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Section B

Semester 6<sup>th</sup>

Subject Plain & Reinforced Concrete  
Design - I

Submitted To,

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Q NO(01):-

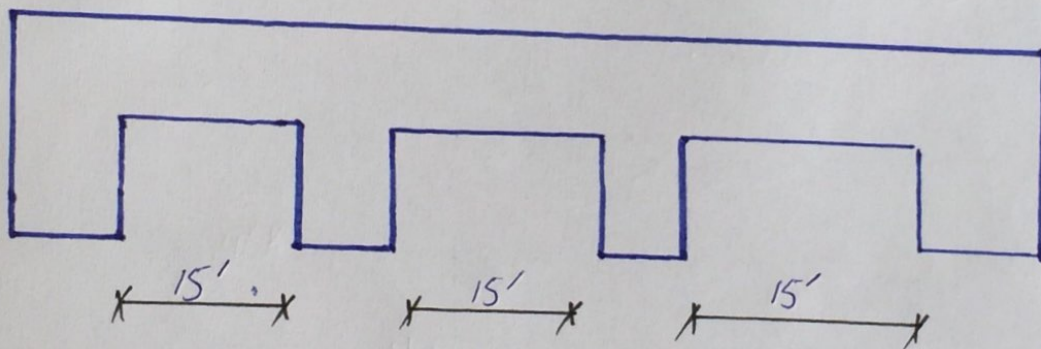
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Given Data:-

- ⊙ 3 equal Spans Concrete slab
- ⊙ Clear Span b/w Support = 15 ft
- ⊙ Factored Live load =  $160 \text{ lb/ft}^2$
- ⊙ Service Floor Finish load =  $20 \text{ lb/ft}^2$
- ⊙  $f'_c = 4000 \text{ psi}$
- ⊙  $f_y = 40 \text{ ksi}$

Solution:-



Step 1 Minimum thickness:

According to Formula

$$t_{\min} = \frac{l}{28} = \frac{15}{22} = 6.4 \approx 6.5''$$

As  $f_y \rightarrow 40 \text{ ksi}$

So we will multiply a factor

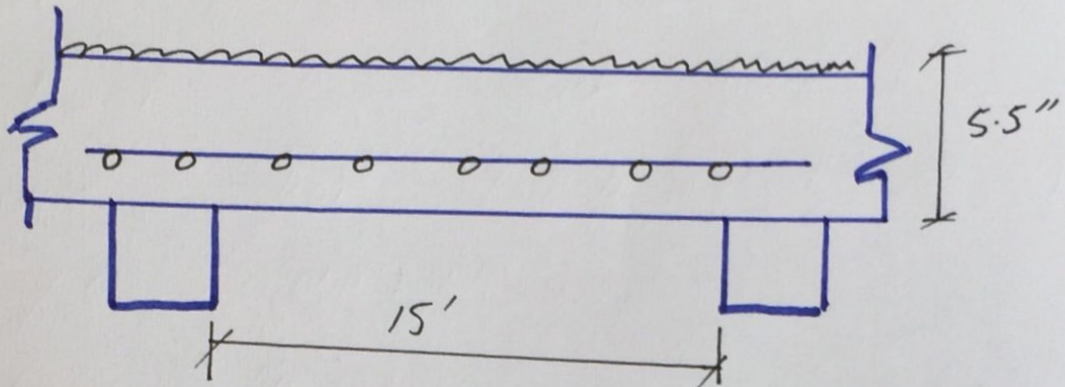
with this thickness. Factor =  $\left(0.4 + \frac{f_y}{1000}\right)$

$$\text{Factor} = 0.8$$



Hence the minimum thickness will be  $6.5 \times 0.8$   
 $t_{min} = 5.2 \approx 5.5''$

