57}{2})}$$

$$= 0.59 \text{ in}^2$$

So we use $A_{st} = 0.59 \text{ in}^2$

Step 7 Area of steel for distribution reinforcement

Using formula.

$$A_{min} = 0.002 \times b \times t \rightarrow (\text{For Grade 40 steel})$$

$$= 0.002 \times 12 \times 5.5 = 0.132 \text{ in}^2$$

Step 8 Spacing for main bars.

Using formula.

$$\text{Spacing} = \frac{A_b}{A_{st}} \times 12$$

We use # 6 bar dia = $(6/8)"$

$$\text{Area} = \pi/4 (6/8)^2 = 0.442 \text{ in}^2.$$

Step 9 Spacing for distribution bars.

$$\text{Spacing} = \frac{A_b}{A_{st}}$$

We use #5 bars dia.

$$\text{dia} = (5/8)"$$

$$\text{Area} = \pi/4 (5/8)^2 = 0.31 \text{ in}^2.$$

$$\text{Spacing} = \frac{0.31}{0.132} \times 12$$

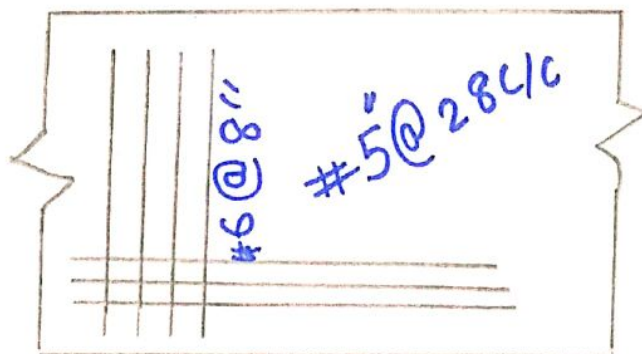
$$= 2.81 \approx 2.8" \text{ c/c}$$

Step 10 Find sketch.

$$f'_c = 4 \text{ ksi}, f_y = 40 \text{ ksi}$$

Main steel #6 at 9" c/c.

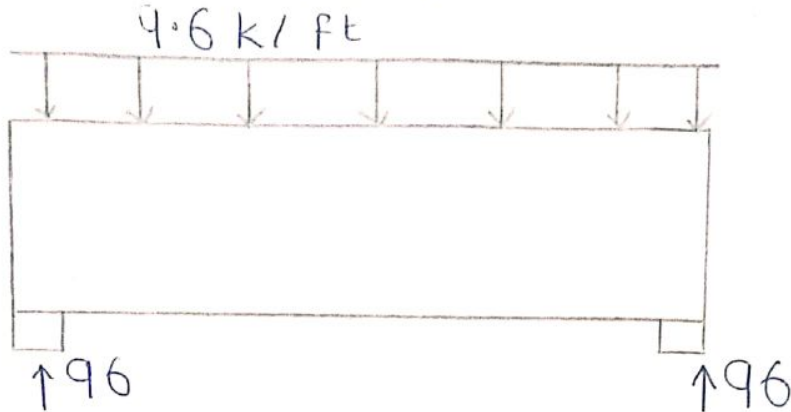
Distribution steel #5 at 28" c/c.



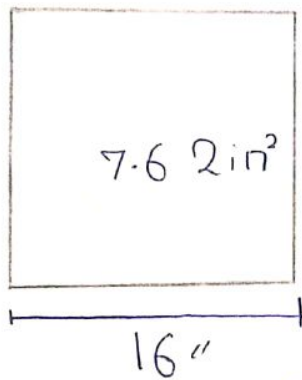
Sol:-

First we have to find unit load of beam
 $b \times hc = \frac{16}{12} \times 150 = 200 \text{ lb/ft} = 0.2 \text{ k/ft}$

$$\begin{aligned} \text{Total factored load} &= 9.4 + 0.2 \\ &= 9.6 \text{ k/ft} \end{aligned}$$



