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Section A

Given:-

factored live load = 160 lb/ft^2

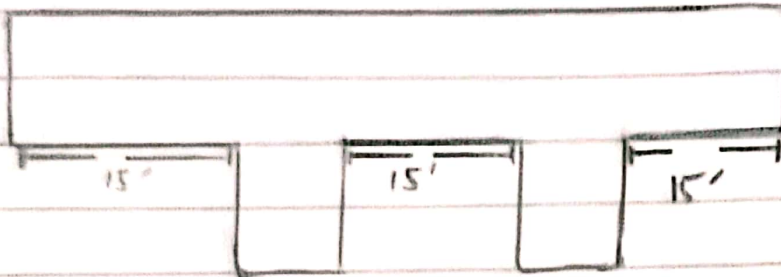
Service floor finish load = 20 lb/ft^2

Clear span b/w support = 15 ft

$f'_c = 4000 \text{ Psi}$

$f_y = 40 \text{ ksi}$

Formula + Solution:-



Minimum thickness:-

As we know that for over hanging slab we $L/28$ so,

$$t_{min} = L/28 = 15/28$$

$$t_{min} = 6.5''$$

As the F_y is no 60 ksi so factor will be multiplied

$$\text{Factor} = (0.4 + F_y/100) = (0.4 + \frac{40}{100})$$

$$\text{Factor} = 0.8$$

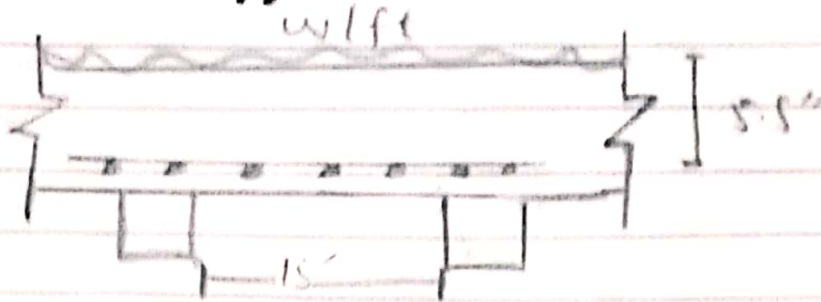
Minimum thickness will be 6.5×0.8

$$t_{min} = 5.2 \text{ or } 5.5''$$

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Step 2:- effective depth:-



As we know that

$$d = t - \text{clear cover} - \frac{1}{2} (\text{dia of main bar})$$

$$d = 5.5 - 0.75 - \frac{1}{2} \left(\frac{5}{8}\right)$$

$$d \approx 4.5''$$

Step 3:- slab's self weight :-

$$\Rightarrow \frac{t}{12} + \gamma_c$$

$$\Rightarrow \frac{5.5}{12} \times 150$$

$$= 68.75 \text{ lb/ft}^2$$

Step * 4 :- T. Factored load.

$$\text{Factored Live load} = 160 \text{ lb/ft}^2$$

$$\text{Factored dead load} = 1.2 (20 + 68.75) \\ = 106.5 \text{ lb/ft}^2$$

$$\text{Total Factored load} = D.L + L.L$$

$$= 106.5 + 160$$

$$= 266.5 \text{ lb/ft}^2$$

$$= 0.2665 \text{ k/ft}^2$$

ps Ultimate momentum:-

By Using formula

$$M_u = \frac{w_u \times L^2}{8} = \frac{0.2665 \times 15^2}{8} \times 12$$

$$= 89.94 \text{ kip-inches}$$

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Section A

Step 6:- Area of steel for main bar by Trial and Repeat method.

Trial 1:-

Let depth of compression blow is
 $a = 0.2 \times t \Rightarrow 0.2 \times 5.5 = 1.1''$

$$A_{st} = \frac{M_u}{\phi \times f_y \times (d - a/2)} = \frac{89.94}{0.90 \times 40 \times (4.5 - \frac{1.1}{2})}$$
$$A_{st} = 0.63 \text{ in}^2$$

Trial 2:-

$$a = \frac{A_{st} \times f_y}{0.55 \times f'_c \times b} = \frac{0.63 \times 40}{0.85 \times 4 \times 12} = 0.62 \text{ in}^2$$

$$A_{st} = \frac{M_u}{\phi \times f_y \times (d - a/2)} = \frac{89.94}{0.90 \times 40 \times (4.5 - \frac{0.6}{2})}$$
$$A_{st} = 0.59 \text{ in}^2$$

Trial 3:-

$$a = \frac{0.59 \times 40}{0.85 \times 4 \times 12} = 0.57''$$

$$A_{st} = \frac{89.94}{0.90 \times 40 \times (4.5 - \frac{0.57}{2})} = 0.59 \text{ in}^2$$

0.59 in² will be used.