Step ②:- Effective depth:-



By Formula

$$d = t - \text{clear cover} - \frac{1}{2} (\text{dia. of main bar})$$

$$= 5.5 - 0.75 - \frac{1}{2} (5/8)$$

$$d \approx 4.5''$$

Step ③:- Self weight of slab:-

By Formula

$$\frac{t}{12} * \gamma_{\text{concrete}}$$

$$= \frac{5.5}{12} * 150 = 68.75 \text{ lb/ft}^2$$

Step ④:- Total Factored load:-

$$\text{Factored load} = 160 \text{ lb/ft}^2$$

So the Factored Dead load will be ;



$$D.L = 1.2 (20 + 68.75) = 106.5 \text{ lb/ft}^2$$

$$\begin{aligned} \text{Total Factored load} &= D.L + L.L \\ &= 106.5 + 160 \\ &= 266.5 \text{ lb/ft}^2 \end{aligned}$$

Step ④⑤:- Ultimate Moment:-  $0.2665 \text{ K/ft}^2$

According To Formula

$$M_u = \frac{w_u \times l^2}{8} = \frac{0.2665 \times (15)^2}{8}$$

$$M_u = 89.94 \text{ Kip-inches}$$

Step ⑥:- Area of Steel For main Bars  
By Trial and repeat method:-

Trial ① let depth of compression block

$$a = 0.2 \times t$$

$$= 0.2 \times 5.5 = 1.1''$$

$$\left. \begin{array}{l} f_c = 0.55 \\ 142.2 \end{array} \right\}$$

$$A_{st} = \frac{M_u}{\phi \times f_y (d - a/2)} = \frac{89.94}{0.9 \times 40 (4.5 - 1.1/2)}$$

$$A_{st} = 0.63 \text{ in}^2$$

Trial ②

$$a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b} = \frac{0.63 \times 40}{0.85 \times 40 \times 12}$$

$$a = 0.62''$$



$$A_{st} = \frac{m_u}{\phi * f_y * (d - \frac{a}{12})} = \frac{89.94}{0.90 * 40 * (45 - \frac{0.63}{2})}$$

$$A_{st} = \cancel{0.63 \text{ in}^2} \quad 0.59 \text{ in}^2$$

Trail ③

$$a = \frac{0.59 * 40}{0.85 * 4 * 12} = 0.57''$$

$$A_{st} = \frac{89.94}{0.90 * 40 * (45 - \frac{0.57}{2})} = 0.59 \text{ in}^2$$

So we used  $A_{st} = 0.59 \text{ in}^2$

Step ⑦:

Area of steel for distribution reinforcement using formula

$$A_{min} = 0.002 * b * t \rightarrow (\text{For grad 40 steel})$$

$$= 0.002 * 12 * 5.5 = 0.132 \text{ in}^2$$

Step ⑧ using formula

Spacing  $\frac{A_b * 12}{A_{st}}$   
we used #6 bar dia =  $(\frac{6}{8})''$

$$\text{Area } \frac{\pi}{4} (\frac{6}{8})^2 = 0.442 \text{ in}^2$$



Step 9: Spacing For distribution bars:-

$$\text{Spacing} = \frac{A_b}{A_{st}} \text{ used \#5 bar}$$

So

$$\text{dia} = \left(\frac{5}{8}\right)'' \quad \text{Area} = \frac{\pi}{4} \left(\frac{5}{8}\right)^2 = 0.31 \text{ in}^2$$

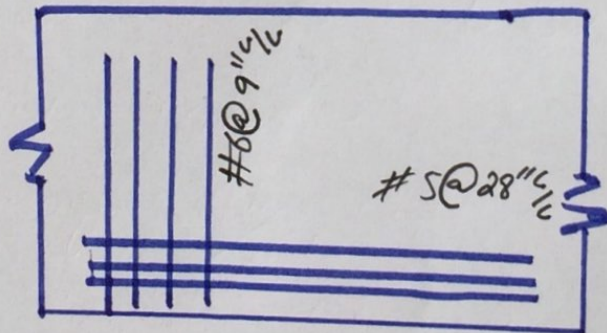
$$\text{Spacing} = \frac{0.31}{0.132} * 12 = 2.8'' \approx 28'' \text{ c/c}$$

Step 10 Final Sketch Finding:-

$$f'_c = 4 \text{ ksi}, \quad f_y = 40 \text{ ksi}$$

Main Steel #6 at 9" c/c

Distribution Steel #5 at 28" c/c



QNO(02) :-

Solution :-

First we will find unit load of beam.

