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section	A
Paper	PRCD-I
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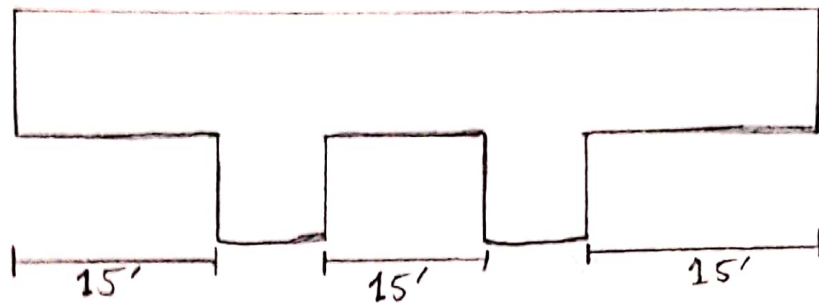
Question #01:

(1)

Given Data:

- 3 equal spans concrete slab
- clear span b/w supports = 15'
- Factored live load = 160 lb/ft²
- service floor finish load = 20 lb/ft²
- $F'_c = 4000$ psi
- $F_y = 40$ ksi

Solution:



Step #01: (Minimum Thickness)

By using formula

$$t_{\min} = L/28 = \frac{15}{28} = 6.4 \approx 6.5''$$

As $F_y \rightarrow 40$ ksi

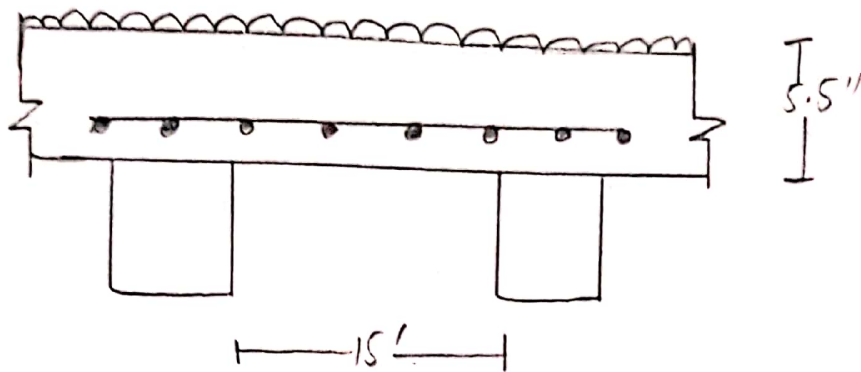
So we will multiply a factor with this thickness

$$\begin{aligned} \text{Factor} &= \left(0.4 + \frac{F_y}{100} \right) \\ &= \left(0.4 + \frac{40}{100} \right) = 0.8 \end{aligned}$$

Hence the minimum thickness will be 6.5×0.8

$$t_{min} = 5.2 \approx 5.5''$$

Step #02: (Effective Depth)



By formula

$$d = t - \text{clear cover} - \frac{1}{2} (\text{dia of main bars})$$
$$= 5.5 - 0.75 - \frac{1}{2} (5/8)$$

$$d \approx 4.5''$$

Step #03: (Self wt. of slab)

By formula

$$\frac{t}{12} + \gamma_{\text{concrete}}$$

$$= \frac{5.5}{12} \times 150 = 68.75 \text{ lb/ft}^2$$

Step #04: (Total Factored Load):

$$\text{Factored live load} = 160 \text{ lb/ft}^2$$

So Factored Dead Load will be

$$D.L = 1.2(20 + 68.75) = 106.5 \text{ lb/ft}^2$$

$$\text{Total Factored Load} = D.L + L.L$$

$$= 106.5 + 160$$

$$= 266.5 \text{ lb/ft}^2 = 0.2665 \text{ k/ft}^2$$

Step# 05 (Ultimate Moment):

(3)

By using formula

$$M_v = \frac{W_v \times L^2}{2} = \frac{0.2665 \times (15)^2}{8} \times 12$$

$$= 89.94 \text{ Kip-inches}$$

Step# 06: Area of Steel For Main bars
By Trial and Repeat Method:

Trial #01:

Let depth of compression block

$$a = 0.2 \times t$$

$$= 0.2 \times 5.5 = 1.1''$$

$$A_{st} = \frac{M_v}{\phi \times f_y \times (d - \frac{a}{2})} = \frac{89.94}{0.90 \times 40 \times (4.5 - \frac{1.1}{2})}$$

$$A_{st} = 0.63 \text{ in}^2$$

Trial #02 =

$$a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b} = \frac{0.63 \times 40}{0.85 \times 4 \times 12} \Rightarrow 0.62 \text{ in}^2$$

$$A_{st} = \frac{M_v}{\phi \times f_y \times (d - \frac{a}{2})} = \frac{89.94}{0.90 \times 40 \times (4.5 - \frac{0.6}{2})}$$

$$A_{st} = 0.59 \text{ in}^2$$

Trial #03:

$$a = \frac{0.59 \times 40}{0.83 \times 4 \times 12} = 0.57''$$

$$A_{st} = \frac{89.94}{0.90 \times 110 \times (4.5 - \frac{0.57}{2})} = 0.59 \text{ in}^2$$

So we will use $A_{st} = 0.59 \text{ in}^2$

Step # 07: Area of Steel for distribution (4) reinforcement.

By formula

$$A_{min} = 0.002 \times b \times t \rightarrow (\text{For Grad 40 steel}) \\ = 0.002 \times 12 \times 5.5 \Rightarrow 0.132 \text{ in}^2$$

Step # 08: Spacing for main bar.

By formula.

$$\text{Spacing} = \frac{A_b}{A_{st}} \times 12$$

We use #6 bar dia = $(\frac{6}{8})''$

$$\text{Area} = \frac{\pi}{4} \left(\frac{6}{8}\right)^2 = 0.442 \text{ in}^2$$

Step # 09: Spacing for distribution bars.

$$\text{Spacing} = \frac{A_b}{A_{st}}$$

We use #5 bars so; dia $(\frac{5}{8})''$

$$\text{Area} = \frac{\pi}{4} \left(\frac{5}{8}\right)^2 = 0.31 \text{ in}^2$$

$$\text{Spacing} = \frac{0.31}{0.132} \times 12 = 2.81 \approx 28'' \text{ c/c}$$

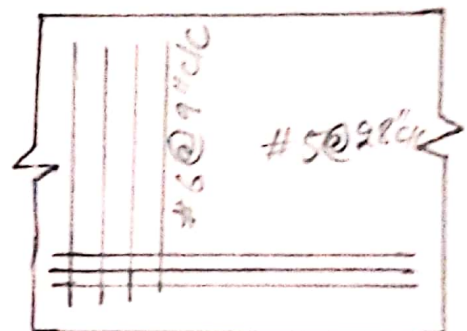
Step # 10:

$$f_c' = 4 \text{ ksi}, f_y = 40 \text{ ksi}$$

Main steel #6 at 9" c/c

Distribution steel

#5 at 28" c/c



Q No. 2):

65

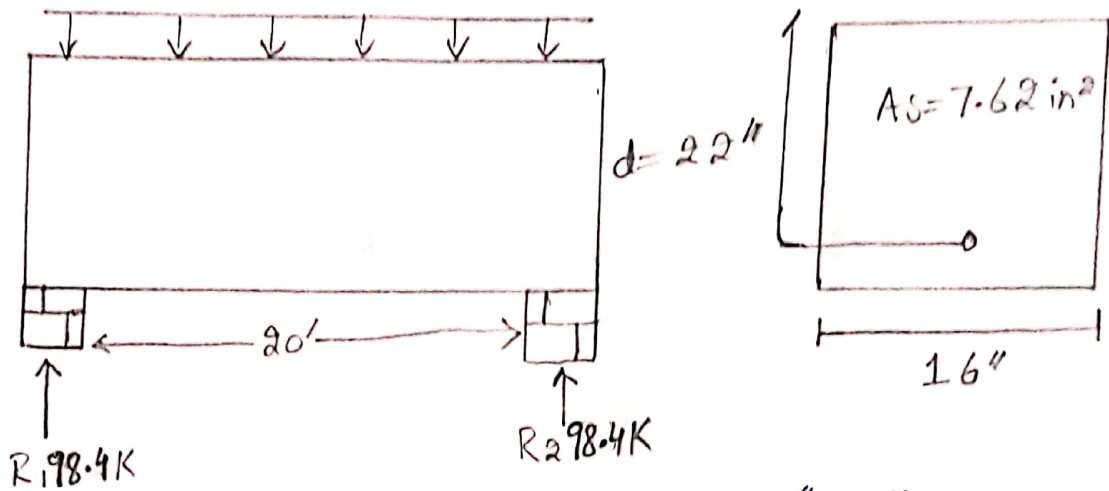
Solution:

At first find unit load of beam

So $b \times d_c$

$$\frac{16 \times 150}{12} = 200 \text{ lb/ft} = 0.2 \text{ K/ft}$$

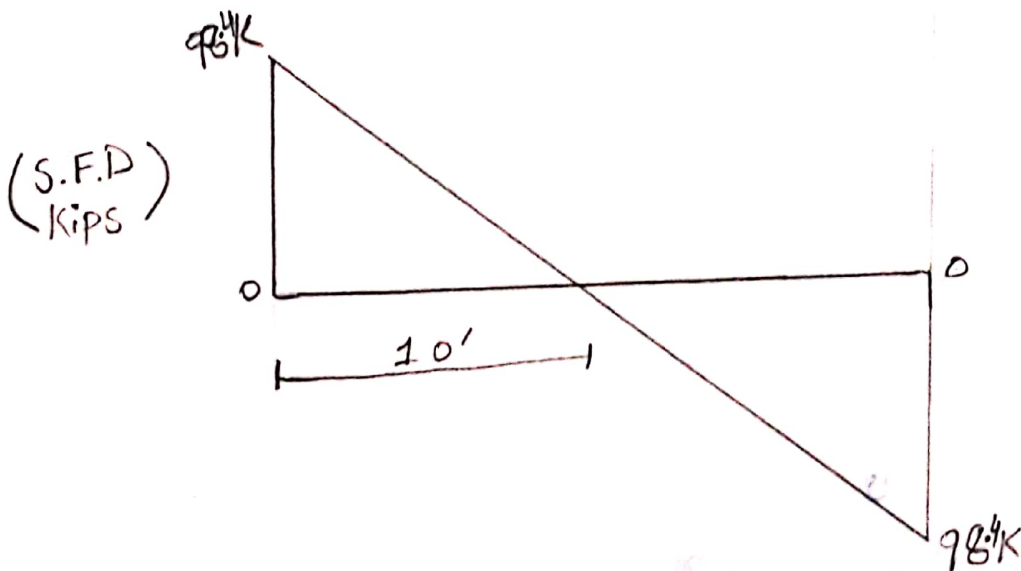
$$\text{Total factored load} = 9.4 + 0.2 = 9.6 \text{ K/ft}$$
$$W = 9.6 \text{ K/ft}$$



Step # 01: Find value of " R_1 " and " R_2 ".

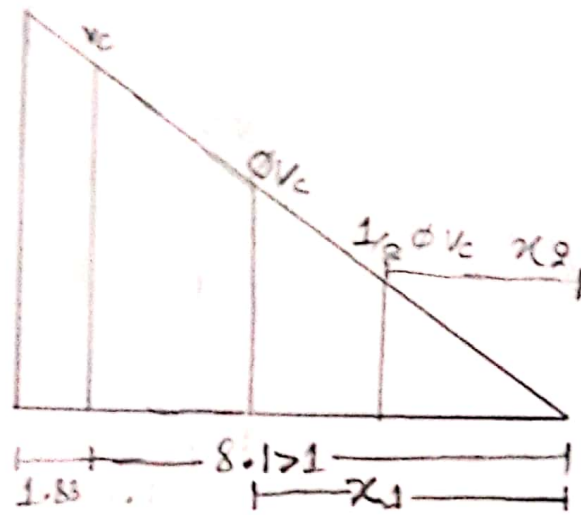
$$\text{Total load} = \frac{9.84 \times 20}{2} = 98.4 \text{ K}$$

Step # 02: Draw its shear force diagram.