$$d = 2''$$

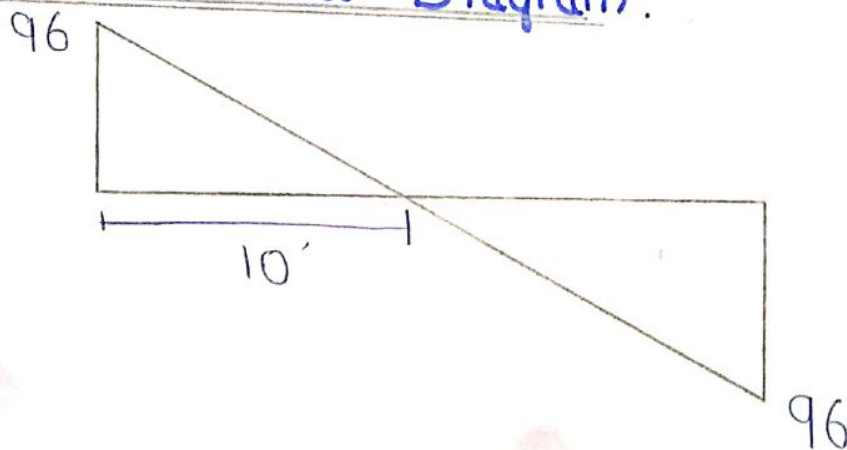


Step 1

Find value of R_1 & R_2

$$\begin{aligned} \text{Total load} &= 9.6 \times \frac{20}{2} \\ &= 96 \text{ k} \end{aligned}$$

Step 2 Shear Force Diagram.

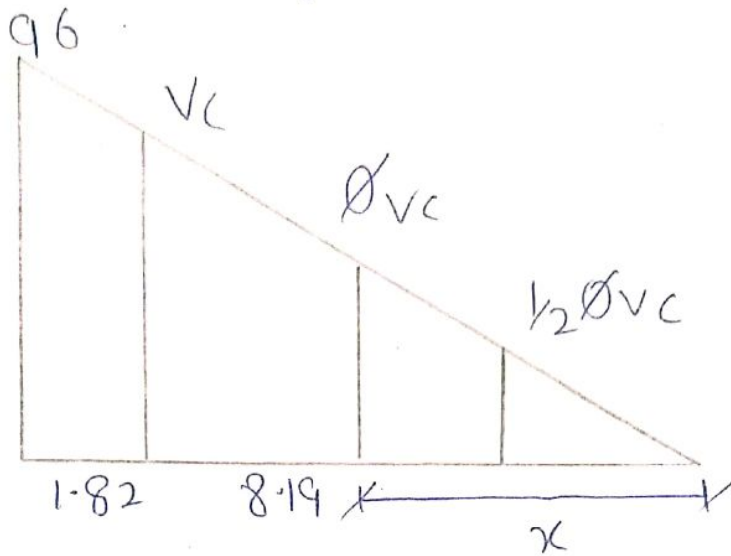


Step 3

Pg 6

Finding value of critical stress & its location

As we know critical section is located at distance "d" from face of $d = 22" = 1.83'$ value of critical shear at distance "d" by similarity triangles



Step 4

Find values of ' δV_c ' and ' $1/2 \delta V_c$ ' and also distance from zero shear to right side.

$$\delta V_c = \delta + 2\sqrt{f_c} \times b_w \times d$$

$$= \frac{0.75 \times 2\sqrt{4000} \times 16 \times 22}{1000}$$

$$\delta V_c = 33.40 \text{ k}$$

Location of δV_c by similarity of ' Δ 's'

$$\frac{q_4}{10} = \frac{33.40}{x_1}$$

$$x_1 = 3.55'$$

Now

$$1/2 \delta V_c = \frac{33.40}{2} = 16.70 \text{ k}$$

$$\text{Location of } 1/2 \delta V_c \Rightarrow \frac{q_4}{10} = \frac{16.70}{x_2}$$

$$x_2 = 1.78$$

Step 5 (Finding value of ϕV_s)

Pg 7

$$V_u = \phi V_s + \phi V_c$$

$$\begin{aligned} \phi V_s &= V_u - \phi V_c \\ &= 76.80 - 33.40 \\ &= 43.40 \text{ k.} \end{aligned}$$