$$\text{As } b \times d_c = \frac{16}{12} \times 150 = 200 \text{ lb/ft}$$

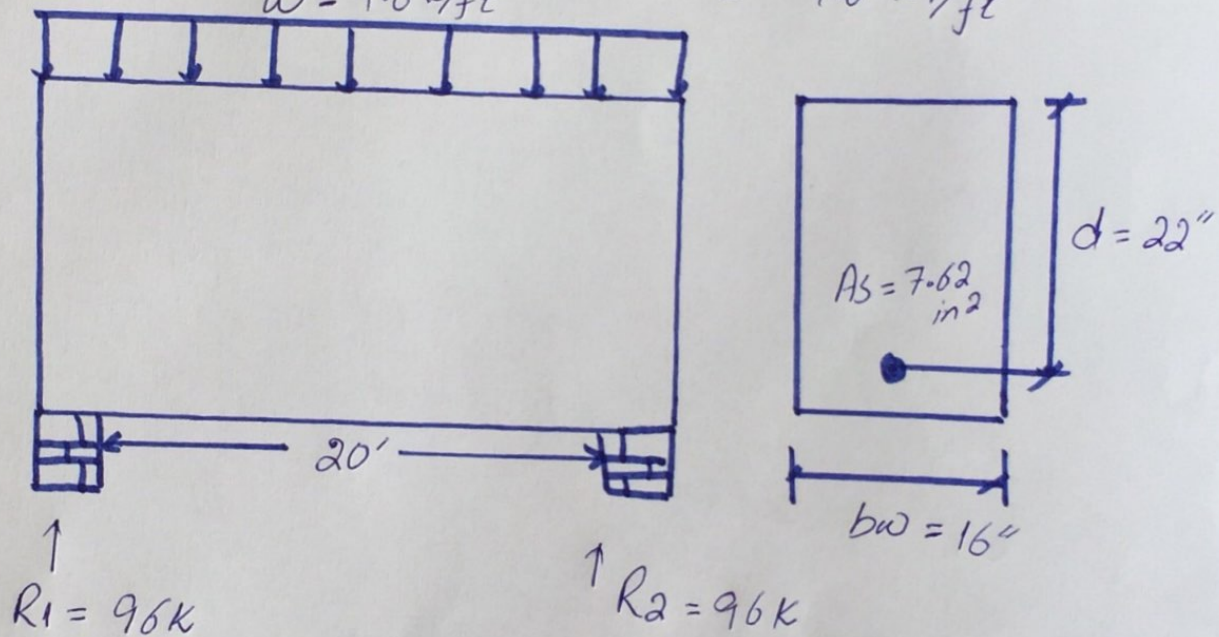
Now

$$\text{or } = 0.2 \text{ kip/ft}$$

$$\text{Total Factored load} = 9.4 + 0.2$$

$$w = 9.6 \text{ k/ft}$$

$$= 9.6 \text{ kip/ft}$$



Step 1 :-

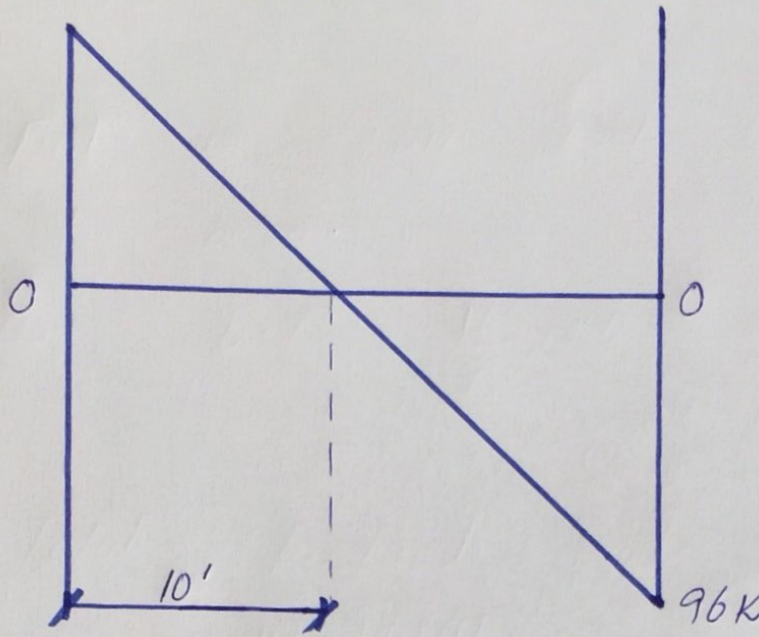
Find the value of  $R_1$  and  $R_2$

$$\text{Total load} = 9.6 \times 20 = 96 \text{ k}$$



Step ② :- "Draw its Shear Force diagram"

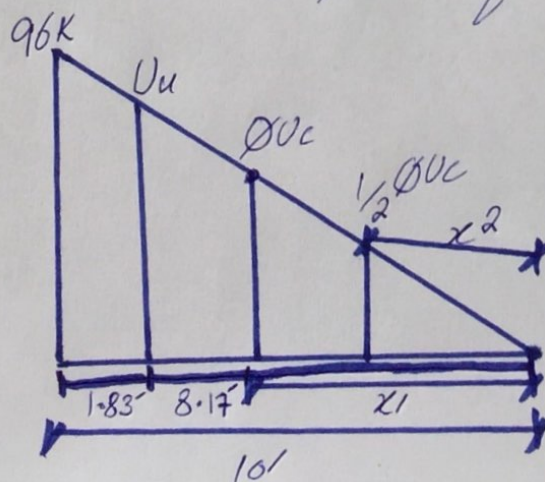
SFD (Kips)



Step ③ :- Find the value of critical <sup>stress ( $U_u$ )</sup> section and its location. ~~at~~

As we know that critical section is located at distance "d" from face of support =  $d = 22" = 1.83'$

Value of critical shear at distance 'd' by similarity of triangles.



From Similarity

$$\Delta's \quad \frac{96}{10} = \frac{U_u}{8.17}$$

$$U_u = 78.43 \text{ k}$$



Step 4:- Find the value of " $\phi U_c$ " and " $\frac{1}{2} \phi U_c$ " and also its distance from zero shear to right side.

