

**Electrical Transmission System Sessional Assignment**

**Total Marks=20**

**Question No 1: A 3-phase, 50-Hz overhead transmission line 100 km long has the following constants:**

**Resistance/km/phase =  $0.1 \Omega$**

**Inductive reactance/km/phase =  $0.2 \Omega$**

**Capacitive Susceptance/km/phase =  $0.04 \times 10^{-4}$**

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**Determine (i) the sending end current (ii) sending end voltage (iii) sending end power factor and (iv) transmission efficiency when supplying a balanced load of 10,000 kW at 66 kV, p.f. 0.8 lagging. Use nominal T method.**

**Question No 2: A (medium) single phase transmission line 100 km long has the following constants:**

**Resistance/km =  $0.25 \Omega$  ; Reactance/km =  $0.8 \Omega$**

**Susceptance/km =  $14 \times 10^{-6}$  siemen; Receiving end line voltage = 66,000 V**

**Assuming that the total capacitance of the line is localised at the receiving end alone, determine**

**(i) The sending end current (ii) The sending end voltage (iii) Regulation and (iv) supply power factor. The line is delivering 15,000 kW at 0.8 power factor lagging.**

**Draw the phasor diagram to illustrate your calculations.**

### Question No 3: Describe Ferranti Effect, Why Ferranti effect occurs? Detail

explanation of the Ferranti effect by considering a nominal pi ( $\pi$ ) model. How to reduce Ferranti effect.

#### SOLUTION:1

$$\text{Total resistance/phase} = 0.1 \times 100 = 10$$

$$\Omega \text{Total reactance/phase. } X_L = 0.2 \times 100 = 20$$

$$\text{Capacitive susceptance, } Y = 0.04 \times 10^{-4} \times 100 = 4 \times 10^{-4} \text{ S}$$

$$\text{Receiving end voltage/phase, } V_R = 66,000 / \sqrt{3} = 38105 \text{ V}$$

$$\text{Load current, } I_R =$$

$$10,000 \times 10^3$$

,

$$\sqrt{3} \times 66 \times 10^3 \times 0.8$$

$$= 109 \text{ A}$$

$$\cos \phi_R = 0.8; \sin \phi_R = 0.6$$

$$\text{Impedance per phase, } Z = R + jX_L = 10 + j20$$

(i) Taking receiving end voltage as the reference phase

We have,

$$\text{Receiving end voltage, } V_R = V_R + j0 = 38,105 \text{ V}$$

$$\text{Load current, } I_R = I_R (\cos \phi_R - j \sin \phi_R) = 109 (0.8 - j0.6) = 87.2 - j65.4$$

$$\begin{aligned} \text{Voltage across C, } V_1 &= V_r + I_r Z/2 = 38,105 + (87.2 - j65.4)(5 + j10) \\ &= 38,105 + 436 + j872 - j327 + 654 = 39,195 + j545 \end{aligned}$$

Charging current,  $I_C = j Y \cdot 14 \times 10^{-4}$

$$(39,195 + j 545) - 0.218 + j 15.6$$

Sending end current,  $I_S = \frac{V_1}{Z} \div \frac{V_2}{Z} = (87.2 - j 65.4) + (0.218 + j 15.6)$

$$= 87.0 - j 49.8 = 100 \angle 29^\circ 47' \text{ A}$$

Sending end current = 100A

(ii) Sending end voltage,  $V_S = V_1 + I_S Z/2 = (39,195 + j 545) + (87.0 - j 49.8)$

$$(5 + j 10)$$

$$= 39,195 + j 545 + 434.9 + j 870 = 40128 + j 1170$$

$$= 40145 \angle 1^\circ 40' \text{ V}$$

Line value of sending end voltage

$$= 40145 \sqrt{3} = 69,533 \text{ V} = 69.53 \text{ KV}$$

(iii) Referring to phases =

$$\theta_1 = \text{angle between } V_r \text{ and } V_s = 1^\circ 40'$$

$$\theta_2 = \text{angle between } V_r \text{ and } I_s = 29^\circ 47'$$

$$\theta_S = \text{angle between } V_s \text{ and } I_s$$

$$= \theta_1 + \theta_2 = 1^\circ 40' + 29^\circ 47' = 31^\circ 27'$$

$$\text{Sending end power} = \cos \theta_s = \cos 31^\circ 27' = 0.853 \text{ lag}$$

