

Linear Algebra

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Linear Algebra

Q1:-

16002

$$(i) \begin{bmatrix} 1 & 0 & 3 & 0 & 5 \\ 0 & 1 & 2 & 0 & 7 \\ 0 & 0 & 1 & 0 & -6 \\ 0 & 0 & 0 & 1 & 0 \end{bmatrix}$$

We are applying $R_2 + 2R_3$ on the next matrix

 $R_2 + 2R_3$

$$(ii) \begin{bmatrix} 1 & 0 & 3 & 0 & 5 \\ 0 & 1 & 0 & 0 & -5 \\ 0 & 0 & 1 & 0 & -6 \\ 0 & 0 & 0 & 1 & 0 \end{bmatrix}$$

Here we got 1's in diagonal and 0's in each term except first row and 3rd column. after getting the right order we need to apply $R_1 - 3R_3$

 $R_1 - 3R_3$

$$(iii) \begin{bmatrix} 1 & 0 & 0 & 0 & -13 \\ 0 & 1 & 0 & 0 & -5 \\ 0 & 0 & 1 & 0 & -6 \\ 0 & 0 & 0 & 1 & 0 \end{bmatrix}$$

\Rightarrow Here we got the exact matrix which have 1's in diagonal and 0's at the right and left sides

Q2: (A)

Transform of the first matrix
into second.

$$\begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 2 & -5 & -1 \end{bmatrix} \begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 0 & 3 & -5 \end{bmatrix}$$

$$\begin{matrix} & & 2R_2 + R_3 & \\ \begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 2 & -5 & -1 \end{bmatrix} & \begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 2 & -5 & -1 \end{bmatrix} \end{matrix}$$

Transform of the 2nd matrix
into 1st.

$$\begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 2 & -5 & -1 \end{bmatrix} \begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 0 & 3 & -5 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 2 & -5 & -1 \end{bmatrix} \xrightarrow{3R_2 + R_3} \begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 5 & -17 & 5 \end{bmatrix}$$

$$\Rightarrow \begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 5 & -17 & 5 \end{bmatrix} \xrightarrow{-3R_2 + R_3} \begin{bmatrix} 1 & 3 & -1 & 5 \\ 0 & 1 & -4 & 2 \\ 0 & 2 & -5 & -1 \end{bmatrix}$$

Q2: (B)

(a) Row Echelon form.

→ (Because the all constants in diagonals are not = 1)

(b) Reduced row Echelon form.

(Because the diagonal are = 2 and the digits above & below the 1's are all = 0).

(c) Reduced row Echelon form.

(Because all the digits above and below the diagonals are 0)

(d) Reduced Echelon form.
diagonal = 1.

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Q3

(A)

P#4

Row Echelon form

- The first non zero number from the left (the leading coefficient) is always to the right of first non zero number in row, above.
- Rows consist of all zeros are at the bottom of matrix.

$$\begin{bmatrix} 1 & 2 & 3 & 4 & 5 \\ 0 & 0 & 2 & 4 & 3 \\ 0 & 0 & 0 & 1 & 2 \end{bmatrix}$$

Reduced Row Echelon form.

- The first non zero number in first row is 1.
- The 2nd row also start with 1. which is also to the right than the lead only in 1st row.
- Any non zero are placed at bottom of matrix.

$$\begin{bmatrix} 1 & 0 & 4 & 0 & 1 \\ 0 & 1 & 2 & 0 & 1 \\ 0 & 0 & 0 & 1 & 3 \end{bmatrix}$$

Practical Used of Reduced row Echelon form.

" In any of our daily life statistical analysis RREE helps us to Count, identify the Pivot Columns In short to examining the highlighted figure.

P#5

Q3 (B) $16002 = ID$

$$\begin{bmatrix} 1 & 6 & 8 \\ 2 & 8 & -1 \\ 0 & 0 & 0 \\ 1 & -4 & 12 \end{bmatrix}$$

$2R_1 - R_2$

$$\begin{bmatrix} 1 & 6 & 8 \\ 1 & 4 & 17 \\ 0 & 0 & 0 \\ 1 & -4 & 12 \end{bmatrix}$$

$R_1 - R_4$

$$\begin{bmatrix} 1 & 6 & 8 \\ 0 & 4 & 17 \\ 0 & 0 & 0 \\ 0 & 10 & -4 \end{bmatrix}$$

$5R_2 - 2R_4$

$$\begin{bmatrix} 1 & 6 & 8 \\ 0 & 4 & 17 \\ 0 & 0 & 0 \\ 0 & 0 & 93 \end{bmatrix} \quad R_3 \cong R_4$$

\Rightarrow

$$\begin{bmatrix} 1 & 6 & 8 \\ 0 & 4 & 17 \\ 0 & 0 & 93 \\ 0 & 0 & 0 \end{bmatrix}$$

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