Step 7:-

Area of steel for distribution Reinforcement
By formula.

$$A_{min} = 0.002 \times b \times t$$
$$= 0.002 \times 12 \times 5.5 \Rightarrow 0.132 \text{ in}^2$$

Step 8:-

Spacing for main bars:

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section A

By formula

$$\text{Spacing} = \frac{A_s \times 12}{A_{st}}$$

We use # 6 bar dia = $(6/8)"$

$$\text{Area} = \pi/4 (6/8)^2 = 0.442 \text{ in}^2$$

Step 9 spacing for distribution bars.

$$\text{Spacing} = \frac{A_b}{A_{st}}$$

We use # 5 bars so

$$\text{dia} = (5/8)" \quad \text{Area} = \pi/4 (5/8)^2 = 0.31 \text{ in}^2$$
$$\text{Spacing} = \frac{0.31 \times 12}{0.442} = 2.81" \approx 3"$$

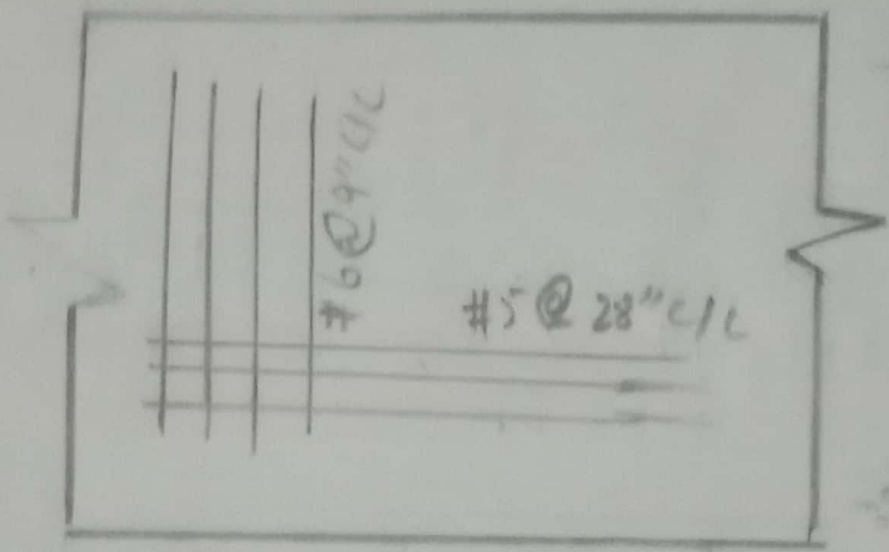
Step 10:-

$$f'_c = 4 \text{ ksi} \quad , \quad f_y = 40 \text{ ksi}$$

Main steel # 6 at 9" c/c

Distribution steel # 5 at 28" c/c

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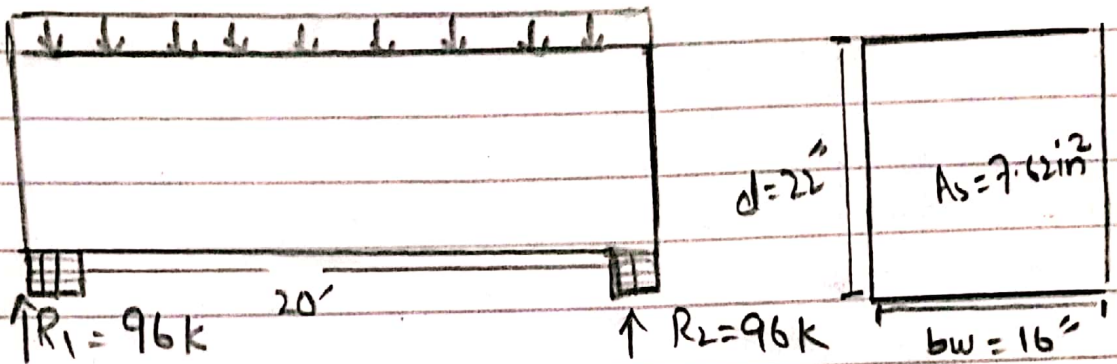
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Section A

Q2 A simply - ... ?

