

Department of Electrical Engineering

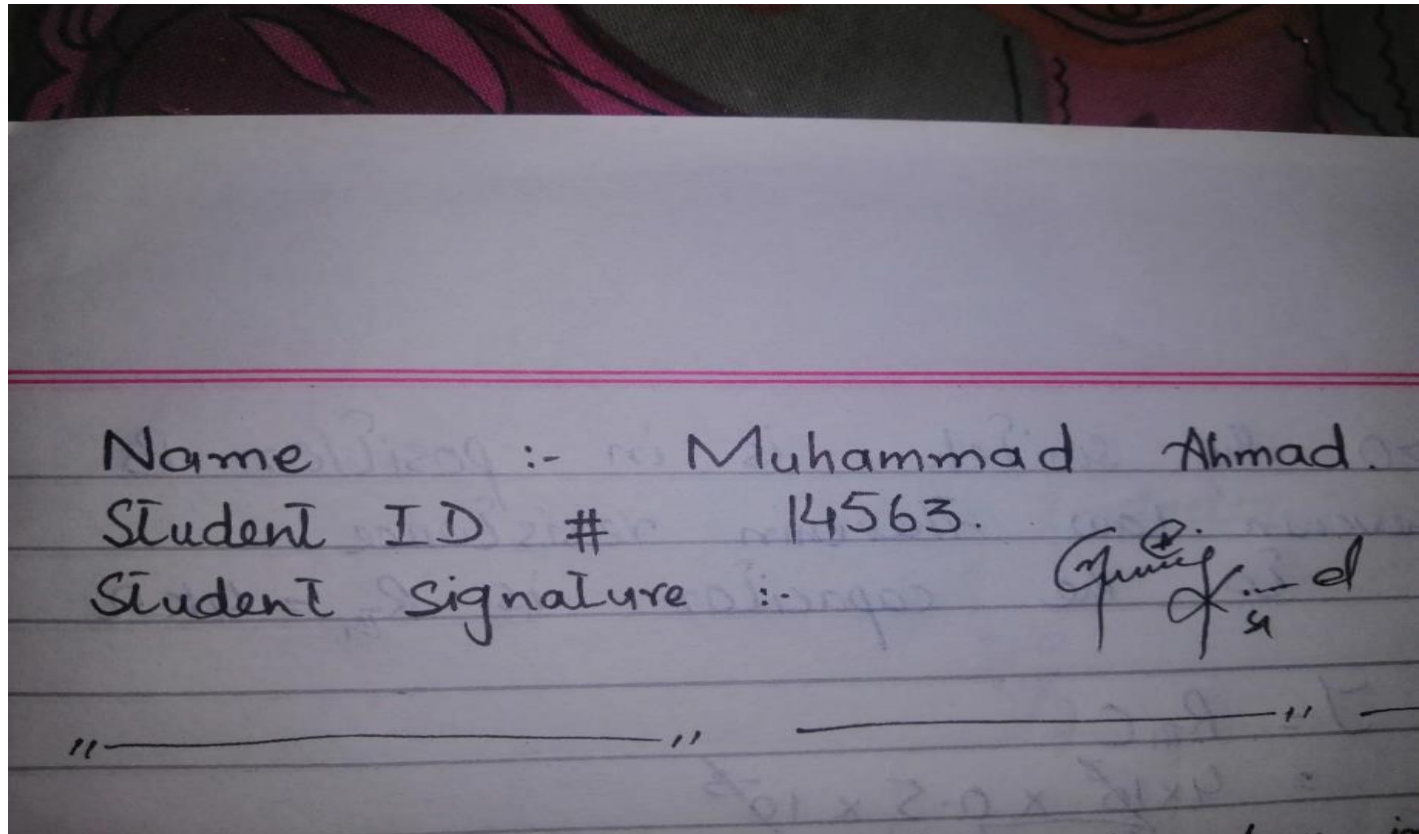
Course Title: Electrical Network Analysis

Module: 4th semester

Student Detail

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QNo1. Assume that a 2000-kW Turbine-generator of 0.85 power factor operates at the rated load. An additional load of 300 kW at 0.8 power factor is added. What KVAR of capacitor is required to operate the turbine generator but keep it from being overload?