$$\begin{aligned} \phi U_c &= \phi * 2 * \sqrt{f'c} * bw + d \\ &= \frac{0.75 * 2 * \sqrt{4000} * 16 + 22}{1000} \end{aligned}$$

$$\phi U_c = 33.40 \text{ K}$$

Location of  $\phi U_c$  by Similarity of  $\Delta$ 's

$$\frac{96}{10} = \frac{33.04}{x_1}$$

$$x_1 = 3.48'$$

Now  $\frac{1}{2} \phi U_c = \frac{33.04}{2} = 16.70 \text{ K}$

Location of  $\frac{1}{2} \phi U_c = \frac{96}{10} = \frac{16.70}{x_2}$

$$x_2 = 1.074'$$

Step 5:- Value of  $\phi U_s$  ( $U_s = \phi U_s + \phi U_c$ )

So  $\phi U_s = U_a - \phi U_c$

$$\phi U_s = 78.43 - 33.04$$

$$\phi U_s = 45.03 \text{ K}$$



Step ⑥:- Check on Section adequacy:-

$$\phi * 8 * \sqrt{f'c} * bw * d = \frac{0.75 * 8 * \sqrt{4000} * 16 * 22}{1000}$$

$$= 133.57K$$

As  $\phi * 8 * \sqrt{f'c} * bw * d > \phi U_s$

It mean that Section is adequate.

Step ⑦:- Check on Maximum Spacing For Stirrups:-

$$\phi * 4 * \sqrt{f'c} * bw * d = \frac{0.75 * 4 * \sqrt{4000} * 16 * 22}{1000}$$

$$= 66.79K$$

As  $\phi * 4 * \sqrt{f'c} * bw * d > \phi U_s = 45.03K$

Thus the maximum Spacing will be Selected from following For conditions.

