

Date: _____

NAME : M. TALHA

Semester : 2

Section : A

ID : 15784

$$Q. 9 \begin{vmatrix} 1 & 2 & 5 \\ 2 & 3 & 1 \\ 3 & 1 & 2 \end{vmatrix}$$

ID number = 5

$$A_{adj} = ?$$

$$\text{Solution } A_{11} = (-1)^{1+1} \begin{vmatrix} 3 & 1 \\ 1 & 2 \end{vmatrix} = (1) \begin{vmatrix} 3 & 1 \\ 1 & 2 \end{vmatrix} 6-1 = 5$$

$$A_{12} = (-1)^{1+2} \begin{vmatrix} 2 & 1 \\ 3 & 2 \end{vmatrix} = (-1) \begin{vmatrix} 2 & 1 \\ 3 & 1 \end{vmatrix} (-1)(4-3) = -1$$

$$A_{13} = (-1)^{1+3} \begin{vmatrix} 2 & 3 \\ 3 & 1 \end{vmatrix} = (1) (2-9) = -7$$

$$A_{21} = (-1)^{2+1} \begin{vmatrix} 2 & 5 \\ 1 & 2 \end{vmatrix} = (-1) (4-5) = +1$$

$$A_{22} = (-1)^{2+2} \begin{vmatrix} 1 & 5 \\ 3 & 2 \end{vmatrix} = (1) (2-15) = -13$$

$$A_{23} = (-1)^{2+3} \begin{vmatrix} 1 & 2 \\ 3 & 1 \end{vmatrix} = (-1) (1-6) = 5$$

$$A_{31} = (-1)^{3+1} \begin{vmatrix} 2 & 5 \\ 3 & 1 \end{vmatrix} = (1) (2-15) = -13$$

$$A_{32} = (-1)^{3+2} \begin{vmatrix} 1 & 5 \\ 2 & 1 \end{vmatrix} = (-1) (1-10) = +9$$

$$A_{33} = (-1)^{3+3} \begin{vmatrix} 1 & 2 \\ 2 & 3 \end{vmatrix} = (1) (3-4) = -1$$

Date: _____

Page 2

$$A \text{ cofactor} = \begin{bmatrix} a_{11} & a_{12} & a_{13} \\ a_{21} & a_{22} & a_{23} \\ a_{31} & a_{32} & a_{33} \end{bmatrix}$$

$$= \begin{bmatrix} 5 & -1 & -7 \\ -2 & -13 & 5 \\ -13 & 9 & -1 \end{bmatrix}$$

Now find P or

$$A \text{ adj} = A \text{ cofactor} = \begin{bmatrix} 5 & -2 & -13 \\ -1 & -13 & 9 \\ -7 & 8 & -1 \end{bmatrix}$$

Q2 Find the cofactors of A_{11}, A_{31}, A_{33}

$$A = \begin{bmatrix} 1 & -2 & 3 \\ -2 & -3 & 1 \\ 4 & -3 & 2 \end{bmatrix}$$

Solution $A_{21} = (-1)^{2+1} \begin{vmatrix} -2 & 3 \\ -3 & 2 \end{vmatrix} = (-1)(-4+9) = -5$

$$A_{21} = 5$$

$$A_{31} = (-1)^{3+1} \begin{vmatrix} -2 & 3 \\ 3 & 1 \end{vmatrix} = (1)(-2-9) = -11$$

$$A_{31} = -11$$

$$A_{33} = (-1)^{3+3} \begin{vmatrix} 1 & -2 \\ -2 & 3 \end{vmatrix} = (1)(3-4) = -1$$

$$A_{33} = (-1)$$

Date: _____

Page 4

$$Q3 \quad A = \begin{bmatrix} 2 & 1 & 1 \\ 1 & 3 & 2 \\ -1 & 1 & 2 \end{bmatrix} \quad I = \begin{bmatrix} 1 & 0 & 0 \\ 0 & 1 & 0 \\ 0 & 0 & 1 \end{bmatrix},$$

Solution Step 1 $|A - \lambda I| = 0$ formula

$$\begin{vmatrix} 2 & 1 & 1 \\ 1 & 3 & 2 \\ -1 & 1 & 2 \end{vmatrix} \rightarrow \begin{vmatrix} 2 - \lambda & 1 & 1 \\ 1 & 3 - \lambda & 2 \\ -1 & 1 & 2 - \lambda \end{vmatrix} = 0$$

$$\begin{vmatrix} 2 & 1 & 1 \\ 1 & 3 & 2 \\ -1 & 1 & 2 \end{vmatrix} \rightarrow \begin{vmatrix} 2 - \lambda & 0 & 0 \\ 0 & 2 & 0 \\ 0 & 0 & 2 \end{vmatrix} = 0$$

$$\begin{vmatrix} 2 - \lambda & 1 & 1 \\ 1 & 3 - \lambda & 2 \\ -1 & 1 & 2 - \lambda \end{vmatrix}$$

Now taken Determinant

$$2 - \lambda ((3 - \lambda)(2 - \lambda) - 1(2 - (2 - \lambda)) + 1(1 + 1(3 - \lambda))) = 0$$

$$2 - \lambda (6 - 3\lambda - 2\lambda + \lambda^2 - 2) - 1(2 - 2 + \lambda) + 1(4 - \lambda) = 0$$

$$2 - \lambda (\lambda^2 - 5\lambda + 4) - 1(\lambda) + 1(4 - \lambda) = 0$$

Date: _____

Page 5

$$2d^2 - 10d + 8 - d^3 + 5d^2 - 4d - d + 4 - d = 0$$

by ordering

$$-d^3 + 7d^2 - 16d + 12 = 0$$

×ing by (-1)

$$d^3 - 7d^2 + 16d - 12 = 0 \rightarrow \textcircled{A}$$

Now put $d = 2 = 0$

then $d = 2$ in above eqn \textcircled{A}

$$d^3 - 7d^2 + 16d - 12 = 0$$

put $d = 2$

$$(2)^3 - 7(2)^2 + 16(2) - 12 = 0$$

$$8 - 7(4) + 32 - 12 = 0$$

$$8 - 28 + 32 - 12 = 0$$

$$-20 + 20 = 0$$

$$0 = 0$$

So $d = 2$ or $d - 2 = 0$