Unit load of Beam:- $\frac{16 \times 150}{12} = 2000 \text{ lb/ft}$
or 0.2 k/ft

So total factored load = $9.4 + 0.2$
 $w = 9.6 \text{ k/ft} = 9.6 \text{ k/ft}$

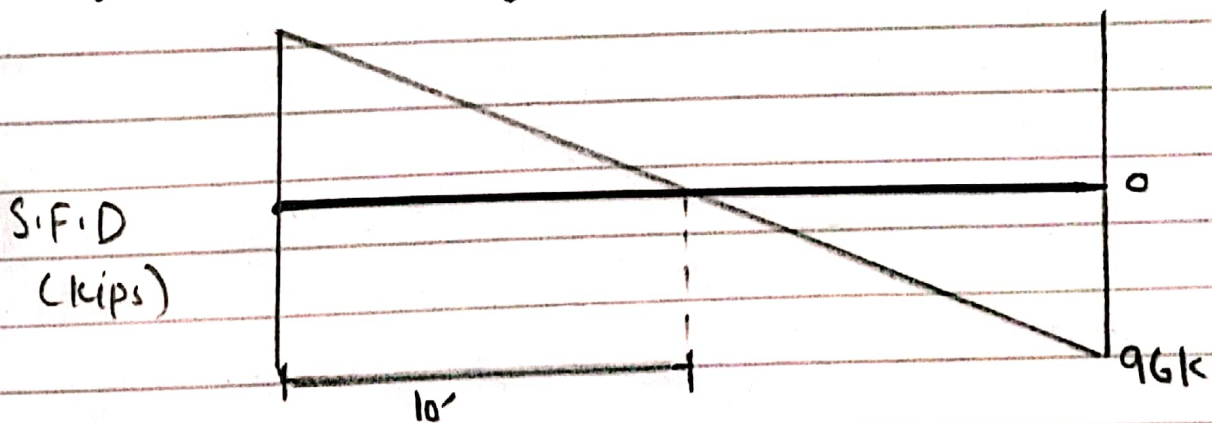


Step 1:-

Values of R_1 & $R_2 = ?$

Total load = $9.6 \times \frac{20}{2} = 96 \text{ k}$

Step 2:- Shear force diagram



Step 3:-

Value of critical stresses & location

As we know that critical section is located at section or distance "d" from face of support =

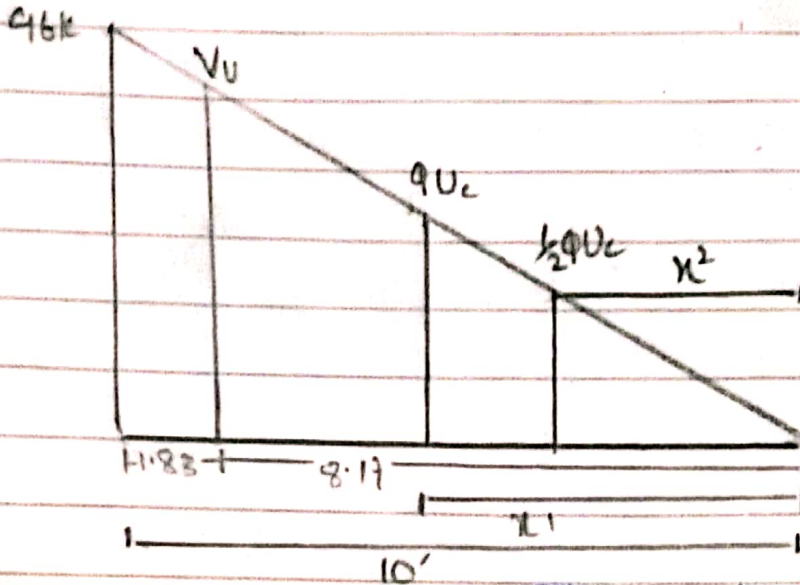
$a = 22'' \Rightarrow 1.83'$

Value of critical shear at distance "d"

