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Sec = A

Paper = Maths II

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H-

Question No#1

Part (B)

GIVEN DATA:-

$$H = 26 \text{ ft}$$

$$\text{Assume diameter} = D = 22 \text{ ft}$$

$$\text{Tangential stress} = 600 \text{ lb/ft}^2$$

Specific weight of water

$$\text{tank} = 62.4 \text{ lb/ft}^3$$

Now find the thickness = ?

Solution:-

The pressure develop by

$$\text{water} = P = \gamma h$$

$$P = \gamma \cdot h$$

$$\Delta t = \frac{rhd}{at} \Rightarrow \frac{rhd}{at}$$

$$at \times \Delta t = rhd$$

$$at = \frac{rhd}{\Delta t}$$

$$t = \frac{rhd}{\Delta t \times a}$$

Putting the values

$$t = \frac{(0.2 \times 4) \times (20 \times 10^{-2}) \times (20 \times 10^{-2})}{6000 \times 2}$$

$$6000 \times 2$$

$$t = 0.24 \text{''}$$

Ans.

Question No # 1
Part (A)

GIVEN DATA:-

height of sec = $h = 300\text{mm}$

Thickness = $b = 20\text{mm}$

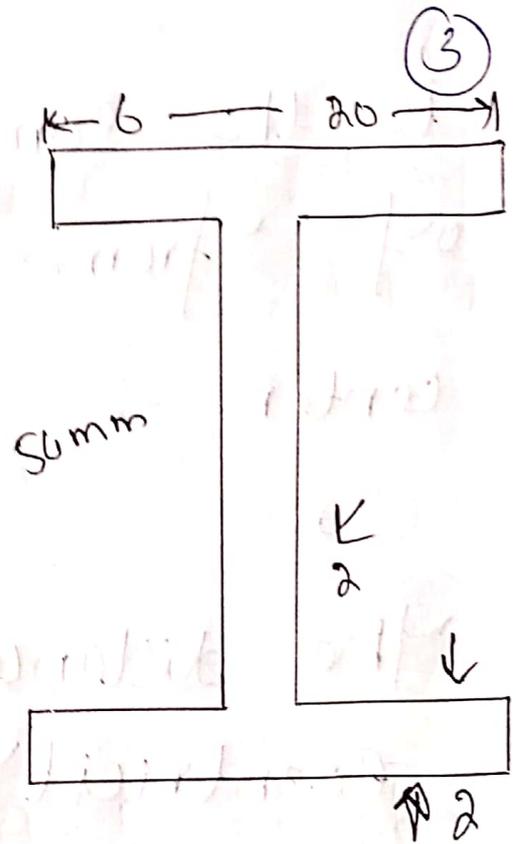
$$\Rightarrow b = 20\text{mm}$$

$$t_p = 2\text{mm}$$

REQUIRED:-

Shear Center = ?

As we know that for the unsymmetrical members of the Shear Center



(4)

is the same distance away
of from the geometrical
center.

So,

The distance is called
eccentricity which are
as given;

Solution:-

$$e = \frac{\sqrt{I_x^2 + I_y^2}}{4I}$$

So,

Here in moment of Inertia

and are given as

$$I = 2\left(\frac{bh^3}{12} + Ay^2\right) + \left(\frac{bh^3}{12} + Ay^2\right)$$

$$\Rightarrow I = 2 \left[\frac{2b(a)^3}{12} + (20 \times 2)(25)^2 \right] + \left(\frac{2(50)^3}{12} + 0 \right)$$

$$I = 50034.66 + 20833.33$$

$$I = 70867.99 \text{ mm}^4$$

Now eq (1)

$$e = \frac{14 h^2 b^2}{4I}$$

$$e = \frac{2 \times (50)^2 \times (25)^2}{4(70867.99)}$$

$$e = 11.0234 \text{ mm}$$

$$e = 11.0234 \text{ mm}$$

Shear center is 11.0234 mm

away from the geometrical center.

QUESTION NO # 2.

PART # (A).

