



**Summers**

**Course Code:** EEE342                      **Course Title:** Electrical Machines  
**Prerequisite:** Circuit Analysis                      **Instructor:** Engr. Sanaullah Ahmad  
**Module:**                      **Program:** BEE **Total Marks:** 30                      **Time Allowed:** \_\_\_\_\_

**Rafaqat ID 14107**

Note: 1) Attempt all questions.

2) Calculators borrowing/exchange is prohibited.

(b) A square ferromagnetic core has a mean path length of 55cm and a cross-sectional area of 150cm<sup>2</sup>. A 200 turn coil of wire is wrapped around one leg of the core. The core is made of a material having magnetization intensity (H) 115 A. turns/m. Find: Marks 10

- a. How much current is required to produce 0.012 Wb of flux in the core?
- b. What is the core's relative permeability at that current level?  
( $4\pi \times 10^{-7} \text{H/m}$ )
- c. What is its reluctance?

CLO 2

Q2 (a) Derive Voltage and Impedance relationship with turn ratio for an ideal transformer? Marks 10

CLO 1

Q3 (a) Define power factor? Differentiate between Real, Apparent and reactive powers? Marks 10

CLO 1

(4)

①

Name

Rafiqat Ullah Khan

ID

14107

Question # 01

Given Data:-

$$\text{Core length} = 55 \text{ cm} = 0.55 \text{ m}$$

$$\text{Cross Area} = 150 \text{ cm}^2 = 0.015 \text{ m}^2$$

$$\text{intensity} = H = 115 \text{ A turns/m}$$

$\Phi$

$$= 0.012 \text{ webers}$$

$N$

$$= 200 \text{ turns}$$

Required:

$$I = ?$$

$$\mu_r = ?$$

$$R = ?$$

First we will find Magnetic field =  $B$

②

Solutions:

$$\Phi = B \cdot A$$

$$B = \frac{\Phi}{A}$$

$$= \frac{0.012}{0.015}$$

$$B = 0.8 \text{ Tesla}$$

$$B = \mu H$$

$$\mu = \frac{B}{H}$$

$$= \frac{0.8}{115}$$

$$\mu = 0.0069 \text{ H/m}$$

Now

$$\mu_r = \frac{0.0069}{3.14 \times 4 \times 10^{-7}}$$

$$\therefore \mu_r = \frac{\mu}{\mu_0}$$

$$\mu_0 = 4\pi \times 10^{-7}$$

$$\mu_r = 5540$$

③

$$T = HL$$

$$= 115 \times 0.55$$

$$T = 63.25 \text{ A-turns}$$

$$T = R\phi$$

$$R = \frac{T}{\phi}$$

$$= \frac{63.25}{0.012}$$

$$R = 5270 \text{ A-turns/Wb}$$

Now find Current

$$I = \frac{F}{N}$$

$$\therefore T = F$$

$$= \frac{63.25}{200}$$

$$I = 0.316 \text{ amps}$$

(4)

Question # 02

Answer: Voltage and Impedance Relationship:

Since

$$\frac{N_p}{N_s} = \frac{V_p}{V_s} = \frac{I_s}{I_p}$$

$$\alpha = \frac{N_p}{N_s}$$

where impedance =  $Z$

$$Z = R + jX$$

$\therefore R = \text{Resistance}$   
 $jX = \text{Reactance}$

$$V = IR$$

$$V = IZ$$

$$R = Z$$

As

$$Z_p = \frac{V_p}{I_p}$$

and

$$Z_s = \frac{V_s}{I_s}$$

$$\alpha = \frac{N_p}{N_s} = \frac{V_p}{V_s}$$

⑤

$$\alpha = \frac{V_P}{V_S}$$

$$\alpha V_S = V_P \quad \text{--- (1)}$$

$$\alpha = \frac{I_S}{I_P}$$

$$\frac{1}{\alpha} = \frac{I_P}{I_S}$$

$$I_P = \frac{I_S}{\alpha} \quad \text{--- (2)}$$

$$Z_P = \frac{V_P}{I_P} \quad \text{--- (A)}$$

Put eq (1) and (2) in (A)

$$Z_P = \frac{\alpha V_S}{I_S/\alpha}$$

$$= \alpha^2 \frac{V_S}{I_S}$$

$$Z_P = \alpha^2 \frac{V_S}{I_S}$$

(6)

$$Z_p = \alpha^2 Z_s$$

$$\therefore Z_s = \frac{V_s}{I_s}$$

$$\frac{Z_p}{Z_s} = \alpha^2$$

$$\frac{Z_p}{Z_s} = \left( \frac{N_p}{N_s} \right)^2$$

$$\therefore \alpha = \frac{N_p}{N_s}$$

Taking Square on B/S

$$\sqrt{\frac{Z_p}{Z_s}} = \sqrt{\left( \frac{N_p}{N_s} \right)^2}$$

$$\frac{N_p}{N_s} = \sqrt{\frac{Z_p}{Z_s}}$$

turn ratio for impedance in Ideal transformer.

7

For Voltage:

EMF equation of Ideal Transformer

$$e_p = -N_p \frac{d\phi}{dt}$$

$$\therefore V_m = V_m \sin \omega t$$

$$\phi_m = \phi_m \sin \omega t$$

$$e_p = -N_p \frac{d(\phi_m \sin \omega t)}{dt}$$

$$= -N_p \omega \cos \omega t \phi_m + \sin \omega t$$

$$= -2\pi f N_p \cos \omega t \phi_m + \sin \omega t$$

$$= -2\pi f N_p \sin(\omega t - 90^\circ) \phi_m + \sin \omega t$$

$$= 2\pi f N_p \sin(90^\circ - \omega t) + \sin \omega t$$

$$e_p = 2\pi f N_p (1) \phi_m$$

max value

$$e_p = 2\pi f N_p \phi_m$$



⑤

$$\frac{V_{\max}}{\sqrt{2}} = V_{\text{rms}}$$

$$e_{p_{\text{rms}}} = 4.44 f N_p \Phi_m$$

$$e_{s_{\text{rms}}} = 4.44 f N_s \Phi_m$$

$$\frac{e_{p_{\text{rms}}}}{e_{s_{\text{rms}}}} = \frac{4.44 f N_p \Phi_m}{4.44 f N_s \Phi_m}$$

$$\frac{e_p}{e_s} = \frac{N_p}{N_s}$$

Voltage Relationship of turn ratio for  
Ideal transformer.

9

Question#03

Answer:

Power factor:

Power factor is the ratio between actual Power and apparent power.

Differenciation B/w Real, apparent and Reactive power:

1- Real Power:

Also know as "Active power". Real

Power is the rate of producing, transforming or using electrical energy it is measured in Watts. and often expressed in kilowatts. (KW).

## 2- Apparent Power:

The product of the voltage in Volts and Current in amperes. It comprises both active and reactive Power. It is measured in Volt-ampers and also expressed in Kilowatt-amperes.

## 3- Reactive Power:

Reactive power is the power where the current is out of phase with the voltage and the "Volts x amps" doesn't do any real work. Current that charges a capacitor, for example or current that creates the magnetic field around a coil for another.