Step 6

Check on Section adequacy

$$\begin{aligned} \phi \times 8 \times \sqrt{f_c'} \times b_w \times d &= \frac{0.75 \times 8 \times \sqrt{4000} \times 16 \times 22}{1000} \\ &= 133.57 \text{ k.} \end{aligned}$$

$$133.57$$

Step 7

Check ^{max} minimum spacing for stirrups

$$\begin{aligned} \phi \times 4 \times \sqrt{f_c'} \times b_w \times d &= \frac{0.75 \times 4 \times \sqrt{4000} \times 16 \times 22}{1000} \\ &= 66.79 \text{ k} > \phi V_s. \end{aligned}$$

\therefore maximum spacing will be selected from following 4 conditions.

1) $s_{\max} = 24''$

2) $d/2 = 22/2 = 11''$

3) $s_{\max} = \frac{0.22 \times 60000}{0.75 \sqrt{4000} \times 16}$
 $= 17.40$

4) $s_{\max} = \frac{0.22 \times 60,000}{50 \times 16}$
 $= 16.50''$

From above 4 conditions Least value of spacing for # 3, 2 legged stirrup will be selected for

Pg 8

$$s_{max} = 11" \text{ C/C.}$$

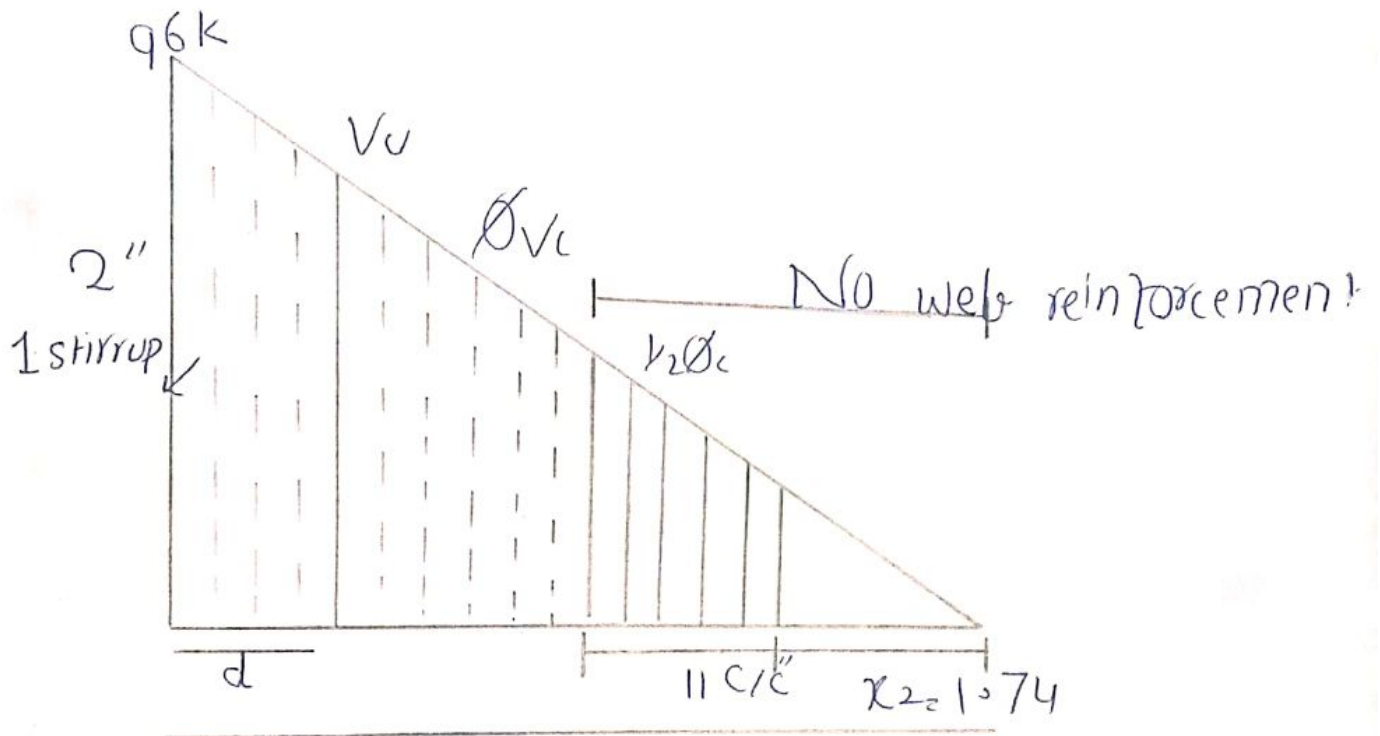