①  $S_{max} = 24''$

②  $\frac{d}{2} = \frac{22}{2} = 11''$

③  $A_u = 0.22$   
④  $f_y = 60000$

③  $S_{max} = \frac{A_u * f_y}{0.75 * \sqrt{f'c} * bw} = 17.40''$  ⑤  $A_u = 0.22$

④  $S_{max} = \frac{A_u * f_y}{50 * bw}$



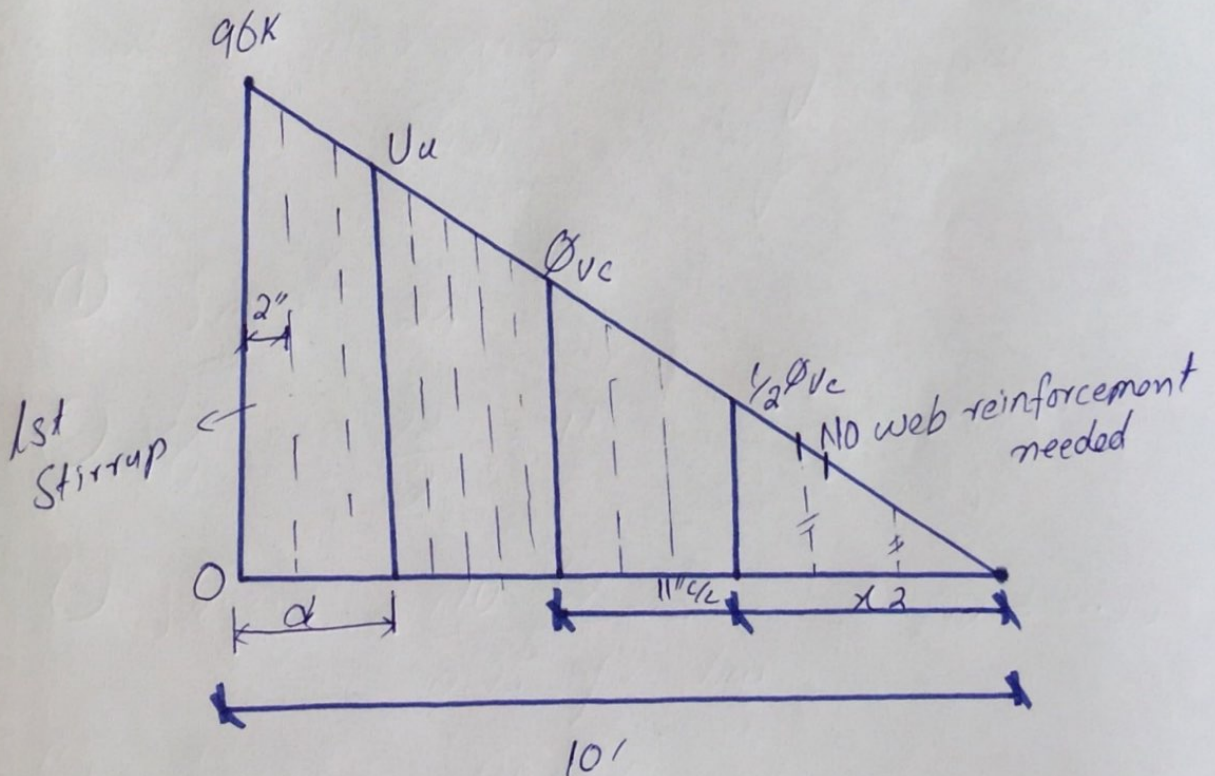
$$f_{max} = \frac{0.22 \times 60000}{50 \times 16} = 16.50''$$

From the above four condition last value of Spacing from #3, U Spad will be selected So,  $f_{max} = 11'' c/c$

Step 8:- Spacing of Stirrup From/ at critical Section:-

$$f = \frac{\phi \times A_v \times f_y \times d}{U_u - \phi V_c} = \frac{0.75 \times 0.22 \times 60 \times 22}{78.43 - 33.40} = 48.4'' \approx 5'' c/c$$

