

(1)

Q1 Answer. (A)

X	X	X <sup>2</sup>	X <sup>2</sup>	XY
3	25	9	625	75
4	24	16	576	96
5	20	25	400	100
6	20	36	400	120
7	19	49	361	133
8	17	64	289	136
9	16	81	256	144
10	13	100	109	130
11	10	121	100	110
12	8	144	64	96
<hr/>	<hr/>	<hr/>	<hr/>	<hr/>
75	172	645	3246	1140

$$N = 10, \sum X = 75, \sum Y = 172$$

$$\sum X^2 = 645$$

$$\sum Y^2 = 3246, \sum XY = 1140$$

Substater in the competing  
from a given gives

$$R = \frac{\sum XY - \left\{ \left( \sum X \right) \left( \sum Y \right) \right\} / N}{\dots}$$

(2)

$$EX \left[ \left( \sum x^2 - \frac{(\sum x)^2}{N} \right) \left( \sum y^2 - \frac{(\sum y)^2}{N} \right) \right]$$

$$= 1140 - \frac{(75)(172)}{10}$$

$$\left[ \left( 645 - \frac{(75)^2}{10} \right) \left( 3246 - \frac{(172)^2}{10} \right) \right]$$

$$= 1140 - 1290$$

$$\left[ \left( 645 - 562.5 \right) \left( 3246 - 2958 \right) \right]$$

$$= \frac{-150}{(82.5)(2876)}$$

$$= \frac{-150}{23727}$$

$$= -0.00632$$

Ans

(3)

### Q1 part (B)

Determine the equation of the least  
regression line of  $y$  on  $x$  and  $x$  on  $y$

$x$	$y$	$x^2$	$y^2$	$xy$
20	5	400	25	100
11	15	121	225	165
15	14	225	196	210
10	17	100	289	170
17	8	289	64	136
18	9	324	81	162
21	12	441	144	252
25	18	<del>625</del>	<del>324</del>	<del>450</del>
28	18	784	324	504
<u>165</u>	<u>124</u>	<u>3209</u>	<u>1604</u>	<u>2099</u>

Regression line  $y$  on  $x$

(4)

$$B = \frac{n\sum xy - \sum x \sum y}{n\sum x^2 - (\sum x)^2}$$

$$B = \frac{9(2099) - (165)(124)}{9(3309) - (665)^2}$$

$$B = \frac{18891 - 20460}{29781 - 27225}$$

$$B = \frac{1569}{2556}$$

$$b = -0.6$$

$$a = \frac{\sum y - b\sum x}{n}$$

$$a = \frac{124 - (-0.6)(165)}{9}$$

$$= \frac{124 - (-99)}{9}$$

①

Q2 part (B)

$$x = 20, 11, 15, 15, 28 = 99$$

$$y = 5, 15, 9, 13, 16 = 58$$

~~x = 20 11 15 10 10 17 18 21 25 28~~

20 11 15 10 10 17 18 21 25 28  
5 15 14 14 17 17 8 9 12 18

y	x	xy	y <sup>2</sup>
5	20	100	400
15	11	165	121
14	15	210	225
17	10	170	100
8	17	136	289
9	18	182	324
12	25	252	441
<del>18</del>	28	504	625
18	28	504	784
<hr/>		<hr/>	<hr/>
114	165	2099	3,30

$$b = \frac{n \sum xy - \sum x \sum y}{n \sum x^2 - (\sum x)^2}$$

(2)

$$b = \frac{9 \times 2,079 - 165 \times 114}{9 \times 3309 - (165)^2}$$

$$b = \frac{81}{2556} \Rightarrow 0.0316$$

$$\bar{x} = \frac{\sum x}{n} = \frac{165}{9} = 18.33$$

$$\bar{y} = \frac{\sum y}{n} = \frac{114}{9} = 12.66$$

$$a = \bar{y} - b\bar{x}$$

$$a = 12.66 - 0.0316 \times 18.33$$

$$a = 12.66 - 0.579$$

$$a = 12.081$$

The estimated regression model.

$$\hat{y} = a + bx$$

$$y = 12.08 + 0.0316x$$

Prediction of  $y$  when  $x =$

③

prediction of  $y$  when  $x =$

$$20 + 11 + 15 + 25 + 28 = 99$$

$$\hat{y} = 12081 + 0 - 0316(99)$$

$$\hat{y} = 12081 - 3128$$

$$y = 15209$$

(5)

$$= \frac{124 - (-99)}{9}$$

$$a = 24.7$$

hence the regression line -

is given by

$$\underline{y^{\wedge} = a + bx}$$

$$= \underline{\hat{y} = 24.7 - 0.6x}$$

Regression line X on Y

$$b = \frac{n \sum xy - \sum x \sum y}{n \sum y^2 - (\sum y)^2}$$

$$b = \frac{9(2099) - (165)(124)}{9(1604) - (124)^2}$$



Ans part (A)