Step 8

Spacing of stirrup from/at Critical Section.

$$f = \frac{0.75 \times 0.22 \times 60 \times 22}{76.80 - 33.44}$$

$$= 5" \text{ C/C}$$

Step 9:-



As we know first stirrup from face of support

$$\frac{f}{2} = \frac{5}{2} = 2.5 \approx 2.$$

Step # 1

Find gross area of concrete

$$A_g = b \times b \quad (\text{Since it is square tied column})$$

$$A_g = 12 \times 12$$

$$= 144 \text{ in}^2 \quad (\text{Actual})$$

Step 2

Finding area of steel

$$\text{Since } A_s = 5\% \text{ of } A_g$$

$$= 0.05 \times 144$$

$$A_s = 7.2 \text{ in}^2$$

Step 3

Ultimate Load carrying capacity

$$P_u = \phi \times 0.80 \times [0.85 \times f_c' \times (A_g - A_s) + A_s \times f_y]$$

$$= 0.65 \times 0.80 [0.85 \times 4 (144 - 7.2) + 7.2 \times 60]$$

$$P_u = 466.50 \text{ k}$$

Step 4 Sketch & design of Ties (c/c distance)

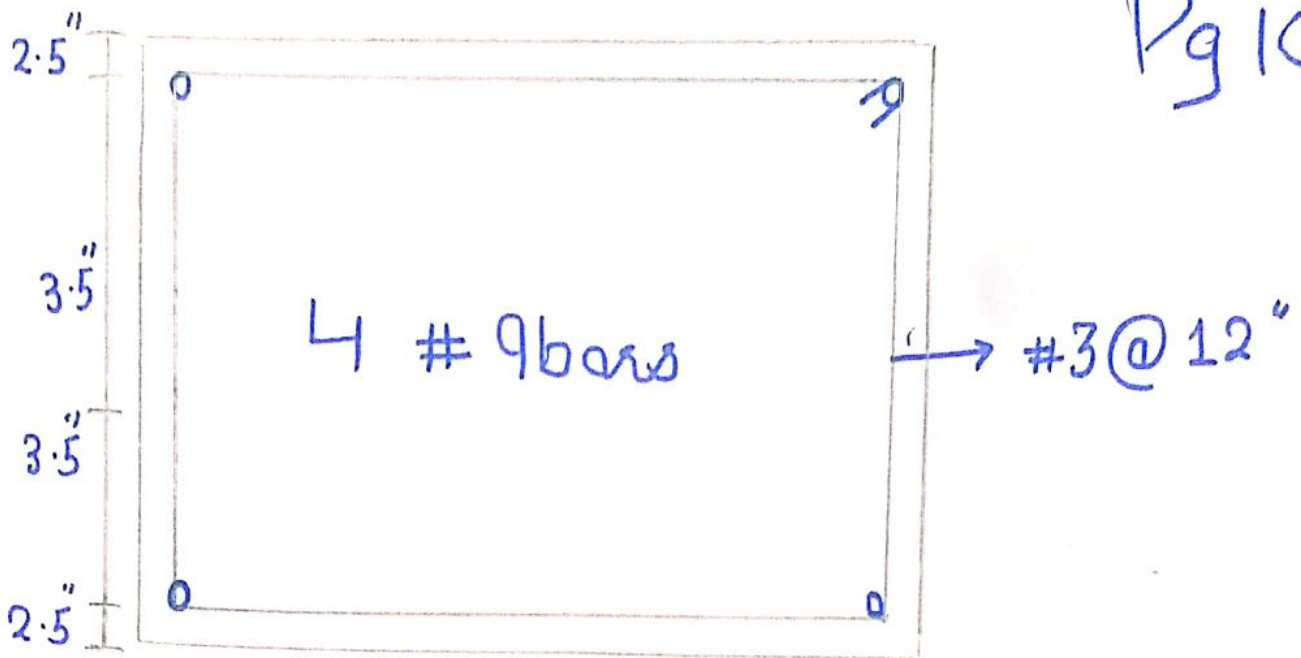
From below value we choose least value.

