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SUB:-

PRCD - I

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QUESTION- 1

GIVEN DATA:

$$f_y = 60000 \text{ psi}$$

$$L.L = 2.47 \text{ k/ft}$$

$$D.L = 1.05 \text{ k/ft}$$

$$w = 10''$$

$$f_c = 4000 \text{ psi}$$

$$h = 20''$$

$$d = h - 3$$

$$d = 17''$$

$$d' = 2.5''$$

SOLUTION:

$$I_{max} = 0.85 \times B \times \frac{f_c}{f_y} \times \left(\frac{\epsilon_u}{\epsilon_u + \epsilon_y} \right)$$

Putting values.

$$0.85 \times 0.85 \times 4/60 \times \left(\frac{0.003}{0.003 + 0.005} \right)$$

$$I_{max} = 0.018$$

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②

Now Area of steel.

$$f_{max} = \frac{A_{ST}}{b \times d}$$

$$A_{ST} = f_{max} \times b \times d$$

$$A_{ST} \Rightarrow 0.0181 \times 10 \times 17$$

$$A_{ST} \Rightarrow 3.07 \text{ in}^2$$

Now design factor moment.

$$M_{U2} = \phi \times A_{ST} \times f_y \times (d - a/2)$$

$$a = \frac{A_{ST} \times f_y}{0.85 f_c' b}$$

$$a = \boxed{} = \frac{3.08 \times 60}{0.85 \times 4 \times 10}$$

$$a = 5.4''$$

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$$M_{U2} = 0.90 \times 3.08 \times 160 \times (17 - 5.4/2)$$

$$M_{U2} = 2378.3 \text{ K}''$$

Now moment of a given load:

Self weight of beam

$$\Rightarrow b \times t \times c$$

$$\Rightarrow \frac{10}{12} \times 150 \times \frac{20}{12}$$

$$\Rightarrow 208.3 \text{ lb/ft.}$$

$$\text{Total factored load} = 1.2 D \cdot L + 1.6 L \cdot L$$

$$\Rightarrow 1.2 (1050 + 208.33) + 1.6 (2470)$$

$$= 5.5 \text{ K/ft.}$$

Ultimate force moment.

$$M_U = \frac{5.5 (18)^2 \times 12}{8}$$

$$M_U = 2653.6$$

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④

As 2378.3 is lesser than 2653.6
It shows that beam should be
doubly design.

Now

$$M_{U1} = M_{U0} - M_{U2}$$
$$= 2653.6 - 2378.3$$

$$M_{U1} = 275.2 \text{ k''}$$

$$M_{U1} = 0 \times A_s' \times f_y \times (d - d')$$

$$A_s' = \frac{M_{U1}}{0 \times f_y \times (d - d')}$$

$$\Rightarrow \frac{275.2}{0.90 \times 60 (17 - 2.5)}$$

$$A_s = 0.35 \text{ in}^2$$

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$$A_s^o = A_{ST} + A_{S'}$$

$$A_s^o = 3.08 + 0.35$$

$$3.43 \text{ in}^2$$

This lies in the tension zone of steel.

Bars selection:

For tensile steel; lets ~~the~~ take bar no 8

$$\begin{aligned} \text{No of bars} &= \frac{A_s}{A_b} = \frac{3.43}{0.785} \\ &= 4.36 \approx 5 \text{ bars.} \end{aligned}$$

For compression steel;

lets take #6 bar.

$$\text{No of bars} = \frac{A_{S'}}{A_b} = \frac{0.35}{0.442}$$

$$\begin{aligned} &\Rightarrow 0.75 \text{ bars} \\ &\approx 1 \text{ bar.} \end{aligned}$$