(iv) Sending end power = 3  $V_s$

$$I_s \cos \theta_s = 3.40,145 \times 100 \times 0.853$$

$$= 10273105 \text{ W} = 10273.105 \text{ KW}$$

Power delivered = 10,000KW

∴ Transmission efficiency =

$$\frac{10,000}{10273.105}$$

$$10273.105$$

$$\times 100 = 97.34\%$$

### **SOLUTION 2**

$$\text{Total resistance, } R = 0.2 \times 100 = 25 \text{ ohms}$$

$$\text{Total reactance, } Xl$$

$$= 0.8 \times 100 = 80 \text{ ohms}$$

$$\text{Total susceptance, } Y = 14 \times 10^{-6} \times 100 - 14 \times 10^{-4} \text{ S}$$

$$\text{Receiving end voltage, } VR = 66,000 \text{V}$$

$$\therefore \text{ Load current } IR =$$

$$\frac{15000 \times 10^3}{66,000 \times 0.8}$$

$$= 284 \text{A}$$

$$\text{Cos}\theta_R = 0.8: \text{sin}\theta_R = 0.6$$

$$\text{Taking receiving end voltage as the reference phasor we have,}$$

$$VR = VR + j0 = 66,000 \text{V}$$

$$\text{Load current } IR = IR (\text{Cos}\theta_R - j \text{sin}\theta_R) = 284 (0.8 - j 0.6) = 227 - j170$$

$$\text{Capacitive current } Ic = jY \times VR = -j14 \times 10^{-4} \times 66000 = -j92$$

$$\text{(i) Sending end current, } IS = IR + Ic = (227 - j170 + j92)$$

$$= 227 - j78$$

$$\text{Magnitude of } IS = \sqrt{(227)^2 + (78)^2}$$

$$= 240 \text{A}$$

$$\text{(ii) Voltage drop } = ISZ = IS$$

$$(R + jXL)$$

$$= (227 - j78) (25 + j80)$$

$$= 5.675 + j1816 - j1950 + 6240$$

$$11,915 + j16210$$

$$\text{Sending end voltage, } VS = VR + IS Z = 66000 + 11915 + j16210$$

$$= 77915 + j16210$$

$$\text{Magnitude of } VS = \sqrt{(77915)^2}$$

$$+ (16210)^2$$

$$\sqrt{\quad} = 79583 \text{ V}$$

$$\text{(III) \% voltage regulation} = \frac{VS - VR}{VR}$$

$$\times 100 =$$

$$\frac{79583 - 66000}{66000}$$

$$\times 100 = 20.58\%$$

$$\text{(IV) referring to exp (i), phase angle between } VR \text{ and } IR \text{ is :}$$

$$\theta_1 = \tan^{-1}$$

$$\frac{-78}{227} = \tan^{-1}(-0.3436) = -18.96^\circ$$

$$\text{Referring to exp (ii), phase angle between } VR \text{ and } VS$$

$$\text{is;}$$

$$\theta_1 = \tan^{-1}$$

$$\frac{16210}{77915} = \tan^{-1}(0.236) = 11.50^\circ$$

$$\text{is;}$$

$$\theta_1 = \tan^{-1}$$

$$\frac{16210}{77915}$$

$$= \tan^{-1}$$

$$(0.236) = 11.50^\circ$$

$$\text{(0.236)} = 11.50^\circ$$

Supply power factor angle,  $\phi_S = 18.96^\circ + 11.50^\circ = 30.46^\circ$

Supply p.f =  $\cos\phi_S$

-  $\cos 30.46^\circ = 0.86$ lag

### **ANSWER NO 3**

#### **Ferranti Effect:**

**Definition:** The effect in which the voltage at the receiving end of the transmission

line is more than the sending voltage is known as the Ferranti effect. Such type of effect mainly

occurs because of light load or open circuit at the receiving end.