Step 9:- Final Sketch:-





QNO(03) :-

Step ① :- Find gross area of concrete :-

$$A_g = b \times b \text{ (Since it is Squared column)}$$

$$A_g = 12 \times 12 = 144 \text{ in}^2 \text{ (Actual)}$$

Step ② :- Find gross area of concrete :-

$$\text{Since } A_s = 5\% \text{ of } A_g$$

$$= 0.05 \times 144$$

$$A_s = 7.2 \text{ in}^2$$

Step ③ :- Ultimate load carrying capacity

$$P_u = \phi \times 0.80 \times [0.85 \times f'_c \times (A_g - A_s) + A_s \times f_y]$$

$$= 0.65 \times 0.80 [0.85 \times 4 [144 - 7.2) + 7.2 \times 60]$$

$$P_u = 466.5 \text{ DK}$$



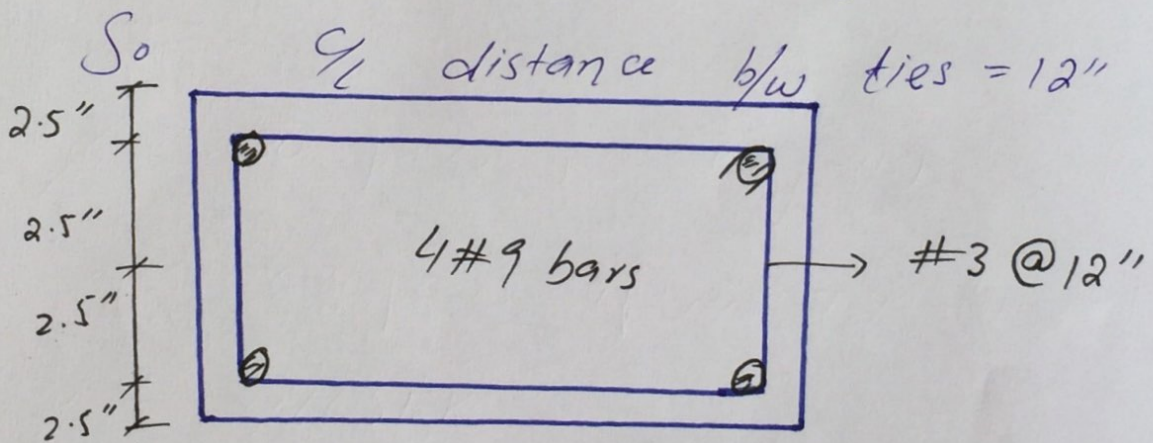
Step 4 :- Sketch (Design of ties)  $\frac{1}{2}$  to distance

From  $L_{10}$  above value we chose the least value of all these.

$$\textcircled{1} \quad 16 \times \text{dia of long bar} = 16 \times \frac{9}{8} = 18''$$

$$\textcircled{2} \quad 48 \times \text{dia of tie bar} = 48 \times \frac{3}{8} = 18''$$

$$\textcircled{3} \quad \text{least column dimension} = 12''$$



Since it is a tied square column so there is no spiral strip used is of rectangular shape due to the specification of the structure there we will use tie stirrups instead. //



Q NO(04) :-

Solution :-

Step (1) Let  $h = 24''$

Step (2) Total weight = wt of soil + wt of  
of  $R_c$

$$= 3 \times 120 + 2 \times 150 = 660 \text{ Ksf}$$

$$= 0.660 \text{ Ksf}$$

Step (3) Effective Bearing Capacity :-

$$q_e = q_a - w = 2.5 - 0.660$$

$$q_e = 1.84 \text{ Ksf}$$

Step (4) Required area For Foundation :-

$$A_{req} = \frac{\text{Service Load}}{q_e} = \frac{100 + 20}{1.84}$$

$$A_{req} = 119.56 \text{ ft}^2$$



Step (5)

Since foundation is Square

$$A_{req} = B \times B = 19.56 \Rightarrow B = 10.934$$

$$B \approx 11'$$

Step (6)

upward bearing Capacity

$$V_{up} = \frac{\text{Factored load}}{(B)^2}$$

$$= \frac{1.2(100) + 1.6(20)}{(10.934)^2}$$

$$V_{up} = 2.609 \text{ K/ft}^2$$

Step (7)

