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Answer NO 1

$$\begin{bmatrix} 1 & 103 & 3 & 0 & 5 \\ 0 & 1 & -103 & 0 & 7 \\ 0 & 0 & 1 & 0 & -6 \\ 0 & 0 & 0 & 1 & 103 \end{bmatrix}$$

Solution

$$103 = 2$$

$$-103 = -4$$

$$\begin{bmatrix} 1 & 2 & 3 & 0 & 5 \\ 0 & 1 & -4 & 0 & 7 \\ 0 & 0 & 1 & 0 & -6 \\ 0 & 0 & 0 & 1 & 2 \end{bmatrix}$$

Multiplying Row three by 4  
and then add to Row two.

$$\begin{bmatrix} 1 & 2 & 3 & 0 & 5 \\ 0 & 1 & -4+4 & 0 & 7-24 \\ 0 & 0 & 1 & 0 & -6 \\ 0 & 0 & 0 & 1 & 2 \end{bmatrix} \quad R_2 + 4R_3$$

$$\begin{bmatrix} 1 & 2 & 3 & 0 & 5 \\ 0 & 1 & 0 & 0 & -17 \\ 0 & 0 & 1 & 0 & -6 \\ 0 & 0 & 0 & 1 & 2 \end{bmatrix}$$

Now multiplying Row two  
by "-2" and then  
add to Row one.

$$\begin{bmatrix} 1 & 2-2 & 3 & 0 & 5+34 \\ 0 & 1 & 0 & 0 & -17 \\ 0 & 0 & 1 & 0 & -6 \\ 0 & 0 & 0 & 1 & 2 \end{bmatrix} \quad R_1 - 2R_2$$

$$\begin{bmatrix} 1 & 0 & 3 & 0 & 39 \\ 0 & 1 & 0 & 0 & -17 \\ 0 & 0 & 1 & 0 & -6 \\ 0 & 0 & 0 & 1 & 2 \end{bmatrix}$$

Now multiplying Row three  
by "3" and then add  
to Row one.

$$\begin{bmatrix} 1 & 0 & 3 & 3 & 0 & 39+18 \\ 0 & 1 & 0 & 0 & 0 & -17 \\ 0 & 0 & 1 & 0 & 0 & -6 \\ 0 & 0 & 0 & 1 & 0 & 2 \end{bmatrix} \quad R_1 - 3R_3$$

$$\begin{bmatrix} 1 & 0 & 0 & 0 & 0 & 57 \\ 0 & 1 & 0 & 0 & 0 & -17 \\ 0 & 0 & 1 & 0 & 0 & -6 \\ 0 & 0 & 0 & 1 & 0 & 2 \end{bmatrix}$$

So this is the final  
Augmented matrix

$$K_1 = 57 \quad K_2 = -17 \quad K_3 = -6 \quad K_4 = 2$$

Verification :

$$K_1 + 2K_2 + 3K_3 = 5$$

putting values

$$57 + 2(-17) + 3(-6) = 5$$

$$57 - 34 - 18 = 5$$

$$57 - 52 = 5$$

$$5 = 5 \longrightarrow \text{true}$$

NOW

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$$11x - 4(11x) = 7$$

$$-17 - 4(-6) = 7$$

$$-17 + 24 = 7$$

$$7 = 7 \rightarrow \text{true}$$

Answer No 2:

Part A:

$$\begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 2 & -5 & -1 \end{bmatrix}$$

$$\begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 0 & 3 & -5 \end{bmatrix}$$

Solution:

first into second :

$$\begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 2 & -5 & -1 \end{bmatrix}$$

multiplying Row two by  
"-2" and then add to Row three

$$\begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 2-2 & -5+8 & -1+4 \end{bmatrix} \quad R_3 - 2R_2$$

$$\begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 0 & 3 & -5 \end{bmatrix}$$

so this is matrix two

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second matrix and first

$$\begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 0 & 3 & -5 \end{bmatrix}$$

multiply Row two by "2"  
and then add to Row one.

$$\begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 0+2 & -8+3 & 4-5 \end{bmatrix} R_3 + 2R_2$$

$$\begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 2 & -5 & -1 \end{bmatrix}$$

So this is the first matrix

ANSWER NO 2  
part B:

$$(a) \begin{bmatrix} e & 0 & 0 & 0 \\ 0 & x & 0 & 0 \\ 0 & 0 & -x & 0 \\ 0 & 0 & 0 & e \end{bmatrix}$$

Solution

it is in echelon form because it satisfies all the following condition

(1) all the entries in a column below a leading entry are zero

(2) each leading entry of a row is in a column to the right of the leading entry of the above row

(3) To satisfy the 3rd condition there is no

zero-row which should be below the all non-zero

$$(b) \begin{bmatrix} 1 & 0 & \pi \\ 0 & 1 & e \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{bmatrix}$$

it is in reduced echelon form because it is already in echelon form and satisfy the further two condition

(1) all the leading 1 is entries in non zero rows are one.