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Section A

by similarity of triangles



from similar triangle = $96/10 = Vu/8.17$

$Vu = 78.43 k$

Step 4: find value of qUc & $1/2 qUc$

$qUc = \phi \times 2 \times \sqrt{f_c} \times b \times d$

$qUc = 0.75 \times 2 \times \sqrt{4000} \times 6 \times 16 \times 2 / 1000$

$qUc = 33.40 k$

location of qUc by similarity of Δs

$\frac{96}{10} = \frac{33.40}{x_1}$

$x_1 = 3.48'$

Now:- $1/2 qUc = \frac{33.40}{2} = 16.70 k$

location of $1/2 qUc \Rightarrow \frac{96}{10} = \frac{16.70}{x_2}$

$x_2 = 1.74'$

Step #5 Value of qVs

So $qVs = Vu - qUc$

$qVs = 78.43 - 33.40$

$qVs = 45.03 k$

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Section A

Step 6:- Check out Section adequacy :-

$$\phi \times 8 \times \sqrt{f_c'} \times b \times d \Rightarrow$$
$$\Rightarrow 0.75 \times 8 \times \sqrt{4000} \times 16 \times 22 / 1000$$
$$= 133.57k$$

As $\phi \times 8 \times \sqrt{f_c'} \times b \times d > \phi V_s$ (Section is adequate)

Step 7 :- Check on ~~main~~ spacing ^{of} stirrups

$$\phi \times 4 \times \sqrt{f_c'} \times b \times d =$$
$$= \frac{0.75 \times 4 \times \sqrt{4000} \times 16 \times 22}{1000} = 66.79k$$

As $\phi 4 \times \sqrt{f_c'} \times b \times d > \phi V_s = 45.03k$

Max spacing will be selected from

i) $s_{max} = 24"$ ii) $d/2 = 22/2 = 11"$

3) $s_{max} = \frac{A_u \times f_y}{0.75 \times \sqrt{f_c'} \times b \times w} \Rightarrow \frac{0.22 \times 60000}{0.75 \times \sqrt{4000} \times 16} = 17.40"$

$$\therefore A_u = \frac{\pi}{4} \left(\frac{3}{8}\right)^2 \Rightarrow 0.11 \times 2 \Rightarrow 0.22$$

4) $s_{max} = \frac{A_u \times f_y}{50 \times b \times w} = \frac{0.22 \times 60000}{50 \times 16} = 16.50$

$s_{max} = 11"$ C/C \therefore (least value of spacing for #3 U shaped)