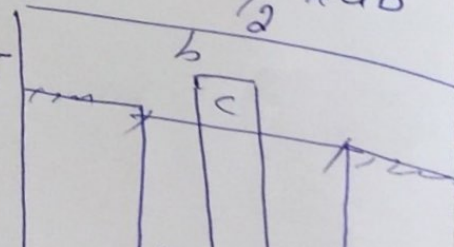
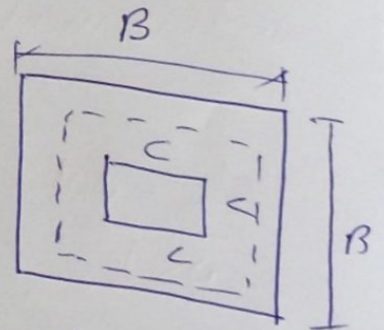
punching shear

$$b_o = 4 * (c + d)$$

$$d = h - \text{clear cover} - \text{dia of bar} - \frac{1}{2} * d_o$$

$$= 24 - 3 - 1 - \frac{1}{2} * 1 = 19.5$$

$$b_o = 4 * (16 + 19.5) = 142''$$





Step 8

$$V_{u2} = V_{up} * (B^2 - (c+d)^2)$$

$$= 2.609 * \left[ (10.934)^2 - \left( \frac{16+19.5}{12} \right)^2 \right]$$

$$V_{u2} = 229.078 \text{ k}$$

Step 9

$$\phi V_{c/p} = \phi * 4 * \sqrt{f'_c} * b_o * d$$

$$= \frac{0.75 * 4 * \sqrt{3000} * 192 * 19.5}{1000}$$

$$\phi V_{c/p} = 454.993 \Rightarrow \underline{\underline{\text{OKey}}}$$

Step 10

Beam Shear (one way shear check)

$$V_{u1} = V_{up} * B * \left( \frac{B}{2} - \frac{1}{2} - d \right)$$

$$= 2.609 * 10.934 * \left( \frac{10.934}{2} - \frac{16}{2} - \frac{19.5}{2} \right)$$

$$V_{u1} = 90.58$$

$$V_{u2} > V_{u1}$$



Step (11) Self Shear capacity

$$\phi V_c = \phi \times 2 \sqrt{f_c} \times B \times d$$

$$= \frac{0.75 \times 2 \sqrt{3000} \times (10.934 \times 12) \times 19.5}{1000}$$

$$= 105.10 > V_{u1} \text{ Okey}$$

Step (12) Ultimate moment

$$M_u = \frac{V_{u1} \times B}{8} \times (B - c)^2$$

~~$$M_u = \frac{2.609 \times 10.934}{2} \times \left(10.934 - \frac{16}{12}\right)^2$$~~

$$M_u = \frac{2.609 \times 10.934}{2} \times \left(10.934 - \frac{16}{12}\right)^2$$

$$M_u = 328.67 \text{ k'} = 3944.07 \text{ k''}$$

Step (13) Area of Steel for main bars  
by Trial Repeated method



Trial ①

$$\text{let } a = 0.2 \times h = 0.2 \times 24 = 4.8''$$

$$A_s = \frac{m_u}{\phi \times f_y \left(d - \frac{a}{2}\right)}$$

$$= \frac{3944.09}{0.9 \times 60 \times \left(11 - \frac{4.8}{2}\right)} = \boxed{18.56 \text{ in}^2}$$

Trial ②

$$a = \frac{4.2 \times 60}{0.85 \times 3 \times 11 \times 12} = 1.53''$$

Trial ③

$$a = 1.28$$

$$\boxed{A_s = 7.1 \text{ in}^2}$$

Step (14)

checked main reinforcement

$$A_{s \text{ min}} = 0.0018 \times B \times h = 0.0018 \times (10.934 \times 12) \times 24$$

$$\boxed{A_{s \text{ min}} = 5.70 \text{ in}^2}$$



Step (15)

using #8 bar

$$\text{No. of bars} = \frac{A_s}{A_b} = \frac{8.58}{0.785}$$

$$= 10.92 \approx 11 \text{ bars in}$$

each direction.

End