(2) Each leading 1 is the only non zero entry in its column

$$(c) \begin{bmatrix} 5 & 0 & 0 & 7 \\ 0 & 1 & 0 & 5 \\ 0 & 0 & 1 & 4 \end{bmatrix}$$



ANSWER NO C:

it is in echelon form because it satisfy all the following condition

- (1) all the entries of a row in a column below leading entry are zero
- (2) each leading entry of a row is in column to the right of the leading entry of the above row
- (3) to satisfy the 3rd condition there is no zero which should be below the all non zero rows

$$(d) \begin{bmatrix} 1 & 0 & 0 & 7 \\ 0 & 0 & 0 & 0 \\ 0 & 0 & 1 & 4 \end{bmatrix}$$

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it is neither in echelon form nor in reduced echelon form because it echelon satisfy the following condition

(1) All the zero rows are below the non zero row

ANSWER NO (3)

part A

the difference between echelon form and reduced echelon form are given below

echelon form :

A rectangular matrix is in echelon form if it has the following

three properties:

(1) All non zero rows are above any rows of all zero

(2) each leading entry of a row is in a column to the right of leading entry of the row above it

(3) All entries in a column below a leading entry are a zero

### Reduced Echelon Form

if a matrix in echelon form satisfy the following additional condition then it is in reduced echelon form for reduced row echelon form.

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(1) the leading entry in each non zero row is (one)

(2) each leading 1 is the only non zero entry in its column.

Answer NO 3:

part (b)

$$\begin{bmatrix} 1 & 102 & 8 \\ 2 & 5 & -1 \\ -103 & 6 & 0 \\ 1 & -4 & 10 \end{bmatrix}$$

Solution:

ID =

$$\begin{bmatrix} 1 & 6 & 8 \\ 2 & 5 & -1 \\ -2 & 0 & 0 \\ 1 & -4 & 14 \end{bmatrix}$$

multiply Row 1 by  
"2" and subtract Row  
two from Row four.

$$\begin{bmatrix} 1 & 6 & 8 \\ 2 & 5 & -1 \\ -2 & 0 & 0 \\ 0 & -16 & 24 \end{bmatrix} \quad 2R_1 - R_2$$

Now add Row two  
Row three

$$\begin{bmatrix} 1 & 6 & 8 \\ 2 & 8 & -1 \\ 0 & 8 & -1 \\ 0 & -16 & 29 \end{bmatrix} \quad R_3 + R_2$$

Now multiply Row three  
by two "2" and then add  
to Row 4.

$$\begin{bmatrix} 1 & 6 & 8 \\ 2 & 8 & -1 \\ 0 & 8 & -1 \\ 0 & 0 & 27 \end{bmatrix} \quad R_4 + 2R_3$$

Now subtract Row two  
from three Row

$$\begin{bmatrix} 1 & 6 & 8 \\ 2 & 8 & -1 \\ -2 & 0 & 0 \\ 0 & 0 & 27 \end{bmatrix} \quad R_3 - R_2$$

Now add Row three  
to Row two

$$\begin{bmatrix} 1 & 6 & 8 \\ 0 & 8 & -1 \\ -2 & 0 & 0 \\ 0 & 0 & 27 \end{bmatrix}$$

Now multiply Row two by  $(-3)$  and then subtract  $2$  times  $(4)$  times of Row one

$$\begin{bmatrix} 1 & 0 & 35 \\ 0 & 8 & -1 \\ -2 & 0 & 0 \\ 0 & 0 & 27 \end{bmatrix} \quad 4R_1 - 3R_2$$

Now multiply Row one by "2" and then add to Row three

$$\begin{bmatrix} 1 & 0 & 35 \\ 0 & 8 & -1 \\ 0 & 0 & 70 \\ 0 & 0 & 27 \end{bmatrix} \quad R_3 + 2R_1$$

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Now multiply Row three  
by "2" and then add  
to 5 times of Row "4"

$$\begin{bmatrix} 1 & 0 & 35 \\ 0 & 8 & -1 \\ 0 & 0 & 20 \\ 0 & 0 & -5 \end{bmatrix} \quad 5R_4 - 2R_3$$

Now multiply Row four  
by "4" and then add  
to Row three.

$$\begin{bmatrix} 1 & 0 & 35 \\ 0 & 8 & -1 \\ 0 & 0 & 0 \\ 0 & 0 & -5 \end{bmatrix} \quad R_3 + 4R_4$$

Now interchanging  $R_3$  into  $R_4$ .

$$\begin{bmatrix} 1 & 0 & 35 \\ 0 & 8 & -1 \\ 0 & 0 & -5 \\ 0 & 0 & 0 \end{bmatrix} \quad R_3 \leftrightarrow R_4$$

This is required echelon

END