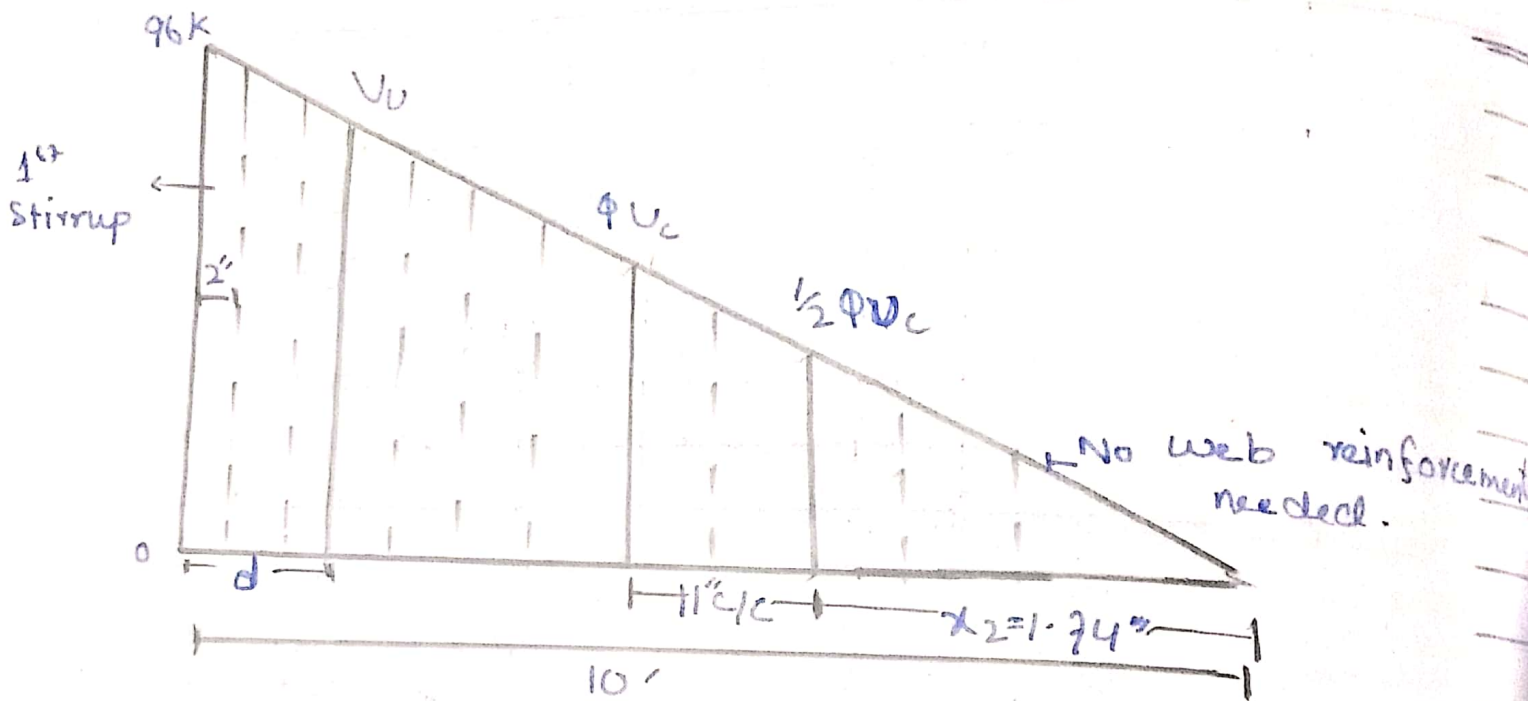
Step 8 :-

Spacing of Stirrup from 1st critical section :-

$$S = \frac{\phi \times A_u \times f_y \times d}{V_u - \phi V_c}$$

$$= \frac{0.75 \times 0.22 \times 60 \times 22}{78.43 - 33.40}$$

$$= 48.4" \text{ or } 5" \text{ C/C.}$$



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Q3 Step 1:-
Gross area of concrete:-

$$A_g = b \times b \text{ (square tied column)}$$

$$A_g = 12 \times 12 = 144 \text{ in}^2 \text{ (Actual)}$$

Step 2:-
Area of steel

$$\text{Since } A_s = 5\% \text{ of } A_g \\ = 0.05 \times 100$$

$$A_s = 7.2 \text{ in}^2$$

Step 3:-

Ultimate load carrying capacity

$$P_u = \phi \times 0.80 \times [0.85 \times f'_c \times (A_g - A_s) + A_s \times f_y]$$