(6)

$$b = \frac{18891 - 20460}{9}$$

$$= \frac{14436 - 15376}{9}$$

$$b = \frac{-940}{9}$$

$$= -104.44$$

$$b = -104.44$$

$$a = \frac{539 - 13}{9}$$

N

$$= \frac{165 - (104.44)(124)}{9}$$

$$a = \frac{165 - 12950.56}{9}$$

$$a = \frac{-12785.56}{9}$$

$$a = -1420.62$$

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hence the regression  
line is given.

$$\hat{x} = 9.1 + by$$

$$(\hat{x} = -5.1 + 1.7y)$$

① No 1. Part (B)

(B) Find the predicted value

of  $y$  for  $x = 20, 11, 15, 25, 28$

and  $x$  for  $y = 5, 15, 9, 12, 16$

$$\hat{y} = 24 - 7 - 0 - 6x$$

$$\hat{x} = -5.1 + 1.7y$$

$x$	$y$	$\hat{y}$	$e$
		$\hat{y} = 24.7 - 0.06x$	$\bar{e} = -5.143$
11	15	12.7	3.4
15	9	18.1	-20.4
25	9	15.7	-10.2
28	12	9.7	15.2
	16	7.5	22.1
	18		25

This is predicted value

(H)

Q:03 Ans part (H)

(Give Data)

2	6	1	5	4	3	3	8	10	1
4	3	3	0	5	2	1	4	10	3
5	3	3	0	3	3	2	2	7	4
1	4	2	4	4	4	6	8	10	7
7	5	6	5	3	2	3	9	2	2

Uncompressed frequency distribution -

No	Tally mark	frequency	cumulation
0	I	1	1
1	IIII	4	5
2	IIIIII	8	13
3	IIIIIIII	11	24
4	IIIIIIII	8	32
5	IIII	5	37
6	IIII	4	41
7	III	3	44
8	II	2	46
9	I	1	47
10	III	3	50

(2)

Q3 Ans part (13)

Given Information of children born to 50 women -

2	6	1	5	1	3	3	8	10	1
	<del>3</del>								
4	3	3	0	5	7	1	4	10	3
5	3	3	6	3	3	2	2	7	4
1	4	2	4	4	4	6	8	10	7
7	5	6	5	3	2	3	9	2	2

Ground frequency Distribution

for given data -  
 $N = 50$

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$$\text{Range} = X_m - X_0$$

$$R = 10 - 1 = \boxed{9}$$

$$K = 1 + 3.3 \log N$$

$$= 1 + 3.3 \log (50)$$

$$= 1 + 3.3 (1.698)$$

$$= 1 + 5.606$$

$$K = 6.606 = \boxed{6}$$

$$H = \text{class interval} = \frac{\text{Range}}{K}$$

$$h = \frac{9}{6} = 1.5 = \boxed{2}$$

we find out the information  
frame data -

$$N = 50, R = 9, K = 6,$$

$$H = 2$$

(4)

Classes	Frequency	Class boundaries	Midpoint
0-1	5	-0.5-1.5	1
2-3	19	1.5-3.5	2.5
4-5	13	3.5-5.5	4.5
6-7	7	5.5-7.5	6.5
8-9	3	7.5-9.5	8.5
10-11	3	10.5-11.5	11

Total 50

Frequency	R, frequency %	C.F	R.C.F
5/50	$5/50 \times 100 = 10$	5	$5/50 = 0.1$
19/50	$19/50 \times 100 = 38$	24	$24/50 = 0.48$
13/50	$13/50 \times 100 = 26$	37	$37/50 = 0.74$
7/50	$7/50 \times 100 = 14$	44	$44/50 = 0.88$
3/50	$3/50 \times 100 = 6$	47	$47/50 = 0.94$
3/50	$3/50 \times 100 = 6$	50	$50/50 = 1.0$

part (B) Q No 3 complete.

①

$\Phi 2 = \text{part A}$

$\Rightarrow$  A fair coin is tossed 5 times -  
Find the probabilities of obtaining  
various number of head -

Let's regard the tossing of  
a coin as an experiment.

Then we observed that -

(1)

Each toss of coin has two  
possible outcome -

(2) The probability of head  
(Success) is  $p = \frac{1}{2}$  and  
Remain the same for successive  
tosses -

(3) The successive tosses of  
the coin are independent.

(4) The coin is tossed 5 times.