$$1) 16 \times \text{dia of long bar} = 16 \times 9/8 = 18''$$

$$2) 48 \times \text{dia of tie bar} = 48 \times 3/8 = 18''$$

$$3) \text{least column dimension} = 12''$$

$$\text{So C/c distance b/w ties} = 12''$$



Since it is a tied square column so there is no spiral stirrup used, the stirrup used is of rectangular shape due to specification of structure thus we have to use tie stirrup instead.

Step 1

$$\text{Let } h = 24''$$

Step 2

$$\begin{aligned} \text{Total weight} &= \text{wt of soil} + \text{wt of RC} \\ &= 3 \times 120 + 2 \times 150 \\ &= 660 \text{ psi} \\ &= 0.660 \end{aligned}$$

Step 3

Effective Bearing capacity

$$\begin{aligned} q_e &= q_a - W = 2.50 - 0.660 \\ &= 1.84 \text{ ksf} \end{aligned}$$

Step 4

Required area for foundation

$$\begin{aligned} \text{Area} &= \frac{\text{Service Load}}{q_c} \\ &= \frac{100 + 120}{1.84} \\ &= 119.56 \text{ ft}^2 \end{aligned}$$

Step 5:-

Since foundation is square.

$$\begin{aligned} \text{Area} &= B \times B \\ &= 119.56 \end{aligned}$$

$$B \Rightarrow \sqrt{119.56} = 10.93 \text{ ft} \approx 11 \text{ ft}$$

Step 6

upward bearing capacity of soil

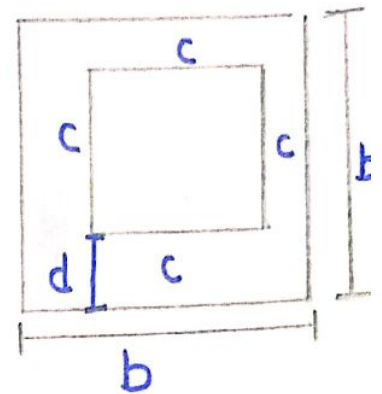
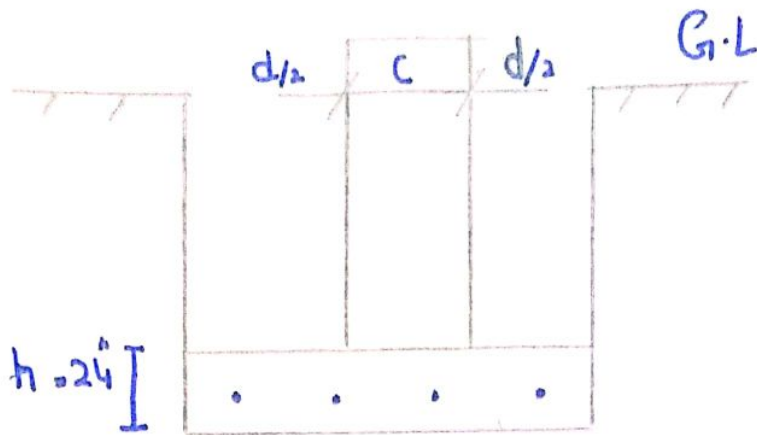
$$q_{up} = \frac{\text{Factored Load}}{(B)^2} = \frac{1.2 \times 100 + 1.6 \times 120}{(11)^2}$$

$$q_{up} = 2.58 \text{ k/ft}^2$$

Step 7 Punching Shear

Pg 12

$$b_o = 4 \times (c + d)$$



$$\begin{aligned} d &= h - c - c - \text{dia of bar} - \frac{1}{2}d_b \\ &= 24 - 3 - 1 - \frac{1}{2} = 19.5'' \\ b_o &= 4 \times (16 + 19.5) \\ &= 142'' \end{aligned}$$