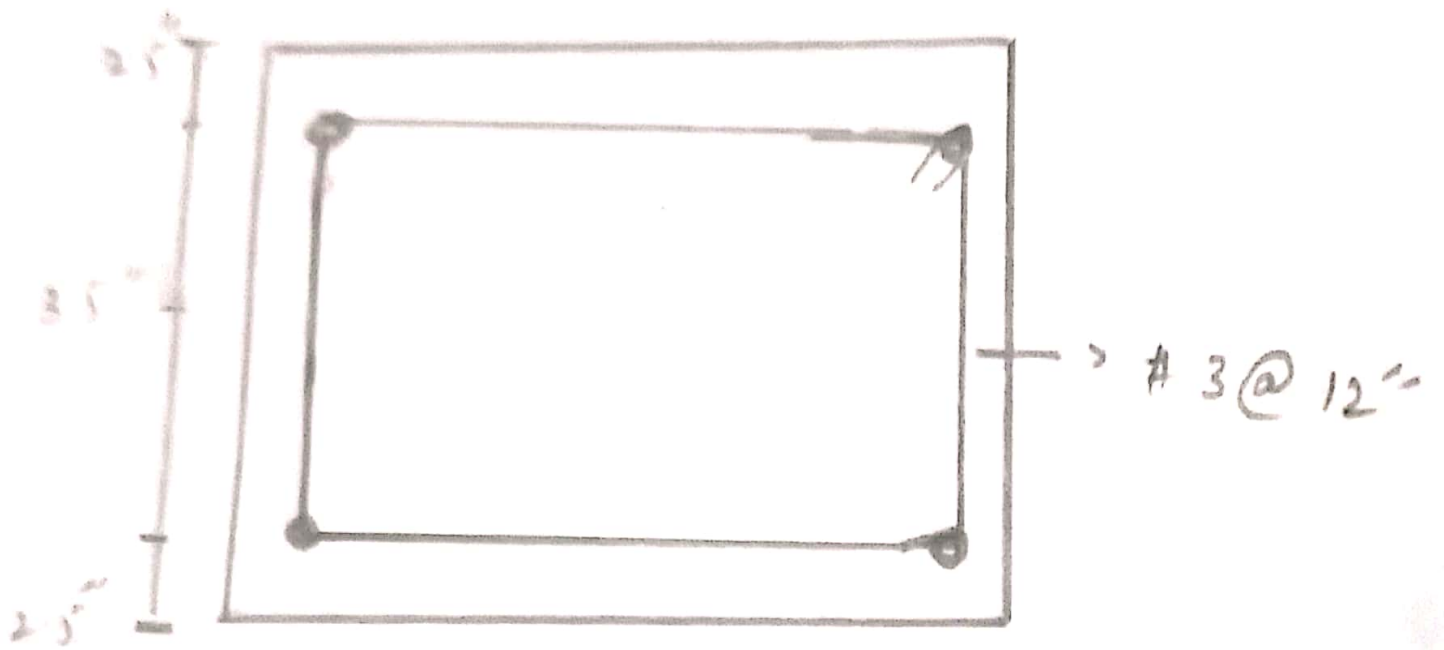
$$P_u = 0.65 \times 0.80 [0.85 \times 4 [144 - 7.2] + 7.2 \times 60]$$

$$P_u = 466.40 \text{ k}$$

Step 4:- from the below value we choose the least value of all these

- 1) 16 x dia of long bar = $16 \times \frac{9}{8} = 18''$
- 2) 48 x dia of tie bar = $48 \times \frac{3}{8} = 18''$
- 3) least column dimension = $12'' = \text{C/C d b/w ties } 12''$

Since it is a tied square column so there is no spiral stirrup used, the stirrup used is a rectangular shape due to the specification of the structure thus we will use stirrups instead.



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Sec A

Q4 Design a square - - - ?

Step 1:-

$$h = 24''$$

Step 2:-

$$\begin{aligned} \text{Total weight} &= \text{wt of soil} + \text{wt of Re} \\ &= 3 \times 120 + 2 \times 150 \\ \text{Total wt} &= 660 \text{ Psf} = 0.660 \text{ ksf} \end{aligned}$$

Step 3:-

$$\begin{aligned} \text{effective bearing capacity, } q_e &= q_u - w \\ q_e &= 2.50 - 0.660 \\ q_e &= 1.84 \text{ ksf} \end{aligned}$$

Step 4:-

$$\begin{aligned} \text{Required area for foundation} \\ A_{req} &= \frac{\text{Service load}}{q_e} = \frac{100 + 120}{1.84} \\ A_{req} &= 119.57 \text{ ft}^2 \end{aligned}$$

Step 5:-

$$\begin{aligned} \text{Since foundation is square } A_{req} &= b \times b \\ A_{req} = 119.57 &\Rightarrow B \approx 11' \end{aligned}$$

