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Section:- A
Semester:- 6th.
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ASSIGNMENT(I)

1) Venture Flume:-

The term flume is applied to devices in which the flow is locally accelerated due to

↳ A streamlined lateral contraction in channel sides.

↳ The combination of the lateral contraction, together with a streamlined hump in the invert (channel bed)

⇒ A venture flume is a critical flow open flume with a constricted flow which causes a drop in the hydraulic grade line, creating a critical depth.

⇒ Venture flumes are used in open-channels for the measurement of very large flow rates, usually given in millions of cubic units.

⇒ For measurement of discharge with venturi flumes, two measurements are required, which are one upstream and one at the throat, if the flow passes in a sub-critical state through the flumes.

⇒ To ensure the occurrences of critical depth at the throat, the flumes are usually designed in such a way as to form a hydraulic jump on the down-stream side of the structure. These are called standing wave flumes.

Question No:-2

Given Data:-

width of channel (b) = 3m
Q = 12 m³/sec

Solution:-

1. Critical Depth :-

$$q = Q/b = 12/3 \Rightarrow \boxed{q = 4 \text{ m}^2/\text{sec}}$$

Also, the critical depth for rectangular channel is given by;

$$y_c = (q^2/g)^{1/3} = \left(\frac{(4)^2}{9.81}\right)^{1/3} \Rightarrow \boxed{y_c = 1.177 \text{ m}}$$

2. The minimum specific energy :-

$$Q = A \cdot V \text{ --- (1)}$$

$$Q = q \cdot b \text{ --- (2)}$$

But equating the above 2 equations.

$$Q = Q$$

$$A \cdot V = q \cdot b$$

$$b \cdot y \cdot V = b \cdot q$$

$$q = y \cdot V \Rightarrow \boxed{V = q/y_c}$$

putting values in equation.

$$V = 4/1.177 \Rightarrow \boxed{V = 3.398 \text{ m/sec}}$$

As we know that;

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$$y = y_c, \quad v = v_c$$

Hence;

$$E_{min} = y_c + \frac{(v_c)^2}{2g}$$
$$= 1.177 + \frac{(3.398)^2}{2(9.81)}$$

$$E_{min} = 1.76m$$

3. Then Alternate Depth when $E = 4m$:

We know that,

$$E = y + \frac{v^2}{2g} \Rightarrow E = y + \frac{Q^2/A^2}{2g}$$

$$E = y + \frac{Q^2}{2g \cdot A^2} \Rightarrow E = y + \frac{Q^2}{2g \cdot B^2 y^2} = y + \frac{q^2}{2g \cdot y^2}$$

putting values;

$$E = y + \frac{(4)^2}{2(9.81) \times y^2} \Rightarrow 4 = y + \frac{(4)^2}{2(9.81)} \times \frac{1}{y^2}$$

$$y = 4 - \frac{16}{19.62} \times \frac{1}{y^2} \Rightarrow y = 4 - 0.815 \times \frac{1}{y^2}$$

$$y = 4 - \frac{0.815}{y^2}$$

From iteration at $y = 4m$ we get;

$$y = 3.948m \approx \boxed{3.95m}$$

=> From the super-critical ⁽⁴⁾ solution, the 2nd term associated with $k \cdot E$ dominates.

So, rearrange as;

$$\sqrt{y^3} = \sqrt{\frac{0.815}{4-y}}$$

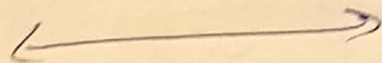
$$y = \sqrt{\frac{0.815}{4-y}}$$

From iteration at $y = 4m$. we get;

$$y = 0.4814m \approx 0.482m$$

Hence alternate depth are

3.95m and 0.482m



ASSIGNMENT (2) :- Q1

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1) Given Data :-

Depth of water (d) = 10 cm = 0.1 m

Velocity, $V = 6$ m/sec

Solution :-

Using Froude Number.

$$Fr = \frac{V}{\sqrt{gy}} \Rightarrow \frac{6}{\sqrt{9.81 \times 0.1}} \quad \boxed{Fr = 6.06}$$

As $Fr > 1$

$6.06 > 1 \rightarrow$ The flow is super-critical.