GIVEN DATA:-

$$b = 100 \text{ mm}$$

$$h = 150 \text{ mm}$$

$$\text{Load} = P = 4 \text{ kN/m}$$

$$\text{Length of beam} = 3 \text{ m}$$

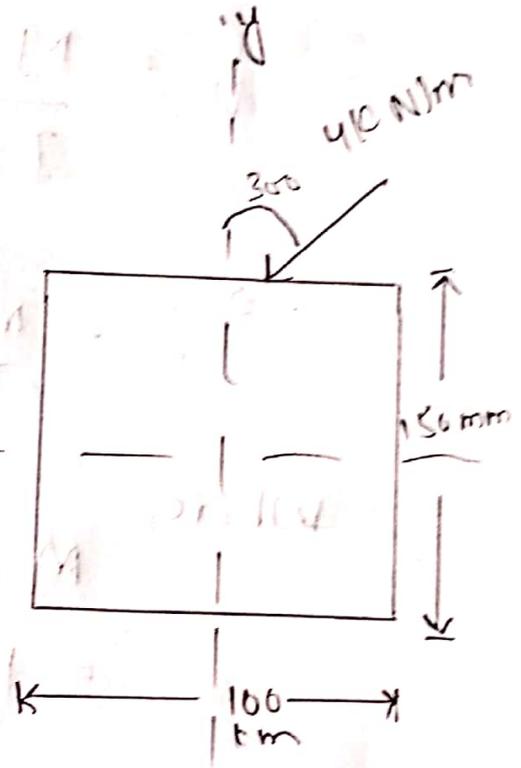
REQUIRED:-

$$\text{Bending Stress} = ?$$

$$N.A = ?$$

As we know that

$$p = \frac{M}{I} \cdot y$$



$$\delta = \frac{M_z Y}{I_z} + \frac{M_y Z}{I_y} \quad \therefore M_z = m \cos \theta$$

$$M_y = m \sin \theta$$

$$\Rightarrow \delta = \frac{m \cos \theta}{I_z} + \frac{m \sin \theta}{I_y} \rightarrow \textcircled{a}$$

where,

$$M = \cos \theta = P \cos \theta = M_z$$

$$= 1.8 \cos 30^\circ = M_z$$

$$M_z = 1.8510$$

$$M \sin \theta = P \sin \theta = M_y$$

$$M_y = 1.2 \sin 30^\circ$$

$$M_y = -11.8563$$

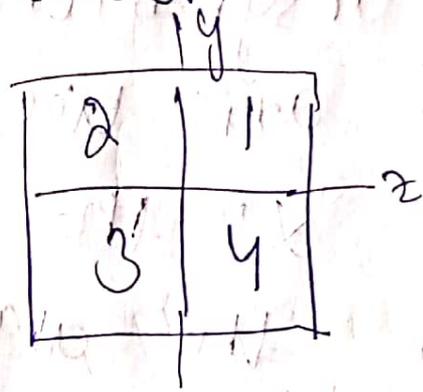
$$\delta = \left(\frac{M_z}{I_z} \right) + \left(\frac{M_y}{I_y} \right)$$

$$\delta = \frac{1.851}{2.812 \times 10^5} + \frac{(-11.8563)}{1.25 \times 10^5}$$

$$= 882078 \text{ Nm}^2$$

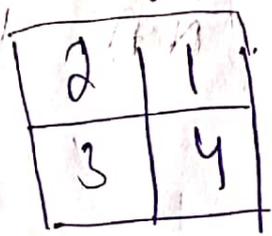
P.T.O

Sign Convention

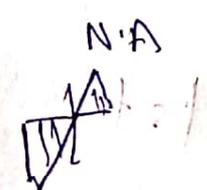
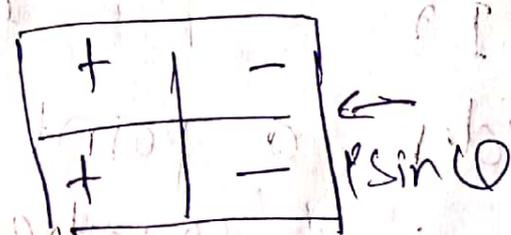


if we take compression as a negative and tension as a positive, and the beam is a simply supported.

