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Question No(1)

Answer (a)

Biconditional Statement

A biconditional statement is a single true statement that combines a true conditional ... with its converse

Conditional Statement

If hypothesis, then conclusion

Converse Statement

If conclusion, then hypothesis.

So if both the conditional & its converse are true,

they can be combined into a Biconditional Statement

"Hypothesis if & only if conclusion".

They can be denoted by double-headed arrow like (\leftrightarrow)

The biconditional $P \leftrightarrow Q$ represented

"P" if & only if "Q"

where "P" is a hypothesis

& "Q" is a conclusion

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Now the following is truth table for biconditional

$P \leftrightarrow Q$

P	Q	$P \leftrightarrow Q$
T	T	F
T	T	F
T	F	F
T	F	T
F	T	T
F	T	T
F	F	T
F	F	F

Part (b)

i) Sam had Pizza last night and Chris finished her homework. $P \wedge Q$

ii) Pat watched the news this morning iff Sam did not have Pizz last Night

$$Q \leftrightarrow \neg P$$

iii) $Q \leftrightarrow (Q \wedge \neg P)$

iv) $Q \leftrightarrow (P \wedge Q)$



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Question No(2)

Answer

Let Suppose

i) $P = \text{It is hot today}$

$Q = \text{It is Sunny}$

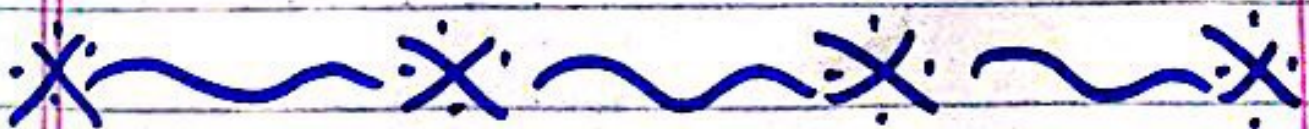
$R = \text{It is raining}$

i) $\text{It is } \cancel{\text{Sun}} \text{ Sunny iff } \& \text{ and}$
 $\text{only if it is hot today}$

ii) $\text{It is hot today iff it is}$
 $\text{Sunny } \& \text{ it is raining}$

iii) $\text{It is hot today iff it}$
 $\text{is Sunny or it is raining}$

iv) $\text{It is raining iff it is hot}$
 $\text{today or it is Sunny.}$



Question No (3)

Answer

Argument: In logic & Philosophy, an argument is a series of statements (in a natural language), called the premises or premisses (both spellings are acceptable), intended to determine the degree of truth of another statement, the conclusion.

"OR"

Mathematics

mathematically argument \Rightarrow

A mathematically argument is a sequence of statement & reasons given with the aim of demonstrating that a claim is true or false.

Example \Rightarrow If it is cloudy outside, then it will rain.

\Rightarrow "It is not cloudy outside"
a conclusion might be

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"It would rain" Intuitively,
This seems valid

→ An argument is considered
valid if from the truth
of all premises, the conclusion
is & must also be true.

**Example of valid argument
form.**

Premises $\Rightarrow P \vee (q \vee r) \ \& \ \sim r$,

Conclusion = $P \vee q$

Example of invalid argument

Premises $\Rightarrow P \vee q \vee \sim r \ \& \ q \vee P \wedge r$,

Conclusion $(P \vee r)$.

**Differentiate valid & invalid
argument** → Argument is valid

if the conclusion is true
when all the premisses are
true or if conjunction of
its premisses imply conclusion

$P_1 \wedge P_2 \wedge P_3 \wedge \dots \wedge P_n \rightarrow C$ is a
tautology.

→ Argument is invalid if
the conclusion is false

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When all the Premises are true or if conjunction of its Premises does not imply Conclusion.

$P_1, P_2, P_3, \dots, P_n \rightarrow C$ is a Contradiction.

→ False Premises & a true conclusion

OR False Premises & a false conclusion.

→ Argument may either valid or invalid & Statement may true or false.

→ **Example** (1) Anyone who lives in the City London, He also lives on the island of London.

He does not live on the island of London.

Therefore, He does not live in the city London (invalid)

2) All cows are black. only cow are black.

Abc is black

Abc is black

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Therefore, Abc is a crow (valid)

truth table

$P \rightarrow Q$: If my ~~computer~~ laptop crashes, I will lose all my photos.

$\sim Q = \text{If } \text{my}$

$\sim Q = 1$ have not lost all my photos. ~~con~~

\Rightarrow Conclusion \Rightarrow

$\sim P \Rightarrow$ My laptop has not crashed

Argument $\Rightarrow [(P \rightarrow Q) \wedge \sim Q] \rightarrow \sim P$

P	Q	$\sim P$	$\sim Q$	$(P \rightarrow Q)$	$[(P \rightarrow Q) \wedge \sim Q] \rightarrow \sim P$
T	T	F	F	T	T
T	F	F	T	F	T
F	T	T	F	T	T
F	F	T	T	T	T

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Question No(4)

Answer

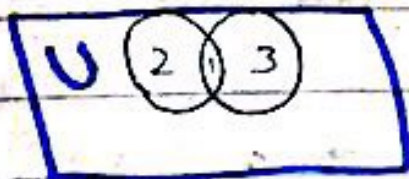
Part (A) Union - Two Set :

operations the Union of two Sets is a set containing all elements that are in "A" or in "B" (Possibly both).