Solution :-

Given :-

$$P_1 = 2000 \text{ kW}$$

$$P_2 = 300 \text{ kW}$$

$$\text{P.f.} = 0.85$$

$$\text{P.f.} = 0.8$$

Original Load :-

$$P_1 = 2000 \text{ kW}$$

$$\text{P.f.} = 0.85$$

$$\cos \theta = 0.85$$

$$\theta = \cos^{-1}(0.85)$$

$$S_1 = \frac{P_1}{\cos \theta_1}$$

$$= \frac{2000}{0.85}$$

$$= 2352.94 \text{ KVA}$$

$$Q_1 = S_1 \sin \theta_1$$

$$Q_1 = (2352.94) \sin(31.79)$$

$$= \underline{1239.54 \text{ KVAR}}$$

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Additional Load:-

$$P_2 = 300 \text{ KW.}$$

$$\cos \theta_2 = 0.8$$

$$\theta_2 = \cos^{-1}(0.8)$$

$$\theta_2 = \underline{\underline{36.87^\circ}}$$

$$S_2 = \frac{P_2}{\cos \theta_2}$$
$$= \frac{300}{0.8}$$

$$S_2 = 375 \text{ KVA.}$$

$$Q_2 = S_2 \sin \theta_2$$
$$= (375) \sin(36.87)$$
$$= \underline{\underline{225.00 \text{ KVAR.}}}$$

Total Load:-

$$S = S_1 + S_2$$

$$S = (P_1 + P_2) + (Q_1 + Q_2)j$$

$$S = P + jQ$$

$$P = 2000 + 300$$

$$P = 2300 \text{ KW.}$$

$$Q = 1239.5 + 225$$

$$Q = 1464.5 \text{ KVAR.}$$

Now the minimum P.F. for 2300 KW load
& not exceeding the KVA rating

$$\cos \theta = \frac{P}{S_1}$$

$$\cos \theta = \frac{2300 \times 10^3}{2352.94 \times 10^3}$$

$$\cos \theta = 0.9778$$

$$\theta = 12.177^\circ$$

the maximum load KVAR

$$Q_{\max} = S_1 \sin \theta$$

$$Q_{\max} = (2352.94) \sin(12.177^\circ)$$

$$Q_{\max} = 496.313 \text{ KVAR.}$$

The capacitor must supply the difference
b/w Total loads
KVAR and the permissible

$$\begin{aligned} \text{Thus } Q_c &= Q - Q_{\max} \\ &= 1464.5 - 496.313 \\ &= \boxed{968.187 \text{ KVAR}} \end{aligned}$$

QNO2:- A balanced abc, sequence one line voltage of a balanced Y-connection source is $V_{AB} = 180 \angle -20^\circ \text{ V}$. If the source is connected to a Δ -connected load of $20 \angle 40^\circ \Omega$. Find the phase and line current.

Solution :-

line Voltage $V_{AB} = 180 \angle -20^\circ \text{V}$
 $Z_{\Delta} = 20 \angle 40^\circ \Omega$

Formula

$$V_L = \sqrt{3} V_p \angle 30^\circ \Rightarrow V_p = \frac{V_L}{\sqrt{3} \angle 30^\circ}$$

Phase Voltage :-

$$V_{an} = \frac{180 \angle -20^\circ \cdot \angle -30^\circ}{\sqrt{3}}$$

$$= \frac{103.9 \angle -50^\circ \text{V}}{3}$$

$$Z_{y\phi} = \frac{Z_{\Delta}}{3}$$

$$= \frac{20 \angle 40^\circ}{3}$$

$$= \underline{6.67 \angle 40^\circ \Omega}$$

Line Current

$$I_a = \frac{V_{an}}{Z_{y\phi}}$$

$$= \frac{103.9 \angle -50^\circ}{6.67 \angle 40^\circ}$$

$$I_a = 15.57 \angle -90^\circ \text{A}$$

$$I_b = I_a \angle -120^\circ = 15.57 \angle 150^\circ \text{A}$$

$$I_c = I_a \angle +120^\circ = 15.57 \angle 30^\circ$$

Phase Current

$$\begin{aligned} \underline{I}_{AB} &= \frac{15.57 \angle -90^\circ}{\sqrt{3}} \cdot \angle 30^\circ \\ &= \underline{9 \angle -60^\circ \text{ A}} \end{aligned}$$

$$\begin{aligned} \underline{I}_{BC} &= \underline{I}_{AB} \angle -120^\circ \\ &= \underline{9 \angle -180^\circ} \end{aligned}$$

$$\begin{aligned} \underline{I}_{AC} &= \underline{I}_{AB} \angle +120^\circ \\ &= \underline{9 \angle 60^\circ \text{ A}} \end{aligned}$$

