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Subject Digital logic and Design (theory)

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QNO2: (a)  $45.25_{10} = ( )_2$

Sol:

$$\begin{aligned}
 & 45.25 \\
 &= (4 \times 10^1) + (5 \times 10^0) + (2 \times 10^{-1}) + (5 \times 10^{-2}) \\
 &= (4 \times 10) + (5 \times 1) + (2 \times 0.2) + (5 \times 0.01) \\
 &= 40 + 5 + 0.2 + 0.05
 \end{aligned}$$

(b)  $10000000.1010_2 = ( ? )_{10}$

Sol:

$$\begin{aligned}
 & 10000000.1010 \\
 & 2^7 + 2^6 + 2^5 + 2^4 + 2^3 + 2^2 + 2^1 + 2^0 + 2^{-1} + 2^{-2} + 2^{-3} + 2^{-4} \\
 & 128 + 64 + 32 + 16 + 8 + 4 + 2 + 1 + 0.5 + 0.25 + 0.125 + 0.0625
 \end{aligned}$$

$$10000000.1010_2 = (255.9375)_{10}$$

(c)  $4D7F_{16} = ( )_{10}$

$$= (4 \times 16) + (13 \times 16) + (7 \times 16) + (15 \times 16)$$

$$= 64 + 208 + 112 + 240$$

$$= 624_{10}$$

(d)  $128_{10} = ( ? )_{16}$

Sol:

$$\frac{128}{16} = 8 \rightarrow 8 \times 16 = \mathbf{80}$$

$$\frac{8}{16} = 0.5 \rightarrow 0.5 \times 16 = 8$$

$$(808)_{16}$$

$$(e) 3A6F_{16} = (?)_{10}$$

$$(3 \times 16) + (A \times 16) + (6 \times 16) + (F \times 16)$$

$$(3 \times 16) + (10 \times 16) + (6 \times 16) + (15 \times 16)$$

$$48 + 160 + 96 + 240$$

$$= (544)_{10}$$

$$(f) 110000111100101_2 = (?)_{16}$$

$$2^{15} + 2^{14} + 2^{13} + 2^{12} + 2^{11} + 2^{10} + 2^9 + 2^8 + 2^7 + 2^6 + 2^5 + 2^4 + 2^3$$

~~$$4096 + 2048 + 1024 + 512 + 256 + 128 + 64 + 32$$~~

$$32768 + 16384 + 8192 + 4096$$

$$2^2 + 2^1 + 2^0$$

$$2048 + 1024 + 512 + 256 + 128 + 64 + 32$$

$$16 + 8 + 4 + 1$$

~~65~~

$$110000111100101$$

$$E \quad 3 \quad E \quad 5$$

$$110000111100101_2 (C3E5)_{16}$$

$$(g) 6173_8 = (?)_{10}$$

$$(6 \times 8^3) + (1 \times 8^2) + (7 \times 8^1) + (3 \times 8^0)$$

$$(6 \times 512) + (1 \times 64) + (7 \times 8) + (3 \times 1)$$

$$3072 + 64 + 56 + 3$$

$$= (3193)_{10}$$

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(h)  $169_{10} = (?)_8$

$$1 \times 10^2 + 6 \times 10^1 + 9 \times 10^0$$

$$1 \times 100 + 6 \times 10 + 9 \times 1$$

$$100 + 60 + 9$$

$$(169)_8$$

(i)  $2A7D_{16} = (?)_8?$

$$(2 \times 16^3) + (A \times 16^2) + (7 \times 16^1) + (D \times 16^0)$$

$$(2 \times 16^3) + (9 \times 16^2) + (7 \times 16^1) + (13 \times 16^0)$$

$$(2 \times 4096) + (9 \times 256) + (7 \times 16) + (13 \times 1)$$

$$8192 + 2304 + 112 + 13$$

$$10621_8$$

(j)  $11111111 = (?)_{10}$

$$\begin{array}{r} \text{11111111} \\ \text{Add 1} \\ \hline \text{11111111} \end{array} \quad \begin{array}{l} \text{2nd} \\ \text{1st complement} \end{array}$$

$$\begin{array}{r} + \quad \quad \quad 1 \\ \text{11111111} \\ \text{Add 1} \\ \hline \text{11111111} \end{array} \quad \begin{array}{l} \text{2nd complement} \end{array}$$

$$\text{11111111} \quad (11111111)_{10}$$

(k)  $-12_{10} = ( )_2$

$$\begin{array}{r} 0000110 \\ \underline{\phantom{0000}11} \\ 0000111 \end{array}$$