Now for alternate depth.

Using specific energy formula

$$E = y + \frac{V^2}{2g} = 0.1 + \frac{(6)^2}{2(9.81)}$$

$$\boxed{E = 1.9348}$$

~~0.8~~

So, $E = 1.9348$ yields the depth $y = 1.93$ m.



Q-2

Given Data:-

velocity, $v = 2 \text{ m/sec}$

water depth (y) = 3 m

Change in bottom elevation = $60 \text{ cm} = 0.6 \text{ m}$.

Gradual downward step = 15 cm .

Solution:-

We know that;

$$E_1 = y_1 + \frac{v_1^2}{2g} = 3 + \frac{(2)^2}{2(9.81)} = \boxed{3.20 \text{ m}}$$

For downward step.

$$E_2 = E_1 - \Delta Z$$
$$= 3.20 - 0.60$$

$$\boxed{E_2 = 2.60 \text{ m}}$$

Now By using formula.

$$E_2 = y_2 + \frac{(v_2)^2}{2g}$$

$$E_2 = y_2 + \frac{(Q/A)^2}{2g} \Rightarrow E_2 = y_2 + \frac{Q^2}{2g \cdot A^2}$$

$$E_2 = y_2 + \frac{Q^2}{2g \cdot B^2 \cdot y^2} = y_2 + \frac{q^2}{2g \cdot y^2}$$

Now putting values

$$E_2 = y_2 + \frac{q^2}{2g \cdot y_2^2}$$

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 $\left(\begin{array}{l} q = v_1 y_1 \\ q = 2 \times 3 \\ = 6 \text{ m}^2/\text{sec} \end{array} \right)$

$$2.60 = y_2 + \frac{(6)^2}{2(9.81)(y_2)^2}$$

$$\boxed{y_2 = 2.34 \text{ m}}$$

Hence, change in depths;

$$\Delta y = y_2 - y_1 \\ = 2.34 - 3$$

$$\boxed{\Delta y = 0.76 \text{ m}}$$

$$\text{So, the change in upset} = 0.76 - 0.6 \\ = 0.16$$

Hence water surface drops 0.16m.

\Rightarrow Now for downward step,

$$E_2 = E_1 - \Delta Z$$

$$= 3.20 - (-0.15) \quad (\text{-ive sign of } 0.15 \text{ due to downward direction})$$

$$\boxed{E_2 = 3.35 \text{ m}}$$

Also from above formula -

$$E_2 = y_2 + \frac{q^2}{2g \cdot (y_2)^2} \Rightarrow 3.35 = y_2 + \frac{(6)^2}{2(9.81) \times y_2^2}$$

$$\boxed{y_2 = 3.17 \text{ m}}$$

$$\text{So, } \Delta y = 3.17 - 3 = \boxed{0.17 \text{ m}}$$

$$\Rightarrow \text{Also the water in downstep} = 0.15 - 0.17 = \boxed{0.02}$$

Hence water rises to 0.02m.

P.T.O

Now, the maximum upstep possible before affecting upstream water lesser is for ⁽⁸⁾

$$y_2 = y_c$$

Hence;

$$y_c = \sqrt[3]{\frac{q^2}{g}}$$

$$y_c = \left(\frac{q^2}{g}\right)^{1/3}$$

$$y_c = \left(\frac{(6)^2}{9.81}\right)^{1/3}$$

$$y_c = 1.54 \text{ m}$$



Assignment (III):-

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Given Data:-

Water depth on upstream side (y_1) = 3.6m
Water depth at downstream side (y_2) = 0.9m
Width of sluice gate (b) = 3.9m

Solution:-

As we know that.