#### **Ferranti effect occurs:**

Capacitance and inductance are the main parameters of the lines having a length 240km or above.

On such transmission lines, the capacitance is not concentrated at some definite points. It is

distributed uniformly along the whole length of the line.

When the voltage is applied at the sending end, the current drawn by the capacitance of the line is

more than current associated with the load. Thus, at no load or light load, the voltage at the

receiving end is quite large as compared to the constant voltage at the sending end

#### **Ferranti effect by considering a nominal pi ( $\pi$ ) model:**

Let us consider the long transmission line in which OE represents the receiving end voltage; OH represents the current through the capacitor at the receiving end. The

phasor FE represents the voltage drop across the resistance R. The voltage drop across the X

(inductance). The phasor OG represents the sending end voltage under a no-load condition.

It is seen from phasor diagram that  $OE > OG$ . In other words, the voltage at the receiving end is

greater than the voltage at the sending end when the line is at no load.

For a small Pi ( $\pi$ ) replica

$$V_s = (1 + ZY/2)V_r + ZI_r$$

Where,  $I_r = 0$  at no load condition

$$V_s = (1 + ZY/2)V_r + Z(0)$$

$$= (1 + ZY/2)V_r$$

$$V_s - V_r = (1 + ZY/2)V_r - V_r$$

$$V_s - V_r = V_r [1 + ZY/2 - 1]$$

$$V_s - V_r = (ZY/2)V_r$$

$$Z = (r + j\omega l)S, \text{ and } Y = (j\omega c)S$$

If the transmission line's resistance is unnoticed

$$V_s - V_r = (ZY/2)V_r$$

Substitute  $Z = (r + j\omega l)S$ , and  $Y = (j\omega c)S$  in the above  $V_s$

$$V_s - V_r = \frac{1}{2} (j\omega l S) (j\omega c S) V_r$$

$$V_s - V_r = -\frac{1}{2} (\omega^2 L C) l c V_r$$

For the lines of overhead,  $1/\sqrt{LC} = 3 \times 10^8 \text{ m/s}$  (velocity of electromagnetic wave transmission on

the broadcast lines).  $1/\sqrt{LC} = 3 \times 10^8 \text{ m/s}$

$$\sqrt{LC} = 1/3 \times 10^8$$

$$LC = 1/(3 \times 10^8)^2$$

$$V_S - V_R = -\frac{1}{2} W^2 S^2 \cdot (1/(3 \times 10^8)^2) V_r$$

$$W = 2\pi f$$

$$V_S - V_R = -((4\pi^2/18) \cdot 10^{-16}) f^2 S^2 V_r$$

The above eq illustrates that  $(V_S - V_r)$  is negative, that means  $V_r$  is greater than  $V_S$ . This is also

illustrated that this effect will also determine by the electrical period of the transmission lines and

frequency.

Generally, for each line

$$V_s = AV_r + BL_r$$

On no load state,

$$I_r = 0, V_r = V_{rnl}$$

$$V_s = AV_{rnl}$$

$$|V_{rnl}| = |V_s|/|A|$$

### How to Reduce Ferranti Effect In Transmission Line:

Electrical machines work on specific electrical energy. If the voltage is far above the ground at the

consumer end their device get damaged, and the windings of the device also burn due to high

electrical energy.

Ferranti effect on extensive transmission lines at no-load status, then the voltage will increase at the

collecting end. This can be restricted by keeping the shunt-reactors next to the collecting end of the



**transmission lines.**

**This reactor allied between the lines along with neutral to give back the capacitive current as of**

**transmission lines. As this outcome happens in lengthy transmission lines, these reactors pay off**

**the transmission lines & thus the voltage is regulated within the set limits.**