$-12_{10} = (0000111)_2$

(l)  $198_{10} = ( ? )_{BCD}$

198

0001 1001 1000

$198_{10} = 000110011000$

(m)  $100001110000 = ( )_{10}$

1000 0111 0000  
8 1 0

$810_{10}$

(n)  $1001010_2 = ( )_{Gray}$

1001010  
Binary to Gray

$(1101110)_{Gray}$

(c)  $10101111_{\text{Gray}} = (?)_2$

$1010 \quad 1111$   
 $(11101001)_2$

(d)  $01000001 = (?)_{\text{ASCII}}$

$01000001 = (22)_{\text{ASCII}}$   
 Symbol  
 "

(e)  $111000 = (?111000)_{\text{Even parity}}$

111000 is even  
 its divisible by 2  
 remainder = 0

$(111000)_{\text{Even parity}}$

QNO2:

(a)  $01111111_2 - 00000111_2$

$01111111$   
 $- 00000111$   


---

$01111000$   
 $+ 1$

using 2nd complement

---

 $01111001$

(b)  $01101010_2 \times 11110001_2$

$$\begin{array}{r} 01101010 \\ \times 11110001 \\ \hline 01100080 \\ \phantom{01100080} 1 \\ \hline 01100001 \end{array} \quad \text{2nd complement}$$

(c)  $10001000_2 \div 00100010_2$

$$\begin{array}{r} 10001000 \\ \div 00100010 \\ \hline 00000000 \\ \phantom{00000000} + 1 \\ \hline 00000001 \\ \hline \hline \end{array} \quad \text{2nd complement}$$

(d)  $6D_{16} - 3F_{16}$

$01101101 - 00111111$

$$\begin{array}{r} 01101101 \\ - 00111111 \\ \hline 10010000 \\ \phantom{10010000} + 1 \\ \hline 10010001 \end{array} \quad \text{2nd complement}$$

(e)  $00010110_{BCD} + 00010101_{BCD} = (?)_{16}$

$0001\ 0110 + 0001\ 0101$

$$\begin{array}{r} 0001\ 0110 \\ + 0001\ 0110 \\ \hline 0010\ 1000 \end{array}$$



$$\begin{array}{r} 16 \\ + 16 \\ \hline 32 \end{array}$$

QNO 3:

$11010011_2$

$1010_2$

1010 )  $\overbrace{11010011000}^{15}$  (

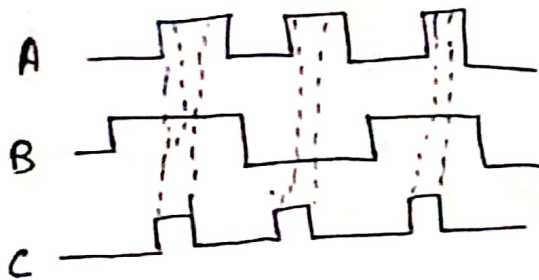
$$\begin{array}{r} 1010 \\ \hline 01100011000 \\ 1010 \\ \hline 0100011000 \\ 1010 \\ \hline 001011000 \\ 1010 \\ \hline 0001000 \\ 1010 \\ \hline 0010 \end{array}$$

R

QNO4: Apply CRC to detect the errors.