Q No 3: Consider a load with value of $V_{rms} = 110 \angle 85^\circ \text{ V}$, $I_{rms} = 0.4 \angle 15^\circ \text{ A}$. Calculate the following

Solution:

Given

$$V_{rms} = 110 \angle 85^\circ \text{ V}$$

$$I_{rms} = 0.4 \angle 15^\circ \text{ A}$$

① Complex power & Apparent power.

$$S = (V_{rms})(I_{rms})$$

$$S = (110 \angle 85^\circ)(0.4 \angle 15^\circ)$$

$$S = (110 \times 0.4) \angle (85^\circ - 15^\circ)$$

$$\underline{S = 44 \angle 70^\circ \text{ VA}}$$

The apparent power.

$$S = |S|$$

$$\underline{S = 44 \text{ VA}} \quad (5)$$

30

(b) find real and reactive Power.

$$S = 44 \angle 70^\circ$$

$$S = 44 [\cos(70^\circ) + j \sin(70^\circ)]$$

$$S = 44 [0.3420 + j0.939]$$

$$S = 15.05 + j41.35$$

Since

$$S = P + jQ$$

the real power is.

$$P = 15.05 \text{ W}$$

the reactive power

$$Q = 41.35 \text{ VAR}$$

value
 $\angle 15^\circ \text{ A}$

(c) the power factor and the load Impedance.

the power factor is.

$$\text{P.F} = \cos(70^\circ)$$

$$\therefore \text{P.F} = 0.342 \text{ (lagging)}$$

The power factor is lagging as the
the reactive power is ~~pos~~ positive.
the load Impedance.

$$Z = \frac{V}{I}$$

$$V = \sqrt{2} V_{\text{rms}}$$

$$I = \sqrt{2} I_{\text{rms}}$$

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$$Z = \frac{110\sqrt{2} \angle 85^\circ}{0.4\sqrt{2} \angle 15^\circ}$$

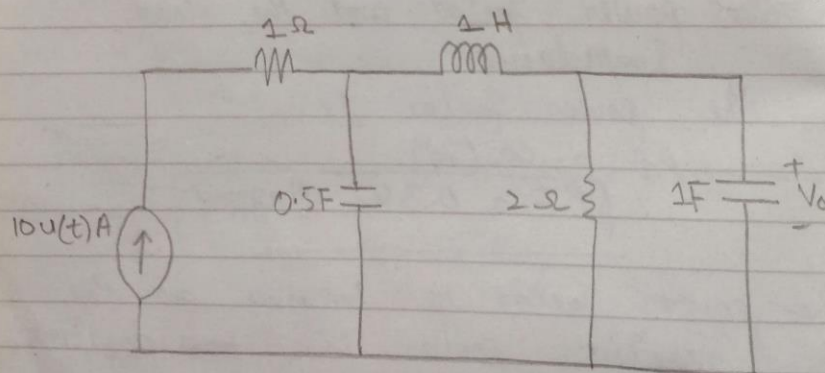
$$Z = 275 \angle 70^\circ \Omega$$

$$Z = 275 [\cos(70^\circ) + j \sin(70^\circ)]$$

$$= 275 [0.342 + j0.939]$$

$$Z = [94.05 + j258.25] \Omega \text{ Am}$$

Q No 4:- Apply Laplace Transform & Calculate the output $V_o(t)$ in the ckt fig



Solution

The Impedance inductor in s-domain is,

$$Z(s) = sL$$

$$\text{for } L = 1H, Z(s) = s.$$

(7)

The impedance capacitor in s-domain is,

$$Z(s) = \frac{1}{sC}$$

For

$$C = 0.5F$$

$$Z(s) = \frac{2}{s}$$

$$C = 1F, Z(s) = \frac{1}{s}$$

At Node 1,

$$\frac{10 - V_1}{s} = \frac{V_1 - V_0}{s} + \frac{s}{2} V_0$$

$$10 = (s+1)V_1 + \left(\frac{s^2}{2} - 1\right)V_0 \rightarrow (1)$$

At Node 2

$$\frac{V_1 - V_0}{s} = \frac{V_0}{2} + sV_0$$

$$V_1 = V_0 \left(\frac{s}{2} + s^2 + 1\right) \rightarrow (2)$$

Substituting (2) into (1) gives.