Therefore the R.V  $X$  which  
denote the number of head  
(Successes)

has a binomial probability



(2)

distribution - with  $p = \frac{1}{2}$   
and  $n = 5$  the possible values  
of  $X$  are 0, 1, 2, 3, 4 and  
5 hence -

$$P(\text{no head}) = P(X=0) = \binom{5}{0} \left(\frac{1}{2}\right)^0 \left(\frac{1}{2}\right)^5$$
$$= 1 \times \left(\frac{1}{2}\right)^5 = \frac{1}{32}$$

$$P(1 \text{ head}) = P(X=1) = \binom{5}{1} \left(\frac{1}{2}\right)^1 \left(\frac{1}{2}\right)^{5-1}$$
$$= 5 \times \left(\frac{1}{2}\right)^5 = \frac{5}{32}$$

$$P(2 \text{ head}) = P(X=2) = \binom{5}{2} \left(\frac{1}{2}\right)^2 \left(\frac{1}{2}\right)^{5-2}$$
$$= 10 \times \left(\frac{1}{2}\right)^5 = \frac{10}{32}$$

$$P(3 \text{ head}) = P(X=3) = \binom{5}{3} \left(\frac{1}{2}\right)^3 \left(\frac{1}{2}\right)^{5-3}$$
$$= 10 \times \left(\frac{1}{2}\right)^5 = \frac{10}{32}$$

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$$P(4 \text{ head}) = P(X=4) = \binom{5}{4} \left(\frac{1}{2}\right)^4$$

$$\left(\frac{1}{2}\right)^5 = 5 \times \left(\frac{1}{2}\right)^4 = \frac{5}{32}, \text{ and}$$

$$P(\text{heads}) = P(X=5) = \binom{5}{5} \left(\frac{1}{2}\right)^5$$

$$\left(\frac{1}{2}\right)^0 = 1 \times \left(\frac{1}{2}\right)^5 = \frac{1}{32}$$

These probability can also be obtain by expanding the Binomial  $\left(\frac{1}{2} + \frac{1}{2}\right)^5$ .

The Binomial P.D for a number of head obtained in 5 tosses of fair coin is

X	0	1	2	3	4	5
f(x)	$\frac{1}{32}$	$\frac{5}{32}$	$\frac{10}{32}$	$\frac{10}{32}$	$\frac{5}{32}$	$\frac{1}{32}$

(1)

Q2 part (B)

Solution here:

we have the Binomial  
probability with wide

$$n = 10$$

$$p = \frac{2}{3}$$

$$q = 1 - p$$

$$q = 1 - \frac{2}{3}$$

$$q = \frac{1}{3}$$

let  $x$  denote the  
number of noun by  
14 then -

$$1) P(x > 4) = 1 - P(x \leq 4)$$

$$= 1 - \sum_{x=0}^4 \binom{10}{x} \left(\frac{2}{3}\right)^x \left(\frac{1}{3}\right)^{10-x}$$

$$= 1 - \left\{ \left(\frac{1}{3}\right)^{10} + 10 \left(\frac{2}{3}\right)^1 \right\}$$

$$\binom{10}{3} \left(\frac{2}{3}\right)^7 \left(\frac{1}{3}\right) + 45 \binom{10}{2} \left(\frac{2}{3}\right)^6 \left(\frac{1}{3}\right)^2 + 120 \binom{10}{2} \left(\frac{2}{3}\right)^5 \left(\frac{1}{3}\right)^3$$

$$= 1 - \frac{1}{59049} (1 + 10 + 130 + 960)$$

$$= 0.9977$$

$$P(X \geq 4) = 0.9803$$

$$(ii) P(X=4) = \binom{10}{4} \left(\frac{2}{3}\right)^4 \left(\frac{1}{3}\right)^6$$

$$= 210 \left(\frac{16}{81} \times \frac{1}{729}\right)$$

$$= \frac{3360}{59049}$$

$$P(X=4) = 0.056$$

(iii)  $P(X=11) = 0$  because  $X$   
can take only value

0, 1, 2, 3, ... 10

(3)

6 or more games

$$P(X=6) = \sum_{x=6}^{10} \binom{10}{x} \left(\frac{2}{3}\right)^x \left(\frac{1}{3}\right)^{10-x}$$

$$= \binom{10}{6} \left(\frac{2}{3}\right)^6 \left(\frac{1}{3}\right)^4 + \binom{10}{7} \left(\frac{2}{3}\right)^7 \left(\frac{1}{3}\right)^3 +$$

$$+ \binom{10}{8} \left(\frac{2}{3}\right)^8 \left(\frac{1}{3}\right)^2 + \binom{10}{9} \left(\frac{2}{3}\right)^9 \left(\frac{1}{3}\right)^1$$

$$+ \binom{10}{10} \left(\frac{2}{3}\right)^{10} \left(\frac{1}{3}\right)^0$$

$$P = 0.228 + 0.261 + 0.196$$

$$+ 0.087 + 0.018$$

$$P = (X \geq 6) = 0.79$$

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