Step 8

$$\begin{aligned} V_{u2} &= q_{up} \times [B^2 - (c+d)^2] \\ &= 2.58 \times \left[\frac{11^2 - (16 + 19.5)^2}{12} \right] \\ V_{u2} &= 289.60 \text{ k.} \end{aligned}$$

Step 9

$$\begin{aligned} \phi V_c &= \phi \times 4 \times \sqrt{f_c'} \times b \times d \\ &= \frac{0.75 \times 4 \times \sqrt{4000} \times 142 \times 19.5}{1000} \\ &= 525.38 \end{aligned}$$

Step 10

Beam shear one way shear Check

$$V_{u1} = q_{up} \times B \times [B/2 - c/2 - d]$$

$$V_u = 2.58 \times 11 \times \left[\frac{11}{2} - \frac{16}{2} - 19.5 \right]$$

$$= 90.95 \text{ k.}$$

Pg 13

Step 11 SELF Shear capacity

$$Q_{vc} = \phi \cdot 2 \times \sqrt{f_c'} \times b \times d$$

$$= \frac{0.75 \times 2 \times \sqrt{4000} [11 \times 12.16]}{1000}$$

$$= 110.04 \text{ k} < V_u, \Rightarrow \text{OK.}$$

Step 12 Ultimate moment.

$$M_u = \frac{q_{up} \times B \times (B - c)^2}{8}$$

$$= \frac{2.58 \times 11 \times (11 - 16/12)^2}{8}$$

$$= 331.49 \text{ k}' \approx 3977.93 \text{ k.}$$

Step 13 Area of steel for main bars by trial & Repeat method.

Trial 1 Let $a = 0.2 \times h = 0.2 \times 2.4 = 4.8''$

$$A_s = \frac{M_u}{\phi \times f_y \times (d - a/2)}$$

$$= \frac{3977.93}{0.90 \times 60 \times (11 - \frac{4.8}{2})}$$

$$= 8.56 \text{ in}^2$$

Trial 2

$$a = \frac{A_s \times f_y}{0.85 \times f_c' \times b} = \frac{8.56 \times 60}{0.85 \times 3 \times 11 \times 12}$$

$$= 1.53''$$

$$A_s = \frac{3977.93}{0.90 \times 60 \times \left(11 - \frac{1.53}{2}\right)}$$

$$= 7.197 \text{ in}^2$$

Trial 3

$$a = \frac{7.197 \times 60}{0.85 \times 3 \times 11 \times 12} = 1.28''$$

$$A_s = \frac{3977.93}{0.90 \times 60 \left(11 - \frac{1.28}{2}\right)} = 7.1 \text{ in}^2$$

$$\therefore \text{So area} = 7.1 \text{ in}^2$$

Step 14

Check min reinforcement by following 3 methods-

$$a) A_{smin} = 0.0018 \times B \times h = 0.018 \times (11 \times 12) \times 24 = 5.70 \text{ in}^2$$

$$b) A_{smin} = \frac{200 \times B \times h}{f_y} = \frac{200}{60000} (11 \times 12) 19.5 = 8.58 \text{ in}^2$$

$$c) A_{smin} = \frac{3 \sqrt{f_c'}}{f_y} \times B \times d = \frac{3 \sqrt{3000}}{60000} (11 \times 12) (19.5) = 7.05 \text{ in}^2$$

From above value greater will be selected

$$A_{smin} = 8.58 \text{ in}^2$$

$$A_b = 0.785 \text{ in}$$

$$\text{No of bars} = \frac{8.58}{0.785} = 10.92 \quad \checkmark \text{ 11 bars in each direction.}$$

Pg 14