

Subject: Applied Calculus

Assignment No.: 01

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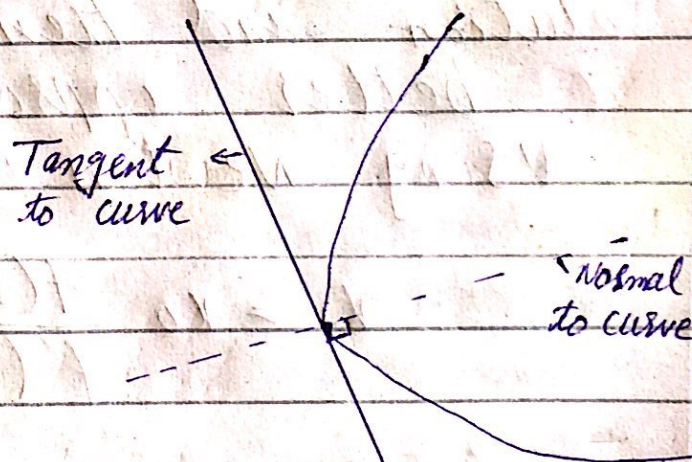
Application of Derivatives and Integration in Engineering.

We use the derivatives to determine the maximum and minimum values of particular function e.g. cost, strength, amount of material used in Building, Profit loss etc.

Derivatives are met in many Engineering and Science problems, especially when the modeling the behavior of moving objects. our discussion begin with some general applications which we can apply specific problems.

Tangents And Normal:

A tangent to a curve is a line that touches the curve at one point and has the same slope as the curve at that point. A normal to a curve is a line perpendicular to a tangent of the curve.



We can find the slope of a tangent at any point (x, y) using $\frac{dy}{dx}$.

Newton's Method:

The process involves making a guess at the true solution and then applying formula to get a better guess and so on until we arrive at an acceptable approximation for the solution.

If we wish to find x so that $f(x) = 0$ then we guess some initial value x_0 which is close to desired solution and then we get a better approximation.

Using Newton Method

$$x_1 = x_0 - \frac{f(x_0)}{f'(x_0)}$$

Related Rates:

If two variables both vary with respect to time and have relation between them, we can express the rate of change of one in terms of one another.

That is we will be finding $\frac{df}{dt}$ for some function $f(t)$.

Curvilinear Motion:

$$v = \frac{ds}{dt}, \quad a = \frac{dv}{dt} = \frac{d^2s}{dt^2}$$

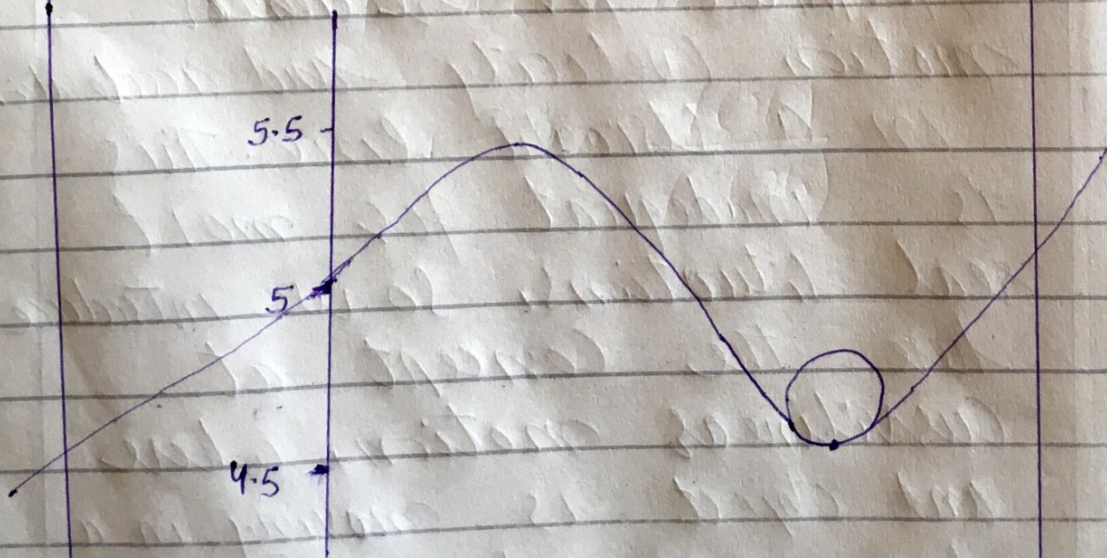
These formula are only appropriate for rectilinear motion (velocity and acceleration) in a straight line. This is inadequate for most real situations, so we introduce here the concept of curvilinear motion, where an object is moving in a along a specified curved path.

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Radius of Curvature:

$$\text{Radius of curvature} = \frac{[1 + (\frac{dy}{dx})^2]^{3/2}}{[\frac{d^2y}{dx^2}]}$$

The radius of curvature of the curve at a particular point is defined as the radius of the approximating circle. This radius changes as we move along the curve. The formula for the radius of curvature at any point x for the curve $y = f(x)$.



Application of Integration

Integration:

The process of finding a function, given its derivatives is called integration or anti derivation.

It is usually used to find Area.

Shear Force and Bending Moment:

Shear force and Bending moment are one of the most important parameters for the structural design.

These parameters affect a structure.

Take example of a rod suspended between two horizontal supports and some load applied at the centre with application of load the beam will load.

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That force is called
called shear force
and product of that
force with distance from
either end is bending
moment.

Length of curve:

Corrugated iron sheeting:
corrugated iron is used extensively
through out the world as
versatile building material
into a regular sine wave
pattern gives it greater
strength than if a flat sheet
is used.

Area Under a Curve by Integration:

In civil engineering
when we are dealing with
curve or structure having
curve then many need

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to find the Area under Curve which is to be constructed so we use integration for this purpose.

$$\text{Area} = \int_a^b f(x) dx$$

Centroid of an Area By Integration:

In tilt-slab construction we have a concrete wall with doors and windows cut out) which we need to raise into position. We don't want the wall to crack as we raise it, so we need to know the centre of mass of the wall. We can find the centroid of an area with straight sides, then we will extend the concept to areas with curved sides where we will use integration.