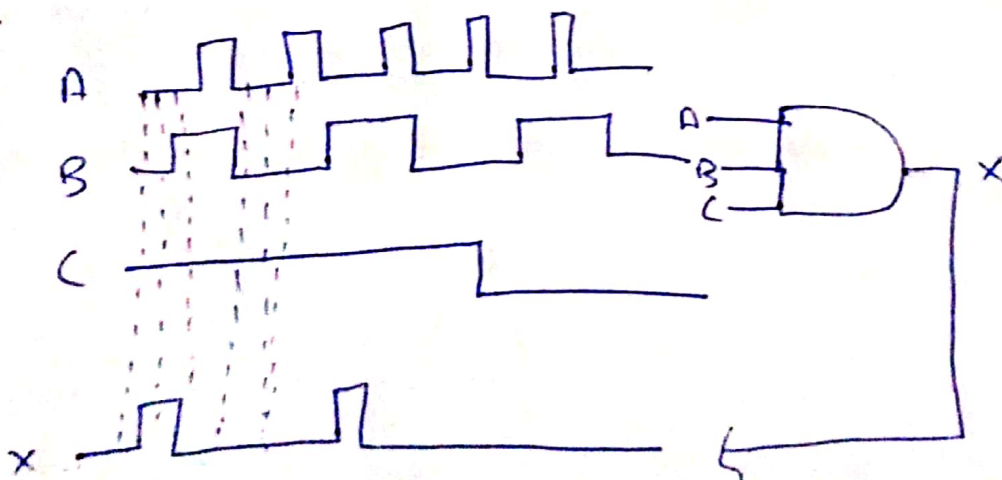
$$\begin{array}{r}
 1010 \overline{) 11010011010} \\
 \underline{1010} \phantom{00000} \\
 00100011010 \\
 \underline{1010} \phantom{00000} \\
 0100011010 \\
 \underline{1011} \phantom{00000} \\
 000111010 \\
 \underline{000111010} \\
 00111010 \\
 \underline{1010} \phantom{00000} \\
 010010 \\
 \underline{1010} \phantom{00000} \\
 00110
 \end{array}$$

QNO5:



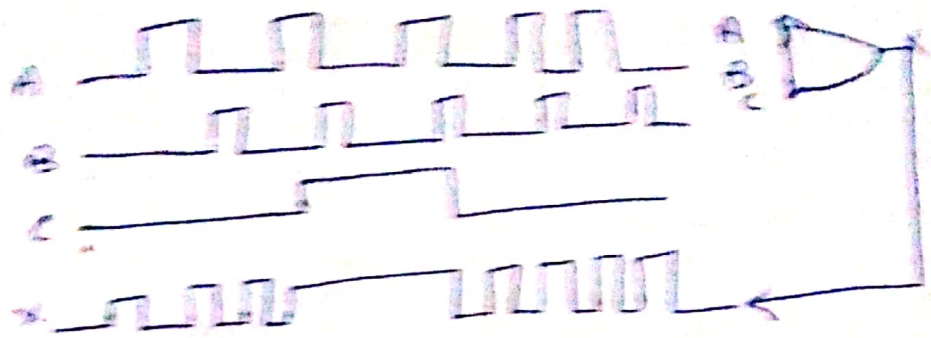
Sol: The output waveform X of the 3 inputs And gate is High only when all three input waveform A, B, C are High.

Sol:



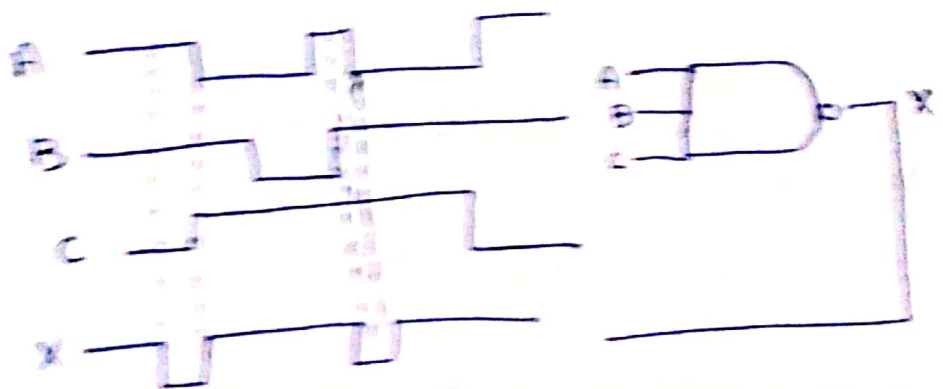


Q6: OR Gate



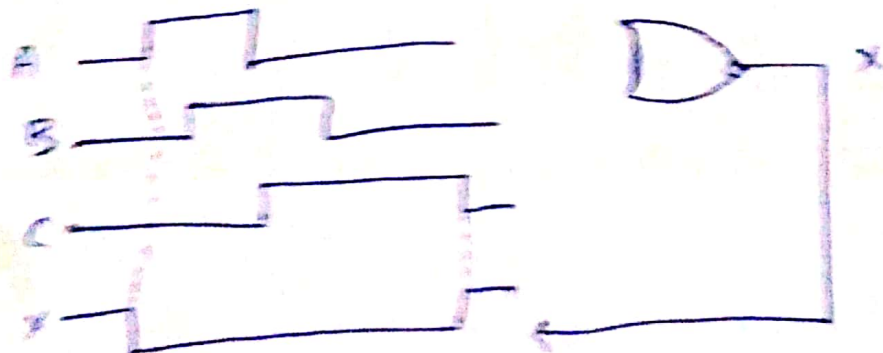
Sol: The output is high when one or more of the inputs waveforms are high as indicated by the output waveform X in timing diagram.