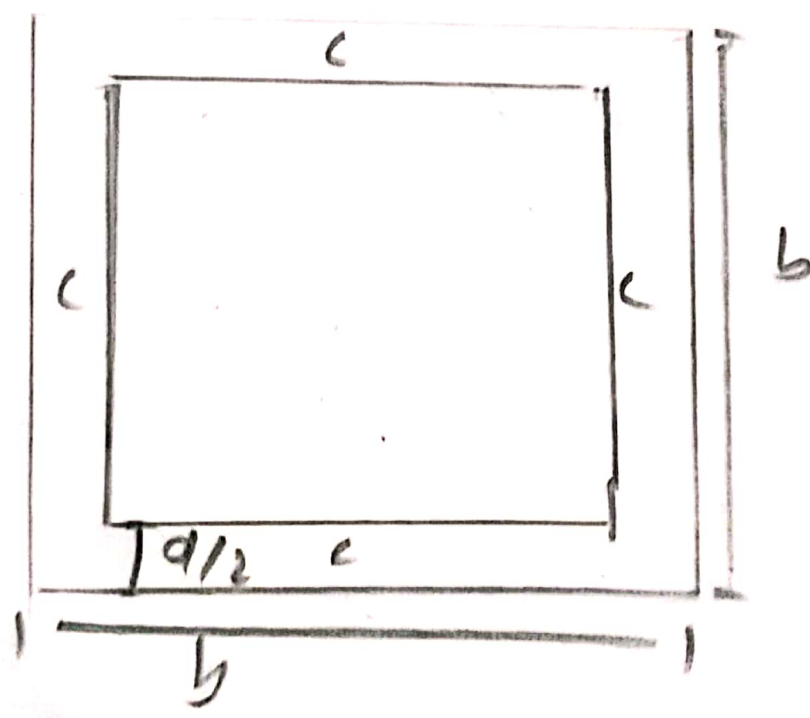
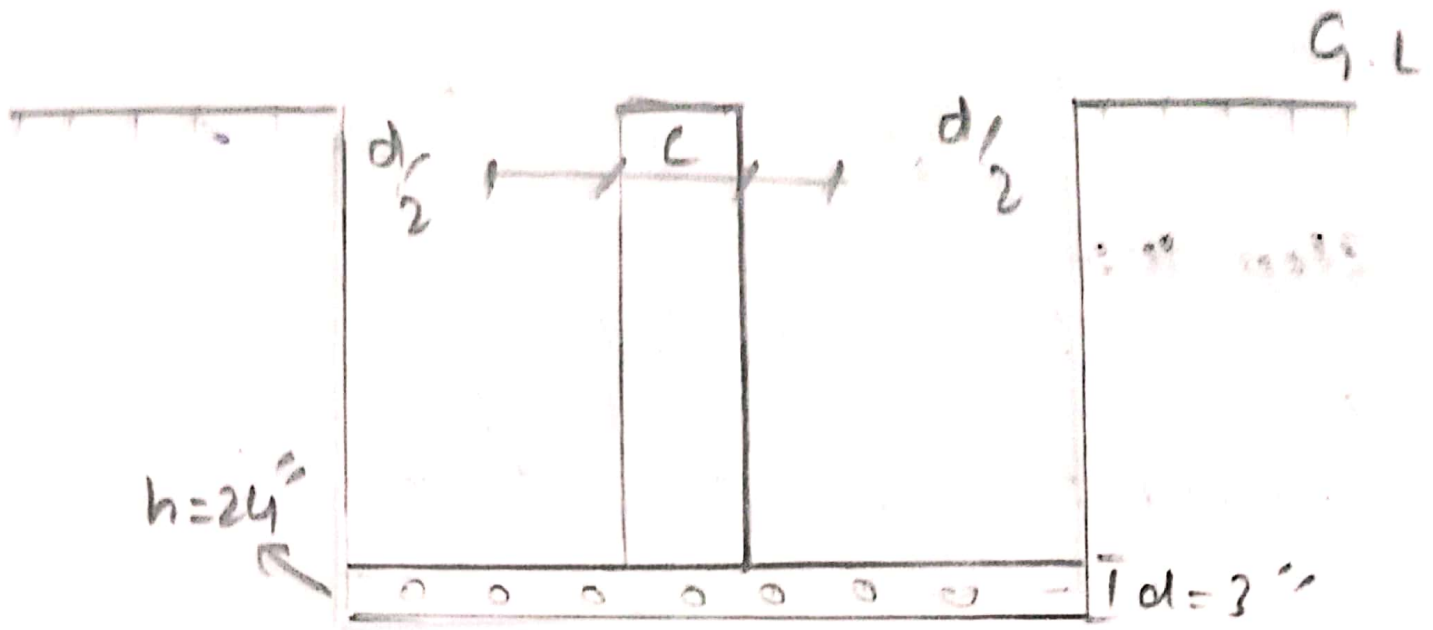
Step 6:-

$$\begin{aligned} \text{Upward bearing capacity of soil.} \\ q_{rup} &= \frac{\text{Factored load}}{B^2} = \frac{1.2 \times 100 + 1.6 \times 120}{11^2} \end{aligned}$$

$$q_{rup} = 2.58 \text{ k/ft}^2$$

Step 7:-

$$\begin{aligned} \text{Punching Shear} \\ b_o &= 4 \times (L + d) \\ d &= h - \text{c.c. - dia of bar} - \frac{1}{2} db \end{aligned}$$