↓ pressure



Quadrant 1, 2 -ve
Quadrant 3, 4 +ve



Quad 1, 4 -ve
Quad 2, 3 +ve

in case of unsymmetrical loading
 the neutral axis lies an
 angle of " α " the principal
 axis and the algebraic
 sum of stress at N.A.
 is zero

$$\sigma = \frac{M \cos \alpha y}{I_z} + \frac{M \sin \alpha z}{I_y} \rightarrow (1)$$

in this case, N.A. passes through
 z, y so

$$\sigma = \frac{M \cos \alpha y}{I_z} + \frac{M \sin \alpha z}{I_y}$$

Let consider a point "A" on
 N.A. lies in quadrant 2,
 where.

a) Bending stress due to $P \cos \theta$ is compressive.

b) Bending stress due to $P \sin \theta$ is tensile.

$$\text{eq (i)} \Rightarrow 0 = -\frac{M \cos \theta y_A}{I_z} + \frac{M \sin \theta z_A}{I_y}$$

$$\Rightarrow 0 = -\frac{M \cos \theta y_A}{I_z} + \frac{M \sin \theta z_A}{I_y}$$

$$\Rightarrow \frac{M \cos \theta y_A}{I_z} + \frac{M \sin \theta z_A}{I_y}$$

$$\frac{y_A}{z_A} = \frac{I_z}{I_y} \frac{\sin \theta}{\cos \theta}$$

$$\Rightarrow \tan \alpha = \frac{I_z}{I_y} \tan \theta \rightarrow \text{(ii)}$$

Now put values of I_z, I_y & θ in eq (ii)

$$\tan \alpha = \frac{I_x}{I_y} \tan 30$$

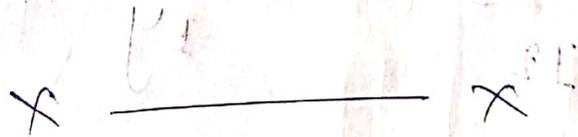
$$\Rightarrow \tan \alpha = \frac{2.8125 \times 10^5 (\tan 30)}{1.25 \times 10^{-5}}$$

$$\tan \alpha = -14.4129$$

$$\alpha = \tan^{-1}(-14.4129)$$

$$\alpha = 1.5^\circ$$

$$\alpha = 1^\circ 30' S''$$



$$(P.T.O)$$

Question # 2

Part # B

GIVEN DATA:

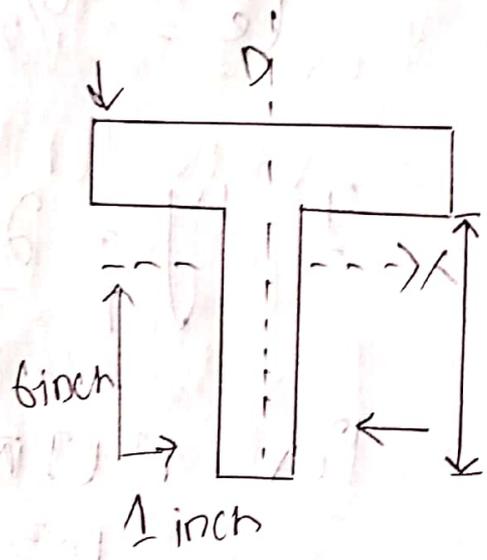
$$L = 10 \text{ ft}$$

$$I_x = 112 \text{ in}^4$$

$$I_y = 18.7 \text{ in}^4$$

$$\sigma_c = 12000 \text{ psi}$$

$$\sigma_t = 5000 \text{ psi}$$



Solution:-

By looking figer

we can judge that

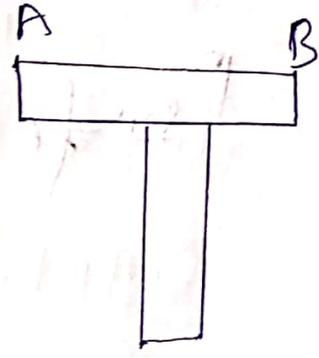
maximum compression would

ocure on a maximum

tension e at B. there

will tension as well a

P.T.O



a compression which will reduce (10)
 that the effect of each other

So we will calculate stress at
 A and C

So,

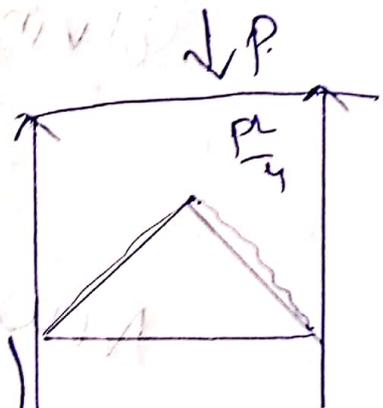
$$\sigma_A = \frac{M_x y}{I_x} + \frac{M_y x}{I_y} \text{ comp}$$

$$\sigma_C = \frac{M_x y}{I_x} + \frac{M_y x}{I_y} \text{ tension}$$

Now $M_x = 48 P \cos 60^\circ$ and $M_y = 48 P \sin 60^\circ$

So

$$M_x = \frac{P \cos 60^\circ (16 \times 12)}{4}$$



$$M_x = 48 P \cos 60^\circ$$

$$M_y = \frac{P \sin 60^\circ (16 \times 12)}{4}$$

$$M_y = 48P \sin 60$$

Now

$$I_x = \frac{M_{xy}}{I_x} + \frac{M_{yx}}{I_y}$$

$$\Rightarrow 1200 = \frac{48P \cos 60 \times 3.07}{112.6} + \frac{48P \sin 60 \times 3}{18.7}$$

Solving the equation

$$P = 1636.6 \text{ lb}$$

Now

$$I_y = \frac{M_{xy}}{I_x} + \frac{M_{yx}}{I_y}$$

$$5000 = \frac{48P \cos 60 \times (5.93)}{112.6} + \frac{48P \sin 60 \times 0.5}{18.7}$$

Solving the equation

$$P = 2104.9 \text{ lb}$$

So the maximum load

(13)

applied should be

1638.6 lb

QUESTION # 3

GIVEN DATA:-

$$\text{length} = 10 \text{ ft}$$

$$E = 10.3 \times 10^6$$

$$b = 0.75$$

$$h = 2$$

factor of safety = 2

Required:

(a) safe load at hinged = ?

(b) safe load at fixed = ?

Solution:-

for hinged columns

$$L_e = L$$

$$I = I_x = \frac{(0.75)(2)^3}{12} = 0.5 \text{ in}^4$$

P.9.0

(b)

$$P_{cr} = \frac{n^2 EI \pi^2}{L_e^2} = \frac{(1)^2 (10.3 \times 10^6) (0.5)^2 \pi^2}{(10 \times 12)^2}$$

$$P_{cr} = \frac{50776940}{14400}$$

$$= 3526.176 \text{ kN}$$

$$P_{\text{safe load}} = \frac{P_{cr}}{\text{Factor of Safety}}$$

$$= \frac{3526.176}{2}$$

$$\Rightarrow 1763.088 \text{ kN}$$

(b) Strut act Column:

$$L_e = L/2 \quad (\text{for fixed ends})$$

$$l_e = 10/2 = 5 \text{ ft}$$

$$I = I_y = \frac{2 \times (0.75)^5}{12} = 0.07 \text{ in}^4$$

$$P_{cr} = \frac{\pi^2 EI \pi^2}{l_e^2} = \frac{(1)^2 (10.3 \times 10^6) (0.07) (3.14)^2}{(5 \times 12)^2}$$

$$P_{cr} = \frac{7108771.6}{(60)^2}$$

$$P_{cr} = 1974.658 \text{ lb}$$

$$P_{\text{safe load}} = \frac{1974.658}{2}$$

$$= 987.3293 \text{ lb}$$

