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Section

A

Assignment No

1, 2, 3

Subject

Hydraulic Engineering.

Qno 1)

Ans 1) Venturi flume

A venturi flume is a critical-flow open flume with a constricted flow which causes a drop in the hydraulic grade line, creating a critical depth. It is used in flow measurement of very large flow rates, usually give a millions of cubic units. A venturi meter would normally measure in millimeter where as a venturi flume measure in meters.

Measurement of discharge with venturi meter flumes require two measurement, one upstream & one at the throat (narrowest cross section). At the flow passes in a subcritical state through the flume if the flume are designed so as to pass the flow from sub to super critical state while passing through the flume, a single measurement at the throat is sufficient for computation of discharge. To ensure the occurrence of critical depth at the throat the flumes are usually designed in such a way that as to form hydraulic jump

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on the downstream side of the structure.

Qno2)

Ans 2) Given data:-

$$b = 3\text{m} \quad \phi = 12\text{m}^3/\text{sec}$$

Required:- a) The critical depth

b) The minimum specific energy

c) The alternate depth where $E = 4\text{m}$

Solution:-

a) Discharge per unit width:-

$$q = \frac{\phi}{b} = \frac{12}{3} = 4\text{m}^3/\text{sec}$$

then rectangular channel

$$h_c = \left(\frac{q^2}{g} \right)^{1/3} = \left(\frac{4^2}{9.81} \right)^{1/3} = 1.177\text{m}$$

b) For rectangular channel:-

$$E_c = \frac{3}{2} h_c \Rightarrow \frac{3}{2} \times 1.17$$

$$E_c = 1.766\text{m}$$

mini specific energy = 1.77

c) As $E > E_c$, there are two possible depth for a given specific energy:-

$$E = h + \frac{v^2}{2g} \quad \text{where} \quad v = \frac{\phi}{A} = \frac{q}{h}$$

For rectangular channel

$$E = h + \frac{q^2}{2gh^2}$$

Substituting values in meter-second units

$$4 = h + \frac{0.8155}{h^2}$$

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For the subcritical (slow, deep) solution, the first term associated with potential energy

$$h = 4 - \frac{0.8155}{h^2}$$

e.g. $h=4$ gives $h = 3.948 \text{ m}$

For the supercritical solution

$$h = \sqrt{\frac{0.8155}{4-h}}$$

$$h = 0.4814 \text{ m}$$

alternate depths are 3.95 m & 0.481 m .

Assignment NO 2:-

Q no 1)

Ans:- solution:-

By checking Froude number

$$Fr = \frac{v}{\sqrt{gy}} \Rightarrow \frac{6}{\sqrt{9.81 \times 0.1}} = 6.06$$

$$\boxed{Fr \quad 6.06 > 1}$$

Flow is supercritical

$$E = y + \frac{v^2}{2g} = 0.1 + \frac{6}{2 \times 9.81}$$

$$E = 1.935$$

For alternate depth $E = 1.935 \text{ m}$

For alternate depth $E = 1.935 \text{ m}$

$$\boxed{y_{alt} = 1.93}$$

Q no 2)

Ans 2) Given data:-

$$V_1 = 2 \text{ m/s}$$

$$y_1 = 3 \text{ m}$$

$$\Delta z = 60 \text{ cm} = 0.6 \text{ m}$$

$$\text{down step} = 15 \text{ cm} = 0.15 \text{ m}$$

Solution:-

$$E_1 = y_1 + \frac{V_1^2}{2g}$$

$$= 3 + \frac{2^2}{2 \times 9.81}$$

$$E_1 = 3.20 \text{ m}$$

Now

$$E_2 = E_1 - \Delta z$$

$$= 3.2 - 0.6$$

$$E_2 = 2.60 \text{ m}$$

Also

$$E_2 = y_2 + \frac{V_2^2}{2g y_2^2}$$

$$2.60 = y_2 + \frac{6^2}{2 \times 9.81 y_2^2}$$

$$y_2 = 2.24 \text{ m}$$

$$\Delta y = 2.24 \text{ m}$$

$$\Delta y = y_2 - y_1$$

$$= 2.24 - 3$$

$$\Delta y = -0.76 \text{ m}$$

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so water surface drop = 0.16m

⇒ For a downward step of 15cm or 0.15m we have

$$E_2 = E_1 - \Delta z = 3.20 - (-0.15)$$

$$E_2 = 3.35\text{m}$$

$$\text{Now } y_2 = 3.17\text{m}$$

$$\Delta y = y_2 - y_1 = 3.17 - 3$$

$$\Delta y = 0.17\text{m}$$

So water surface rises 0.02m

⇒ The max upstep possible before affecting upstream water surface level is h_0

$$y_2 = y_c$$

$$y_c = 3 \sqrt{\frac{q^2}{g}}$$

$$y_c = 3 \sqrt{\frac{6^2}{9.8}}$$

$$y_c = 1.54\text{m}$$

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Assignment NO 3:-

Q no 1)

Given data:-

$$y_1 = 3.6 \text{ m} \quad y_2 = 0.9 \text{ m}$$
$$b = 3.9 \text{ m}$$

Sol:-

$$E_1 = E_2$$

$$y_1 + \frac{v_1^2}{2g} = y_2 + \frac{v_2^2}{2g} \quad \text{--- (1)}$$

Now

$$Q = A_1 v_1 = A_2 v_2$$

$$b y_1 v_1 = b y_2 v_2$$

$$y_1 v_1 = y_2 v_2$$

$$v_2 = \frac{y_1}{y_2} \times v_1$$

$$v_2 = \frac{3.6}{0.9} \times v_1$$

$$\boxed{v_2 = 4 v_1} \quad \text{--- (2)}$$

Put in eq (1)

$$y_1 + \frac{v_1^2}{2g} = y_2 + \frac{v_2^2}{2g}$$

$$3.6 + \frac{(v_1)^2}{2g} = 0.9 + \frac{(4v_1)^2}{2g}$$

$$\frac{(v_1)^2}{2g} - \frac{16v_1^2}{2g} = 0.9 - 3.6$$

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$$\frac{v_1^2 - 16v_1^2}{2g} = -2.7$$

$$\frac{-15v_1^2}{2g} = -2.7$$

$$\sqrt{v_1^2} = \sqrt{\frac{2.7 \times 2 \times 9.81}{15}}$$

$$v_1 = 1.879 \text{ m/sec}$$

Put in eq (2) we will get

$$\Rightarrow v_2 = 4v_1$$

$$v_2 = 4(1.879) = \boxed{7.516 \text{ m/sec}}$$

$$As \quad \phi_1 = A_1 v_1 = b_1 y_1 v_1$$

$$= 3.9 \times 3.6 \times 1.879$$

$$\boxed{\phi_1 = 26.38 \text{ m}^3/\text{sec}}$$

$$\phi_2 = A_2 v_2 = b_2 y_2 v_2$$

$$= 3.9 \times 0.9 \times 7.516$$

$$\boxed{\phi_2 = 26.38 \text{ m}^3/\text{sec}}$$

$$\phi = \phi_1 = \phi_2 = 26.38 \text{ m}^3/\text{sec}$$

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Froude number at upstream side

$$Fr_1 = \frac{V_1}{\sqrt{g y_1}} = \frac{1.879}{\sqrt{9.81 \times 3.6}}$$

$$\boxed{Fr_1 = 0.31}$$

subcritical flow

Froude number at downstream side

$$Fr_2 = \frac{V_2}{\sqrt{g y_2}} = \frac{7.516}{\sqrt{9.81 \times 0.9}}$$

$$\boxed{Fr_2 = 2.52}$$

super critical flow