$$E_1 = E_2$$

$$y_1 + \frac{V_1^2}{2g} = y_2 + \frac{V_2^2}{2g} \quad \text{--- (1)}$$

Also, by discharge formula;

$$Q = A_1 V_1 = A_2 V_2$$

$$b_1 y_1 V_1 = b_2 y_2 V_2$$

$$b \cdot y_1 V_1 = b y_2 V_2$$

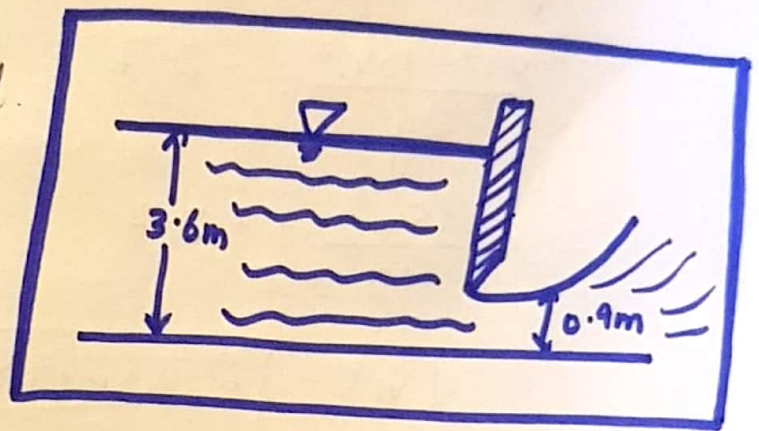
$$y_1 V_1 = y_2 V_2$$

$$V_2 = \frac{y_1}{y_2} \times V_1$$

$$= \frac{3.6}{0.9} \times V_1$$

$$\boxed{V_2 = 4V_1} \quad \text{--- (2)}$$

putting values in eq (1)



$$\therefore \boxed{b = b_1 = b_2}$$

$$y_1 + \frac{v_1^2}{2g} = y_2 + \frac{v_2^2}{2g}$$

$$3.6 + \frac{v_1^2}{2g} = 0.9 + \frac{(4v_1)^2}{2g}$$

$$3.6 + \frac{v_1^2}{2g} = 0.9 + \frac{16v_1^2}{2g}$$

$$\frac{v_1^2}{2g} - \frac{16v_1^2}{2g} = 0.9 - 3.6$$

$$\frac{v_1^2 - 16v_1^2}{2g} = -2.7$$

$$\frac{-15v_1^2}{2g} = -2.7$$

$$\sqrt{v_1^2} = \sqrt{\frac{2.7 \times 2(9.8)}{15}}$$

$$v_1 = 1.879 \text{ m/sec}$$

putting value of v_1 in eq (2)

$$v_2 = 4v_1$$

$$v_2 = 4(1.879)$$

$$v_2 = 7.516 \text{ m/sec}$$

Also;

$$Q_1 = A_1 v_1$$

$$= b y_1 v_1 = 3.9 \times 3.6 \times 1.879$$

$$Q_1 = 26.38 \text{ m}^3/\text{sec}$$

$$Q = Q_1 = Q_2 = 26.38 \text{ m}^3/\text{sec}$$

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Now;

Froude no. on upstream side :-

$$Fr_1 = \frac{V_1}{\sqrt{gy_1}} = \frac{1.879}{\sqrt{9.81 \times 3.6}}$$

$$\boxed{Fr_1 = 0.31}$$

As $Fr_1 < 1$

$0.31 < 1 \rightarrow$ subcritical flow.

Froude no. on downstream side :-

$$Fr_2 = \frac{V_2}{\sqrt{gy_2}} = \frac{7.516}{\sqrt{9.81 \times 0.9}}$$

$$\boxed{Fr_2 = 2.52}$$

As $Fr_2 > 1$

$2.52 > 1 \rightarrow$ supercritical flow.

←—————→
End!