Q7: Input NAND gate



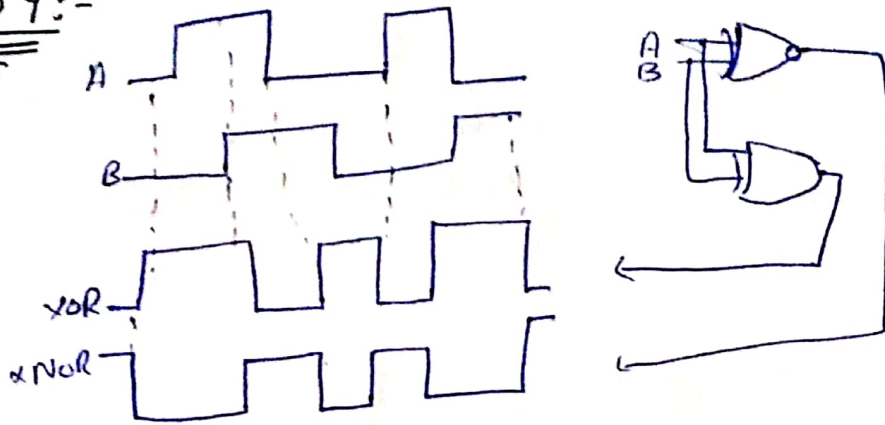
Sol: The output waveform X is low only when all three inputs waveforms are high as shown in the timing diagram.

Q8: 3-input NOR gate



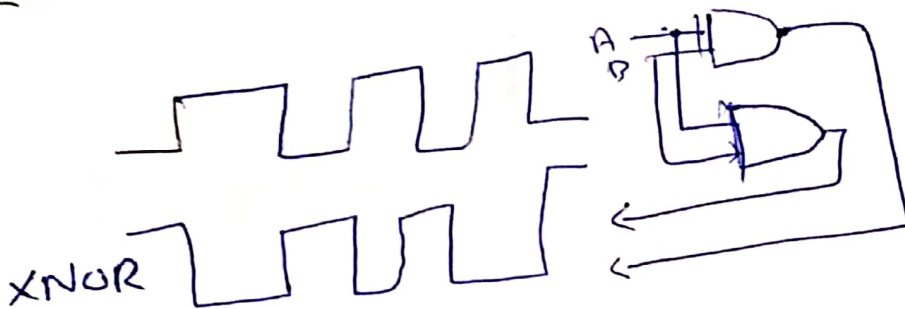
Sol: The output X is low when any input is high as shown by output waveform X in the timing diagram.

QNO 9:-



Sol:- The outputs waveform are shown in figure 2. Notice the XOR output is High only when both inputs are at opposite levels. Notice that the XNOR output is high only when both inputs are the same.

QNO 10:- XNOR



QNO 11:- using Boolean algebra techniques.