$$10 = (s+1) \left(\frac{s^2 + s}{2} + 1\right) V_0 + \left(\frac{s^2}{2} - 1\right) V_0$$

$$= s(s^2 + 2s + 1.5) V_0$$

$$V_0 = \frac{10}{s(s^2 + 2s + 1.5)}$$

$$= \frac{A}{s} + \frac{Bs + C}{s^2 + 2s + 1.5}$$

$$10 = A(s^2 + 2s + 1.5) + Bs^2 + Cs.$$

$$s^2: \quad 0 = A + B.$$

$$s: \quad 0 = 2A + C.$$

Constant

$$10 = 1.5A \rightarrow A = \frac{20}{3}$$

$$B = -\frac{20}{3}$$

$$C = -\frac{40}{3}$$

$$V_o = \frac{20}{3} \left[\frac{1}{s} - \frac{s+2}{s^2+2s+1.5} \right]$$

$$= \frac{20}{3} \left[\frac{1}{s} - \frac{s+1}{(s+1)^2 + 0.7071^2} - \frac{(1.414) \cdot 0.7071}{(s+1)^2 + 0.7071^2} \right]$$

Taking the inverse Laplace Transform

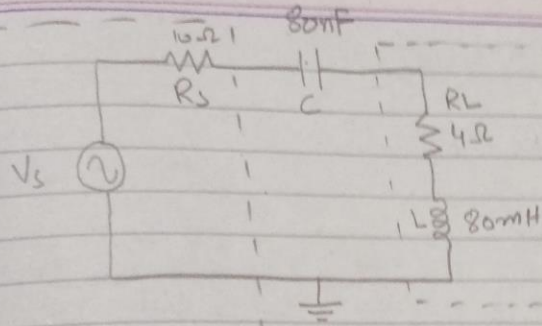
$$V_o(t) = \frac{20}{3} \left[1 - e^{-t} \cos(0.7071t) - 1.414e^{-t} \sin(0.7071t) \right] u(t) \text{ V}$$

Qnos:- A coupling capacitor of 80nF is used to block dc current

Solution:-

(a) At what frequency is maximum power transfer to the speaker.

Es.



The amplifier and the capacitor act as a source; hence the source impedance.

$$Z_s = R_s - jX_c$$

The speaker act as a load; hence load impedance.

$$Z_L = R_L + jX_L$$

The maximum power is transferred to the speaker or load when the load impedance is equal to the complex conjugate of thevenin impedance.

In the ckt, the thevenin's Impedance is equal to the source Impedance. Hence maximum power is transferred to the speaker when.

$$\frac{0.7071}{(s+1)+0.7071}$$

transform

$$e^t \sin 0.7071t$$

$u(t) \text{ V}$

80nF
dc

s max-
he speak.

$$Z_L = Z_S'$$

$$R_S = R_L$$

$$X_C = X_L$$

$$X_C = X_L \rightarrow \frac{1}{\omega C} = \omega L$$

$$\text{or } \omega = \frac{1}{\sqrt{LC}} = \frac{2\pi f}{\text{Angular Frequency}}$$

$$f = \frac{1}{2\pi\sqrt{LC}}$$

Substitute 80 nF For capacitor &
80 mH For Inductor (L)

$$f = \frac{1}{2(\pi)(\sqrt{(80 \times 10^{-3})(80 \times 10^{-9})})}$$

$$= \frac{1}{2(3.14)(80 \times 10^{-6})}$$

$$= \frac{1 \times 10^6}{502.4}$$

$$= \frac{1000000}{502.4}$$

$$= 1990.44$$

$$f = \boxed{1.990 \text{ KHz}}$$

(11)

$$(b) P = \frac{N_s^2}{R_s + R_L} I_s^2 R_L$$

$$P = \left(\frac{N_s}{R_s + R_L} \right)^2 R_L$$

$$P = \left(\frac{5}{10+4} \right)^2 4 = 0.5104 \text{ W.}$$

$$= 510 \text{ mW.}$$

Thus the power P , delivered to the speaker at the frequency $f = 1.99 \text{ kHz}$

is 510 mW

L.

Angular
Frequency

For ϵ