Step#03 Finding value of critical stress V_u & its location.

As we know that critical location is located distance "d" from face of support $d = 22" = 1.83'$ value of critical shear at distance "d" by similarity triangles.



From similar Δ 's $\frac{9.6}{10} = \frac{V_u}{8.17}$

$$V_u = 78.43 \text{ K}$$

Step#04: Finding value of " ϕV_c " and " $\frac{1}{2} \phi V_c$ " and its distance from zero shear to right side.

$$\phi V_c = \phi \times 2 \times \sqrt{F'_c} \times b_w \times d = \frac{0.75 \times 2 \times \sqrt{4000} \times 16000}{1000}$$

$$\phi V_c = 33.40 \text{ K}$$

Location of ϕV_c by similarity of Δ 's

$$\frac{9.84}{10} = \frac{33.40}{x_1}$$

$$x_1 = 3.39'$$

Now $\frac{1}{2} \phi V_c = \frac{33.40}{2} = \boxed{16.70 \text{ K}}$ (7)

Location of $\frac{1}{2} \phi V_c \Rightarrow \frac{98.4}{10} = \frac{16.70}{x_2}$

$x_2 = \boxed{1.69'}$

Step #05 Find value of ϕV_s ($V_u = \phi V_s + \phi V_c$)

So we have

$\phi V_s = V_u - \phi V_c$

$\phi V_s = 80.39 - 33.40$

$\phi V_s = \boxed{46.99 \text{ Kips}}$

Step #06: Check section Adequacy

$\phi \times 8 \times \sqrt{F'_c} \times b_w \times d = \frac{0.75 \times 8 \times \sqrt{4000} \times 16 \times 22}{1000}$

$= \boxed{133.57 \text{ K}}$

$133.57 \text{ K} > \phi V_s$ (mean section is adequate)

Step #07: Check mini spacing for stirrups

$\phi \times 4 \times \sqrt{F'_c} \times b_w \times d \Rightarrow \frac{0.75 \times 4 \times \sqrt{4000} \times 16 \times 22}{1000}$

$= \boxed{66.79 \text{ K}} > \phi V_s = 44.03 \text{ K}$

Thus max spacing will be selected from the following 4 conditions.

① $S_{max} = 24''$

② $d/4 = \frac{22}{2} = 11''$

③ $S_{max} = \frac{A_v \times f_y}{0.75 \times \sqrt{F'_c} \times b_w}$

$$\therefore AV = \frac{\pi}{4} \left(\frac{3}{8} \right)^2 \therefore AV = 0.11 \times 2 = 0.22$$

(8)

$$S_{max} = \frac{0.22 \times 60000}{0.75 \times \sqrt{4000} \times 16}$$

$$\textcircled{4} S_{max} = \frac{AV \times f_y}{50 \times b_w} = \frac{0.22 \times 60000}{50 \times 16} = 16.50$$