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$$d = 24 - 3 - 1 - \frac{1}{2}(1) = 19.5''$$

$$b^o = 4 \times (16 + 19.5) = 142''$$

Step 8:-

$$\begin{aligned} V_{u2} &= q_{up} \times \left[\frac{B^2 - (c+d)^2}{12} \right] \\ &= 2.58 \times \left[\frac{11^2 - (16 + 19.5)^2}{12} \right] \\ V_{u2} &= 289.60 \text{ k} \end{aligned}$$

Step 9:-

$$\begin{aligned} \phi V_{c/p} &= \phi \times 4 \times \sqrt{f'_c} \times b \times d \\ &= \frac{0.75 \times 4 \times \sqrt{4000} \times 142 \times 19.5}{1000} \end{aligned}$$

$$\phi V_{c/p} = 525.38$$

Step 10:-

Beam shear / one way shear check

$$V_{u1} = q_{up} \times B \times \left[\frac{B}{2} - \frac{c}{2} - d \right]$$

$$V_{u1} = 2.58 \times 11 \times \left[\frac{11}{2} - \frac{16}{2} - 19.5 \right]$$

$$V_{u1} = 90.95 \text{ k}$$

Step 11:-

Self shear capacity

$$\phi V_c = \phi \times 2 \times \sqrt{f'_c} \times b \times d$$

$$= \frac{0.75 \times 2 \times \sqrt{4000} \times [11 \times 12.16]}{1000}$$

$$= 110.04 \text{ k} > V_{u1} \Rightarrow \text{O.K.}$$

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Sec A

Ultimate moment:-

$$M_u = \frac{q_{up} \times B \times l^2}{8} = \frac{2.58 \times 11 \times (11-15)^2}{8 \times 12}$$

$$M_u = 331.49 \text{ k} \approx 3977.93 \text{ k}$$

Step 13:- Area steel for main bars

Trial 1:- Let $a = 0.2 \times h \Rightarrow 0.2 \times 24 = 4.8''$

$$A_s = \frac{M_u}{\phi \times f_y \times (d - \frac{a}{2})} = \frac{3977.93}{0.90 \times 60} = 8.56 \text{ in}^2$$

Trial 2 $a = \frac{A_s \times f_y}{0.85 \times f_c' \times b} = \frac{8.56 \times 60}{0.85 \times 3 \times 11 \times 12} = 1.53''$

$$A_s = \frac{3977.93}{0.90 \times 60 \times (\frac{11 - 1.53}{2})} = 7.197 \text{ in}^2$$

Trial 2 $a = \frac{7.197 \times 60}{0.85 \times 3 \times 11 \times 12} = 1.28''$

$$A_s = \frac{3977.93}{0.90 \times 60 \times (\frac{11 - 1.28}{2})} = 7.1 \text{ in}^2 \text{ this will be used}$$

Step 14:- $A_{smin} = 0.0018 \times B \times h = 0.0018 \times (11 \times 12) \times 24 = 5.70 \text{ in}^2$

$$\hookrightarrow A_{smin} = \frac{200}{f_y} \times B \times h = \frac{200}{6000} \times 11 \times 12 \times 19.5$$

$$= 8.58 \text{ in}^2$$

$$A_{smin} = \frac{3 \times \sqrt{f_c'}}{f_y} \times B \times d = \frac{3 \times \sqrt{3000}}{6000} (11 \times 12) \times 19.5$$

$$= 7.05 \text{ in}^2$$

from the above greater value

8.58 will be used

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Step 15:

Using 8# bar

$$A_b = 0.785 \text{ in}^2$$

$$\text{No of bars} = \frac{A_s}{A_b} = \frac{8.58}{0.785} = 10.92$$

11 bars in each directions