$$A\bar{B} + A\bar{B}C + A\bar{B}CD + A\bar{B}CDE$$

$$A\bar{B}(1 + C + CD + CDE)$$

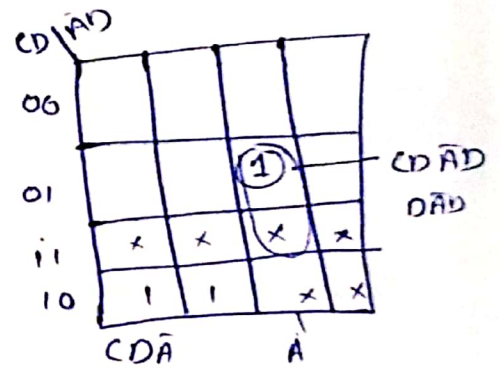
$$A\bar{B}(1) + A\bar{B}CD(0)$$

$$A\bar{B}(1 + C)(1)$$

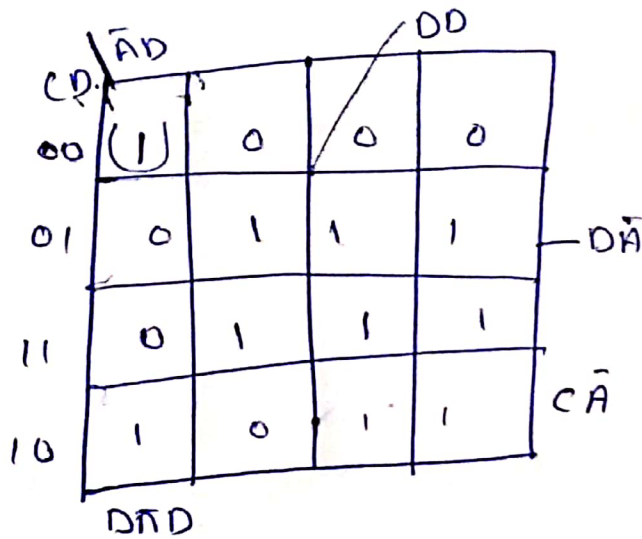
$$A\bar{B}(A + \bar{B})(A + C)$$

Q12:

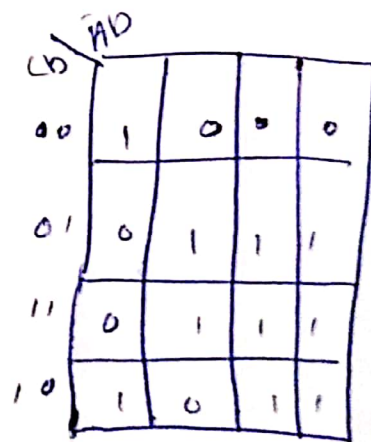
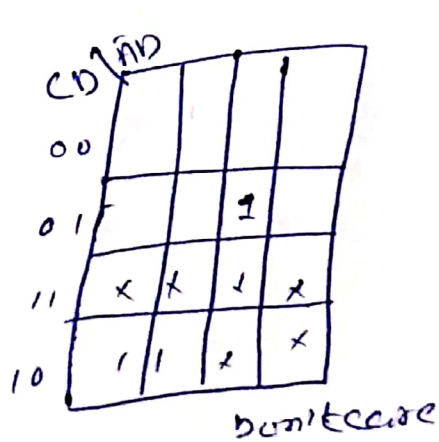
Input				Output
A	B	C	D	V
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	1
1	0	0	1	x
1	0	1	0	x
1	0	1	1	x
1	1	0	0	x
1	1	0	1	x
1	1	1	0	x
1	1	1	1	x



Q13:



Q14:



QNO 15:  $\bar{A}\bar{B}\bar{C} + \bar{A}B\bar{C} + A\bar{B}\bar{C} + ABC$

Sol: The binary value of the expression are

$000 + 011 + 101 + 110$

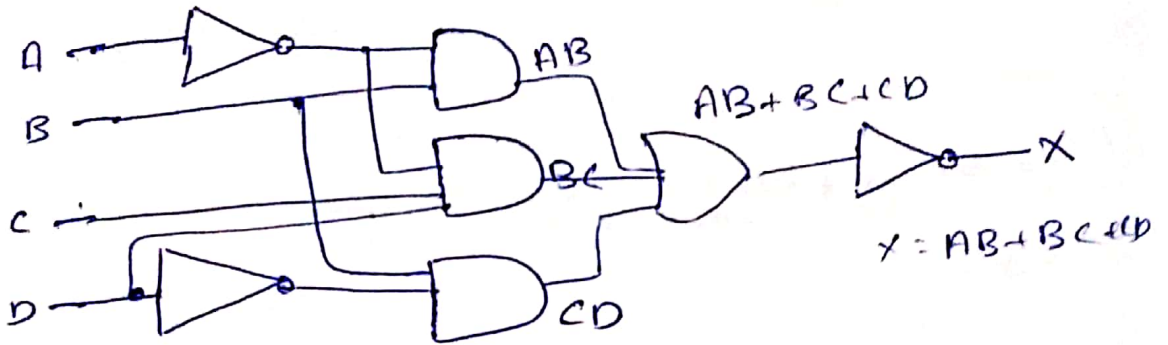
map the standard sop expression and group the cells are show in figure

