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SUBMITTED TO: SIR ANWAR SHAMIM

SUBJECT : Prob & Statistics

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(7830)

Q No 1 : Compute & analyse the result of the least square regression equation & coefficient of correlation of 'Y' on 'X' for the following data. compare your manual results with the outcomes of SPSS?

Temperature = 53 62 57 71 78 10(30) 86 87 96 91 94 94
chirps per mint = 20 32 45 60 80 100 120 140 160 180 200 210

X	Y	XY	X ²
53	20	1060	2809
62	32	1984	3844
57	45	2565	3249
71	60	4260	5041
78	80	6240	6084
30	100	3000	900
86	120	10320	7396
87	140	12180	7596
96	160	15360	9216
91	180	16380	8281
94	200	18800	8836
94	210	11280	8836
$\Sigma = 899$	$\Sigma = 1347$	$\Sigma = 103429$	$\Sigma = 72088$

$$y = a + bx \text{ --- (i)}$$

$$a = \bar{y} - b\bar{x} \text{ --- (ii)}$$

$$\text{So } \bar{y} = \frac{\sum y}{n} = \frac{1347}{12} = 112.25$$

$$\bar{x} = \frac{\sum x}{n} = \frac{899}{12} = 74.92$$

Where

$$b = \frac{n \sum xy - \sum x \cdot \sum y}{n \sum x^2 - (\sum x)^2}$$

$$b = \frac{12(103429) - (899)(1347)}{12(72088) - (899)^2}$$

$$b = 0.53$$

putt the value of \bar{y} , b , \bar{x} in eqn (ii)

$$a = 112.25 - 0.53(74.92)$$

$$a = 112.25 - 39.7076$$

$$a = 72.54$$

Q2 (A)

Solution

$$(i) \quad n(S) = \binom{13}{3} = 286$$

let A = Donate all balls are different colours

$$n(A) = \binom{4}{1} \binom{4}{1} \binom{5}{1} = 4 \times 4 \times 5 = 80$$

$$P(A) = \frac{n(A)}{n(S)} = \frac{80}{286} = \boxed{0.28}$$

(ii)

let B = Donate all balls of same colour

$$n(B) = \binom{4}{3} \text{ (Red)} \text{ or } \binom{4}{3} \text{ (White)} \text{ or } \binom{5}{3} \text{ (Green)}$$

$$= \binom{4}{3} + \binom{4}{3} + \binom{5}{3} = 4 + 4 + 10 = 18$$

$$P(B) = \frac{n(B)}{n(S)} = \frac{18}{286} = \boxed{0.063}$$

Q no (2)

(B)

Solution

$$n(S) = \binom{12}{1} = 12$$

Let A = denote the event the exactly one egg is bad.

$$n(A) = \binom{2}{1} \binom{10}{1} = 2 \times 10 = 20$$

$$P(A) = \frac{n(A)}{n(S)} = \frac{20}{12} = \boxed{0.16}$$

(ii) let B = be the event at least one egg is bad is selected.

$$n(B) = \binom{2}{1} \binom{10}{1} + \binom{2}{2} \binom{10}{2}$$

$$= 2 \times 10 + 1 \times 45 = 20 + 45 = 65$$

$$P(B) = \frac{n(B)}{n(S)} = \frac{65}{12} = \boxed{0.58}$$

Q No # 3

The following are the score made by three batsmen A, B & C in a series of 10 innings.

A =	12	15	6	73	7	10(30)	199	36	84	29
B =	47	12	76	48	4	10(30)	37	48	13	3
C =	15	23	52	4	24	10(30)	74	52	13	4

- (a) Find the range of batsmen A, B & C ?
- (b) Who is more consistent player ?
- (c) Compare A with B, B with A & A with C ?

Solution:

	A	B	C
	12	47	15
	15	12	23
	6	76	52
	73	48	4
	7	24	24
(10)	30	30	30
	199	37	74
	36	48	52
	84	13	13
	29	3	4

So:

Range = $X_m - X_o$

$$\begin{aligned} \text{(i)} \Rightarrow \text{Range of A} &= X_m - X_o \\ &= 199 - 6 \\ &= \boxed{193} \end{aligned}$$

$$\begin{aligned} \text{(ii)} \text{ Range of B} &= X_m - X_o \\ &= (10) 30 - 3 \\ &= \boxed{27} \end{aligned}$$

$$\begin{aligned} \text{(iii)} \text{ Range of C} &= X_m - X_o \\ &= 30 - 4 \\ &= \boxed{26} \end{aligned}$$

Batsman A		Batsman B		Batsman C	
X	X ²	Y	Y ²	Z	Z ²
12	144	47	2209	15	225
15	225	12	144	23	529
6	36	76	5776	52	2704
73	5329	48	2304	4	16
7	49	4	16	24	576
(10) 30	900	30	900	30	900
199	39601	37	1369	74	5476
36	1296	48	2304	52	2704
84	7056	13	169	13	169
29	841	3	9	4	16
$\Sigma X = 491$	$\Sigma X^2 = 55477$	$\Sigma Y = 318$	$\Sigma Y^2 = 15200$	$\Sigma Z = 291$	$\Sigma Z^2 = 13315$

P.T.O

$$\Rightarrow S_z = \sqrt{\frac{\sum z^2}{n} - \left(\frac{\sum z}{n}\right)^2}$$

Put value.

$$= \sqrt{\frac{13315}{10} - \left(\frac{29.1}{10}\right)^2}$$

$$S_z = 36.37$$

$$\Rightarrow C.V = \frac{S_z}{\bar{z}}$$

$$= \frac{36.37}{29.1}$$

$$C.V = 124.98\%$$

\Rightarrow Bestman **A** is more consistent as its value of coefficient of variance is smallest.

(i) \Rightarrow Compare "A" with "B".
 \Rightarrow B is consistent:

(ii) \Rightarrow Compare "B" with "A"
 \Rightarrow B is consistent

(iii) \Rightarrow Compare 'A' with 'C':
 \Rightarrow A is more consistent: