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***Dep***                        ***civil engineering***

***Subject***                ***Probability and statistics***

***Assignment***        ***Final term***

***Semester***                ***8<sup>th</sup>***

***Submitted to***        ***Sir Anwar shamim***

Q No 1

Compute and analyse the results of the least squares regression equation and Co-efficient of Correlation of Y on X for the following data. Compare your manual with the outcome of SPSS?

	ID											
Temperature	53	62	57	71	78	81	86	87	96	91	94	94
chirps per min	20	32	45	60	80	100	120	140	160	180	200	210

Solution: (i) (A) Least Square Regression Equation.

$$\bar{y} = a + bx$$

$$a = \bar{y} - b\bar{x}$$

$$b = \frac{n \sum xy - \sum x \sum y}{n \sum x^2 - (\sum x)^2}$$

②

X	Y	XY	X <sup>2</sup>	Y <sup>2</sup>
53	20	1060	2809	400
62	32	1984	3844	1024
57	45	2565	3249	2025
71	60	4260	5041	3600
78	80	6240	6084	6400
ID= 81	100	8100	6561	10000
86	120	10320	7396	14400
87	140	12180	7569	19600
96	160	15360	9216	25600
91	180	16380	8281	32400
94	200	18800	8336	40000
94	210	19740	8836	44100
$\Sigma x = 950$	$\Sigma y = 1347$	$\Sigma xy = 116989$	$\Sigma x^2 = 77722$	$\Sigma y^2 = 199549$

$$\bar{x} = \frac{\Sigma x}{n} = \frac{950}{12} = 79.16$$

$$\bar{y} = \frac{\Sigma y}{n} = \frac{1347}{12} = \underline{\underline{112.25}}$$



(3)

$$b = \frac{n \sum xy - \sum x \sum y}{n \sum x^2 - (\sum x)^2}$$

$$b = \frac{12(116989) - (950)(1347)}{12(77722) - (950)^2}$$

$$b = 4.11$$

$$a = \bar{y} - b\bar{x}$$

$$a = 112.25 - 4.11(79.16)$$

$$a = -213.0976$$

$$\bar{y} = a + bx$$

$$\bar{y} = -213.0976 + 4.11x$$

Regression line equation

(4)

(B) Co efficient Correlation  $\gamma$  on  $x$ .

$$\gamma = \frac{n \sum xy - \sum x \sum y}{\sqrt{n \sum x^2 - (\sum x)^2} \sqrt{n \sum y^2 - (\sum y)^2}}$$

$$\gamma = \frac{12(116989) - (950)(1347)}{\sqrt{12(77722) - (950)^2} \sqrt{12(199549) - (1347)^2}}$$

$$\gamma = \frac{124218}{5.6019 \times 10^{11}}$$

$$\boxed{\gamma = 2.217 \times 10^{-7}}$$

$\Rightarrow$  Hence the estimated regression coefficient  $b = 4.11$  which indicate that the value of  $y$  increase by  $4.11$  units of increase in  $x$ .

B5 : 0.82769811107047

SUMMARY OUTPUT

Regression Statistics	
Multiple R	0.909779155
R Square	0.827698111
Standard Error	6.720036402
Observations	12

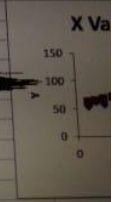
ANOVA

	df	SS	MS	F	Significance F
Regression	1	2169.327774	2169.327774	48.03766901	4.03958E-05
Residual	10	451.5888924	45.15888924		
Total	11	2620.916667			

	Coefficients	Standard Error	t Stat	P-value	Lower 95%	Upper 95%	Lower 95.0%	Upper 95.0%
Intercept	56.13958451	3.941081363	14.24471594	5.73823E-08	47.358308	64.92086101	47.358308	64.92086101
X Variable 1	0.211822558	0.030561963	6.930921224	4.03958E-05	0.143726261	0.279918855	0.14372626	0.279918855

RESIDUAL OUTPUT

Observation	Predicted Y	Residuals
1	60.37603567	-7.376035672
2	62.91790637	-0.91790637





Q2

(a)  $\Rightarrow$  Solution:

$$n(S) = \binom{13}{3} = 286$$

4 - R
4 - W
5 - G
13 - balls

Let  $A$  = Denote all balls are of different colours.

$$n(A) = \binom{4}{1} \binom{4}{1} \binom{5}{1} = 4 \times 4 \times 5 = 80$$

$$P(A) = \frac{n(A)}{n(S)} = \frac{80}{286} = 0.28$$

$2 \times 2 \times 2 = 8$ even $\times$ even $\times$ even = even	$3 \times 2 \times 2 = 12$ odd $\times$ even $\times$ even = even	$3 \times 3 \times 2 = 18$ odd $\times$ odd $\times$ even = even
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Interpretation: There are 28% chances that all balls are of different colours.