Example \Rightarrow Let suppose $A = \{1, 2\}$
 $\&$ $B = \{2, 3\}$ Now $A \cup B = \{1, 2\} \cup \{2, 3\} \Rightarrow \{1, 2, 3\}$

Thus we can write $x \in (A \cup B)$ if & only if $(x \in A)$ or $(x \in B)$.

Union Represented by 'U'



Truth table for Union

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A	B	A ∪ B
0	0	0
0	0	0
0	1	1
0	1	1
1	0	1
1	0	1
1	1	1
1	1	1

Part "B"

Intersection The intersection of two sets is a new set that contains all of the elements that are common in both sets. The intersection is can be write written as $A \cap B$ or $A \cap B$.

Intersection represented by " \cap "

An intersection only taken common element.

For example $A = \{1, 2, 3, 4\}$ $B = \{3, 4, 5, 6\}$
 $A \cap B = \{3, 4\}$.

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Truth table For Intersection

P	q	$P \cap q$
T	T	T
T	F	F
F	T	F
F	F	F



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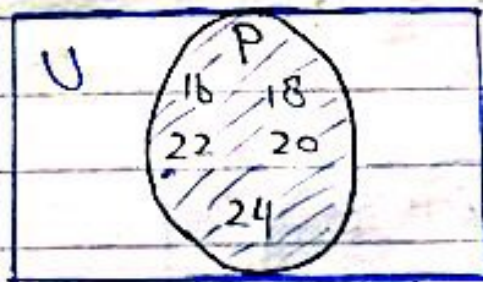
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Question No(S)

Answer Part "B"

Solution(B) Let $P = \{16, 18, 20, 22, 24\}$

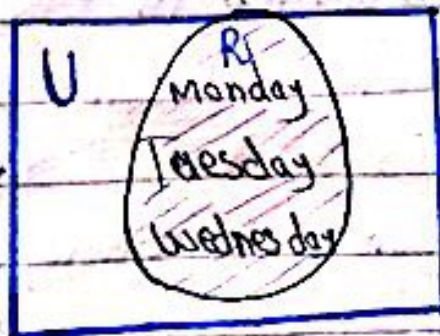
Now Venn Diagram of Set "P"



Part(c) Solution

Let $R = \{\text{Monday, Tuesday, Wednesday}\}$

Venn Diagram.



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Part (D) Solution

$$2x - 3 < 11$$

$$\Rightarrow 2x < 11 + 3$$

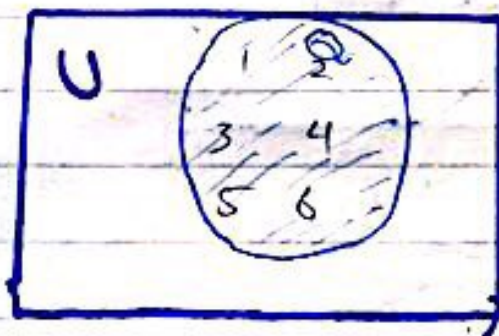
$$2x < 14$$

$$\frac{2x}{2} < \frac{14}{2}$$

$$x < 7$$

So the set is

$$Q = \{1, 2, 3, 4, 5, 6\}$$



Part (A)

Venn Diagram \Rightarrow A Venn diagram is an illustration that uses circles to show the relationship among things. Circles that overlap have a commonality while circles

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That do not overlap do not share those traits.

Venn diagrams help to visually represent the similarities & differences b/w two concepts.

They have long been recognized for their usefulness as educational tools. Since the mid-20th century, Venn diagrams have been used as part of the introductory logic curriculum & in elementary-level educational plans around the world.

Important: Venn-Diagram have been used since the mid-20th century in classroom from the elementary school level to introductory logic.

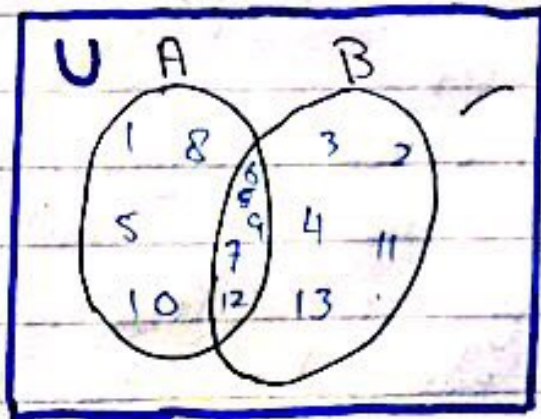
Applications: Venn diagrams are used to depict how used items relate to each other against an overall backdrop, universe, data set or environment.

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Example = There are two sets, $A = \{1, 5, 6, 7, 8, 9, 10, 12\}$ & $B = \{2, 3, 4, 6, 7, 9, 11, 12, 13\}$. The section where the two sets overlap has the numbers contained in both Set A & B, ~~is~~ referred to as the intersection of A & B. The two sets put together, gives their union which comprises of all objects in A, B which are: $\{1, 2, 3, 4, 5, 6, 7, 8, 9, 10, 11, 12, 13\}$



U = a complete Venn Diagram represents this.



The End