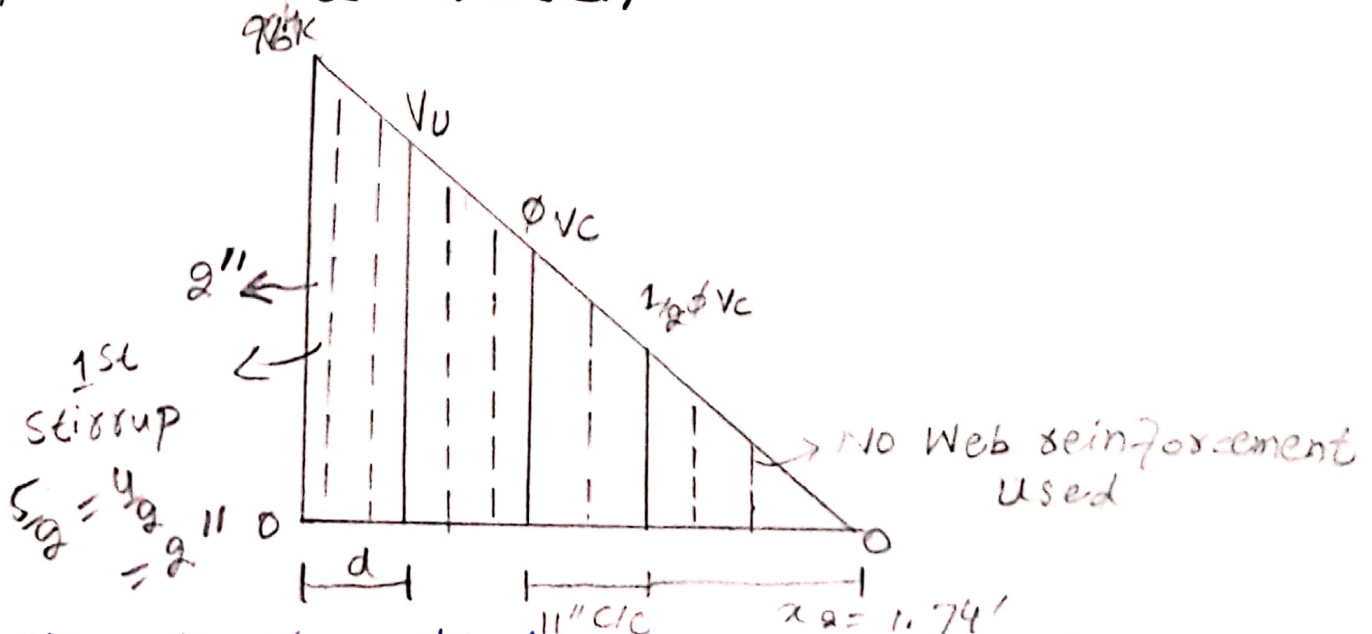
From the above 4 conditions, least value of spacing for #3 U Shaped will be selected so $S_{max} = 11" C/C$

Step # 08 Spacing of stirrup from a critical section.

$$S = \frac{\phi \times A_{ux} \times f_y \times d}{V_u - \phi V_c} = \frac{0.75 \times 0.22 \times 60 \times 22}{80.39 - 33.40}$$

$$S = 4" C/C$$

Step # 09 Final sketch



We know that first stirrup from face of support = $S/2 = 2.5 \approx 2"$

Q NO. 3:

(9)

Solution:

Step # 01: Find gross area of concrete.

$$A_g = b \times b \text{ (since it is square tied column)}$$

$$A_g = 12 \times 12 = 144 \text{ in}^2 \text{ (Actual)}$$

Step # 02: Find the area of steel.

$$\begin{aligned} \text{Since } A_s &= 5\% \text{ of } A_g \\ &= 0.05 \times 144 \end{aligned}$$

$$A_s = 7.2 \text{ in}^2$$

Step # 03: Ultimate load carrying capacity

$$\begin{aligned} P_u &= \phi \times 0.80 \times [0.85 \times f'_c \times (A_g - A_s) + A_s \times f_y] \\ &= 0.65 \times 0.80 [0.85 \times 4 [144 - 7.2] + 7.2 \times 60] \end{aligned}$$

$$P_u = 466.50 \text{ K}$$

Step # 04: Sketch & design of Ties (c/c distance)

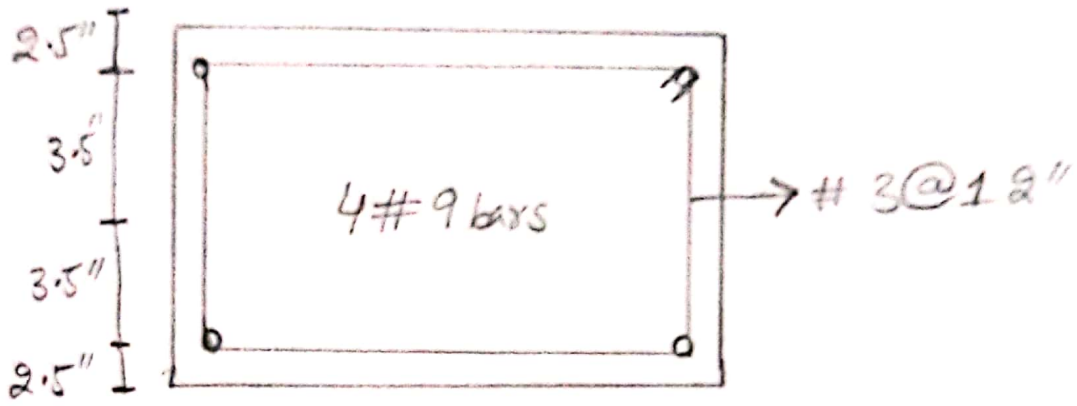
From the below value we choose the least values of all thus;

$$\begin{aligned} 1) 16 \times \text{dia of Long bar} &= 16 \times 9/8 \\ &= 18'' \end{aligned}$$

$$\begin{aligned} 2) 48 \times \text{dia of Tie bar} &= 48 \times 3/8 \\ &= 18'' \end{aligned}$$

$$3) \text{Least column dimension} = 12''$$

$$\text{So c/c distance b/w ties} = 12''$$



Since it is a tied square column, so there is no spiral stirrup used; the stirrup used is of rectangular shape due to the specification of the structure thus we will use tie stirrups instead.

Q4):

11

Step # 01: Let $h = 24''$

Step # 02:

$$\begin{aligned} \text{Total weight} &= \text{Wt of soil} + \text{Wt of RC} \\ &= 3 \times 120 + 2 \times 150 \\ &= 660 \text{ psf} = 0.660 \text{ Ksf} \end{aligned}$$

Step # 03: Effective bearing Capacity.

$$\begin{aligned} \sigma_e &= \sigma_a - W \\ &= 2.50 - 0.660 \end{aligned}$$

$$\sigma_e = 1.84 \text{ Ksf}$$

Step # 04: Requisitionment Area for Foundation.

$$\begin{aligned} A_{req} &= \frac{\text{Service Load}}{\sigma_e} = \frac{100 + 120}{1.84} \\ &= 119.57 \text{ ft}^2 \end{aligned}$$

Step # 05: Since Foundation is square

$$A_{req} = b \times b = 119.57 \approx 11'$$

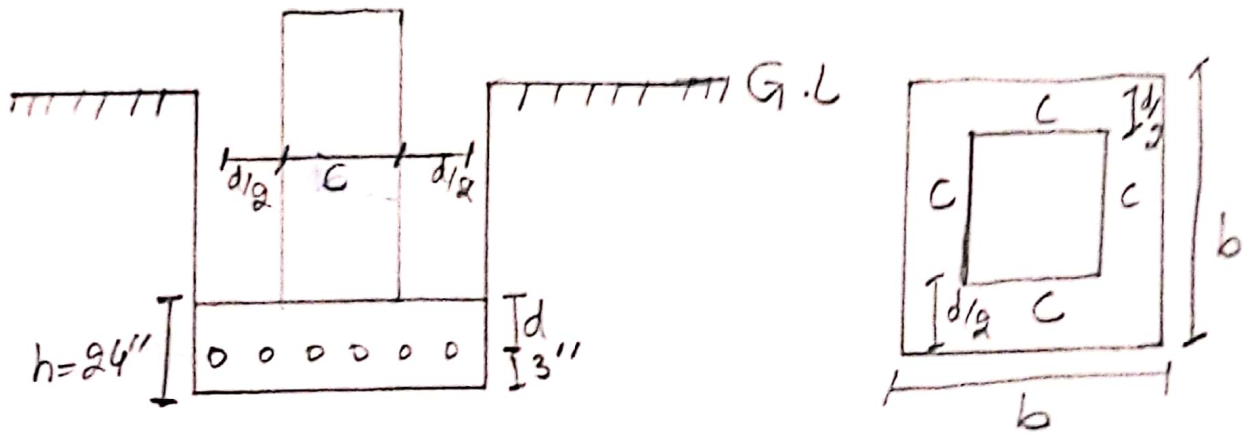
Step # 06: Upward bearing Capacity of soil

$$\sigma_{up} = \frac{\text{Factored load}}{(B)^2} = \frac{1.2 \times 100 + 1.6 \times 120}{11^2}$$

$$\sigma_{up} = 2.58 \text{ K/ft}^2$$

Step # 07: Punching Shear

$$b_o = 4 \times (c + d)$$



$$d = h - c - c - \text{dia} \Rightarrow \text{bar} - \frac{1}{2} d_b$$

$$= 24 - 3 - 1 - \frac{1}{2}(1) = 19.5''$$

... Take #8 bar
dia = $(8/8)'' = 1''$

$$b_o = 4 \times (16 + 19.5) = 142''$$

Step # 08:

$$V_{v2} = q_{up} \times [B^2 - (c+d)^2]$$

$$= 2.58 \times [11^2 - (\frac{16+19.5}{12})^2] \times 7$$

$$V_{v2} = 289.60 \text{ K}$$

Step # 09:

$$\phi V_{cp} = \phi \times 4 \times \sqrt{f'c} \times b \times d$$

$$= \frac{0.75 \times 4 \times \sqrt{4000} \times 142 \times 19.5}{1000}$$

$$\phi V_{cp} = 525.38$$

Step # 10: Beam ^{var/one} way shear check

$$V_{u1} = q_{up} \times B \times [\frac{B}{2} - \frac{c}{2} - d]$$

$$V_{u1} = 2.58 \times 11 \times [\frac{11}{2} - \frac{16}{2} - 19.5]$$

$$V_u = 90.95 \text{ K}$$

(13)

Step # 11: self shear capacity.

$$\begin{aligned} Q_{V_c} &= \phi \times 2 \times \sqrt{f'_c} \times b \times d \\ &= \frac{0.75 \times 2 \times \sqrt{4000} \times [11 \times 12 - 16]}{1000} \\ &= 110.04 \text{ K} > V_u \Rightarrow \text{OKay} \end{aligned}$$

Step # 12 Ultimate Moment.

$$\begin{aligned} M_u &= \frac{V_{up} \times B}{8} \times (B - C)^2 = \frac{2.58 \times 11}{8} \times \left(11 - \frac{16}{12}\right)^2 \\ M_u &= 331.49 \text{ K}' \approx 3977.93 \text{ K}'' \end{aligned}$$

Step # 13: Area of steel for main bars by Trail and Repeat Method.

Trail # 01:

$$\text{Let } a = 0.2 \times h = 0.2 \times 24 = 4.8''$$

$$A_s = \frac{M_u}{\phi \times f_y \times (d - a/2)} = \frac{3977.93}{0.90 \times 60 \times \left(11 - \frac{4.8}{2}\right)} = 8.56 \text{ in}^2$$

Trail # 02:

$$a = \frac{A_s \times f_y}{0.85 \times f'_c \times b} = \frac{8.56 \times 60}{0.85 \times 3 \times 11 \times 12} = 1.53''$$

$$A_s = \frac{3977.93}{0.90 \times 60 \times \left(11 - \frac{1.53}{2}\right)} = \boxed{7.197 \text{ in}^2}$$

Trail # 03:

$$a = \frac{7.197 \times 60}{0.85 \times 3 \times 11 \times 12} = 1.28''$$

$$A_s = \frac{3977.93}{0.90 \times 60 \left(11 - \frac{1.28}{2}\right)} = \boxed{7.1 \text{ in}^2}$$

So that area = 7.1 in²

Step #14: Check the min reinforcement by following 3 Method:

$$\text{a) } A_{s\text{min}} = 0.0018 \times B \times h = 0.0018 \times (11 \times 12) \times 24 = 5.70 \text{ in}^2$$

$$\text{b) } A_{s\text{min}} = \frac{200}{f_y} \times B \times h = \frac{200}{60000} \times (11 \times 12) \times 19.5 = 8.258 \text{ in}^2$$

$$\text{c) } A_{s\text{min}} = \frac{3 \times \sqrt{f'_c}}{f_y} \times B \times d = \frac{3 \times \sqrt{3000}}{60000} \times (11 \times 12) \times 19.5 = 7.05 \text{ in}^2$$

From above value greater value will be selected Thus $A_{s\text{min}} = 8.58 \text{ in}^2$

Step #15: Using # 8 bar

$$A_b = 0.785 \text{ in}^2$$

$$\text{No. of bars} = \frac{A_s}{A_b} = \frac{8.58}{0.785} = 10.92 \approx 11 \text{ bars in each direction.}$$