(ii) let  $B$  = Denote all balls of Same Colours.

$$n(B) = \binom{4}{3} \text{ or } \binom{4}{3} \text{ or } \binom{5}{3}$$

Red                  white                  Green

$$= \binom{4}{3} + \binom{4}{3} + \binom{5}{3} = 4 + 4 + 10 = 18$$

$$P(B) = \frac{n(B)}{n(S)} = \frac{18}{286} = 0.063$$

Interpretation:- There are 6.3% chances that all balls of same colour.



Q2  
(b) Solution:

$$n(S) = \binom{12}{4} = 495$$

2 - B
10 - G
12 - Eggs

Let  $A$  = denote the event that exactly one egg is bad.

$$n(A) = \binom{2}{1} \binom{10}{3} = 2 \times 120 = 240$$

$$P(A) = \frac{n(A)}{n(S)} = \frac{240}{495} = 0.48$$

Interpretations: There are 48% chances that exactly one egg is bad.

(ii) Let  $B$  = be the event that at least one bad egg is selected.

$$\begin{aligned} n(B) &= \binom{2}{1} \binom{10}{3} + \binom{2}{2} \binom{10}{2} \\ &= 2 \times 120 + 1 \times 45 = 240 + 45 = 285 \end{aligned}$$

$$P(B) = \frac{n(B)}{n(S)} = \frac{285}{495} = 0.58$$

Interpretation: There are 58% chances that at least one bad egg is selected.

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X

Q3

①

ok - not a square

ok - not a square

o - 11k

241

ok - not a square

2 - 13

Solution:

	A	B	C
	12	47	15
	15	12	23
	6	76	52
	73	48	4
	7	4	24
10	81	81	81
	199	37	74
	36	48	52
	84	13	13
	29	3	4



(2)

$$\text{Range} = X_m - X_0$$

$$\text{Range of A} = X_m - X_0$$

$$= 199 - 6$$

$$= 193$$

$$\text{Range of B} = X_m - X_0$$

$$= 81 - 3$$

$$= 78$$

$$\text{Range of C} = X_m - X_0$$

$$= 81 - 4$$

$$= \underline{\underline{77}}$$

(3)

BATSMAN A		BATSMAN B		BATSMAN C	
X	X <sup>2</sup>	Y	Y <sup>2</sup>	Z	Z <sup>2</sup>
12	144	47	2209	15	225
15	225	12	144	23	529
6	36	76	5776	52	2704
73	5329	48	2304	4	16
7	49	4	16	24	576
81	6561	81	6561	81	6561
199	39601	37	1369	74	5476
36	1296	48	2304	52	2704
84	7056	13	169	13	169
29	841	3	9	4	16
$\Sigma X = 542$	$\Sigma X^2 = 61138$	$\Sigma Y = 369$	$\Sigma Y^2 = 20864$	$\Sigma Z = 342$	$\Sigma Z^2 = 18976$



(4)

BATSMAN A :

$$\bar{x} = \frac{\sum x}{n} \quad \therefore n = 10$$

$$= \frac{542}{10} = \underline{\underline{54.2}}$$

$$S_x = \sqrt{\frac{\sum x^2}{n} - \left(\frac{\sum x}{n}\right)^2}$$

$$= \sqrt{\frac{61138}{10} - \left(\frac{542}{10}\right)^2}$$

$$S_{\bar{x}} = 56.35$$

$$C.V = \frac{56.35 \times 100}{\bar{x}} = \frac{56.35}{54.2} \times 100$$

$$C.V = 1.03 \times 100$$

$$C.V = 103.96$$



⑤

BATSMAN B

$$\bar{y} = \frac{\sum y}{n} = \frac{369}{10} = \cancel{37.9} 36.9$$

$$S_y = \sqrt{\frac{\sum y^2}{n} - \left(\frac{\sum y}{n}\right)^2}$$

$$= \sqrt{\frac{20861}{10} - \left(\frac{369}{10}\right)^2}$$

$$= 26.91$$

$$C.V = \frac{26.91}{36.9} \times 100$$

$$\boxed{C.V = 72.92\%}$$

(6)

BATSMAN C :

$$\bar{z} = \frac{\sum z}{n} = \frac{342}{10} = 34.2$$

$$S_z = \sqrt{\frac{\sum z^2}{n} - \left(\frac{\sum z}{n}\right)^2}$$

$$= \sqrt{\frac{18976}{10} - \left(\frac{342}{10}\right)^2}$$

$$S_z = 26.98$$

$$C.V = \frac{S_z}{\bar{z}} = \frac{26.98}{34.2} \times 100$$

$$\boxed{C.V = 78.88}$$

(7)

BATSMAN B is more consistent  
as its value of Co-efficient of  
Variation is smallest.

Compare A with B.

$\Rightarrow$  B is consistent.

Compare B with A

$\Rightarrow$  B is more consistent.

Compare A with C.

$\Rightarrow$  C is more consistent.