	c	0	1	
AB				
00		1	1	— $\bar{A}C$
01			1	
11				
10		1	1	— $\bar{B}$

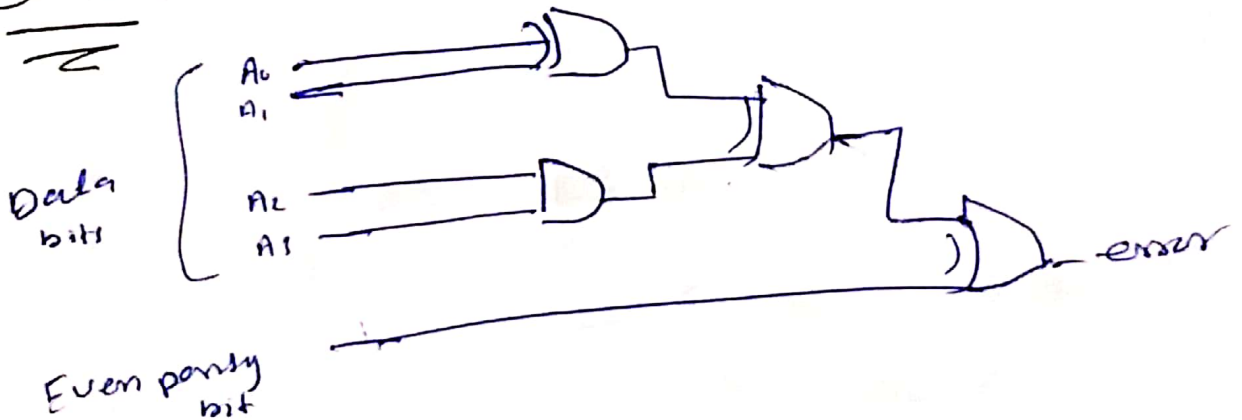
QNO 16: notice the wrap around the 4 cell group that includes the top row and the bottom row of 1s. The remaining 1 is absorbed in overlapping group of two cell. The group of four 1s produce a single variable term.

\* that is the minimum expression is equivalent to the original standard expression.

Q17



Q18: No gate

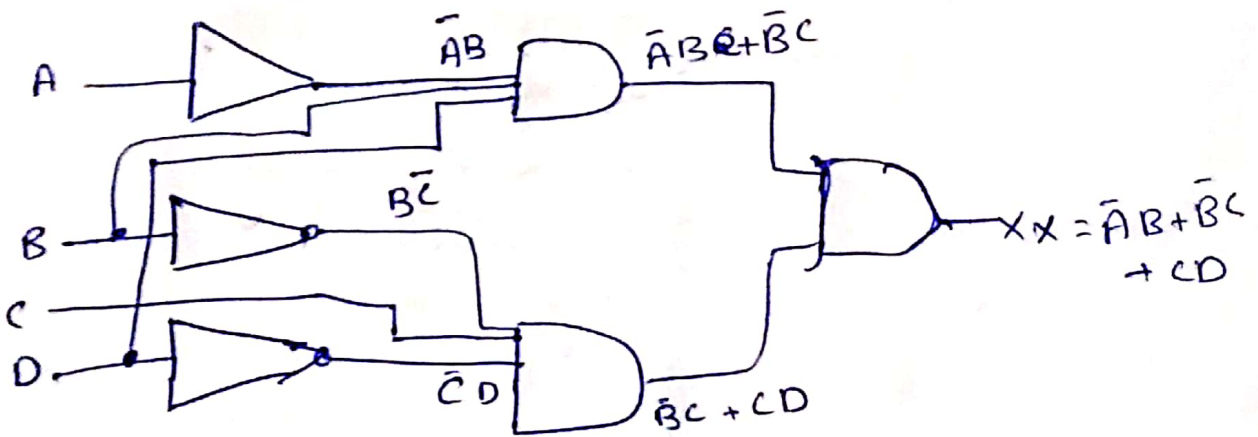


Sol<sup>n</sup>

The circuit in figure produce a 1 output where there is an error in the five bit code and a 0 when there is no error.

Q No (19) :-

A	B	C	D	X
0	0	0	0	0
0	0	0	1	0
0	0	1	0	0
0	0	1	1	0
0	1	0	0	0
0	1	0	1	0
0	1	1	0	0
0	1	1	1	0
1	0	0	0	0
1	0	0	1	0
1	0	1	0	0
1	0	1	1	0
1	1	0	0	0
1	1	0	1	0
1	1	1	0	0
1	1	1	1	0



The end