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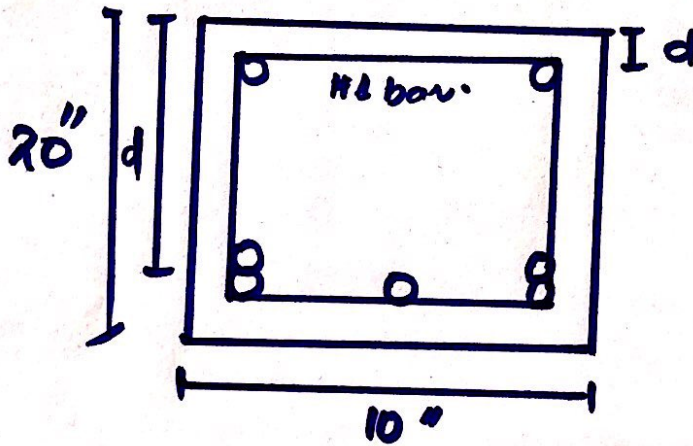
Minimum width of beam

$$(2 \times 1.5) + 2 \left(\frac{3}{8} \right) + \left(5 \times \frac{8}{8} \right) + \left(4 \times \frac{8}{8} \right)$$

$$\Rightarrow 12.75''$$

As $12.75''$ is greater than $10''$

Therefore it should be multiple layers.



$$d = 20 - 1.5 - \frac{3}{8} - \frac{8}{8} - \frac{1}{2} \left(\frac{8}{8} \right)$$

$$d = 16.62''$$

$$d' = 1.5 + \frac{3}{8} + \frac{1}{2} \left(\frac{8}{8} \right) = 2.25''$$

Design moment:

$$M_d = \phi \times \left[A_s' \times f_y \times (d - d') \right. \\ \left. + (A_s - A_s') \times f_y \times \left(\frac{d - d'}{2} \right) \right]$$

$$a = \frac{(A_s - A_s') \times f_y}{0.85 \times \rho \times b} = \frac{(5 \times 0.785 - 1 \times 0.44) \times 60}{0.85 \times 4 \times 10}$$

$$a = 6.15''$$

$$0.90 \times \left[1 \times 0.44 \times 60 \times (16.62 - 2.25 + \right. \\ \left. 5 \times 0.785 - 1 \times 0.44 \times 60 \times \left(16.25 - \frac{6.15}{2} \right) \right]$$

$$M_d = 2891.50$$

$M_d = 2891.50$ is greater than

$2.653.561$ so the design

is fine.



QUESTION- 2

(a) BOND STRESS:-

The bond stress design is defined as The shear force per unit nominal surface area of reinforcing bar. The stress is acting on the interface bars between bars and surrounding concrete and along the direction parallel to the bar.

DEVELOPMENT LENGTH:-

It is defined as that length of embedment necessary to develop ~~the~~ the full tensile strength of the bar controlled by splitting or pullout. The length over which force develops is called development length.

Doubly Reinforced beam:

Because of the high design stresses, Double Reinforced beams are not common as they are in NSD. They are more useful for control of cracks and deflection as well as binding the top and bottom reinforcement.

<C>

T-BEAM:-

- ↳ Flexure capacity of T-Beam varies based on sign of moment
- ↳ In T-beam slabs and beams are connected and acts as one member.
- ↳ Design procedure depends on the location of moment.

RECTANGULAR BEAM:-

- ↳ In Rectangular beam flexure capacity depends on location of reinforcement to the yield.
- ↳ Simple design and require no complications.
- ↳ Slab is placed on the beam so that there is no connection between slab and beam.

<d>

Effect of strength reduction factor on
flexure strength :

In the design of flexure strength the strength reduction factor decreases from tension - controlled section to compression controlled section to increase the safety with decreasing ductility. Depending on the structure compression controlled sections have less ductility thus they act simultaneously to hold together the structure.

<e>

Following are design methods of PRC.

ULTIMATE LOAD DESIGN:-

The method which limits the structural usefulness of material of the structure upto ultimate load.

LIMIT STATE METHOD:-

Method which limits the structure usefulness of material or structure upto certain load at which acceptable limit of service ability and safety are applied.

ELASTIC METHOD:-

Methods which limits the structural usefulness of material of structure upto certain load at which the min stress is extreme fiber reaches the characteristics strength of material in bending.

QUESTION-3

GIVEN DATA:-

$$L_c \text{ distance} = 10'$$

$$\text{span} = 32'$$

$$\text{slab} = 6''$$

$$\text{width} = 14''$$

$$\text{total depth} = 28''$$

$$\text{Effective depth} = 25''$$

$$\text{dead load} = 50 \text{ lb/ft}^2$$

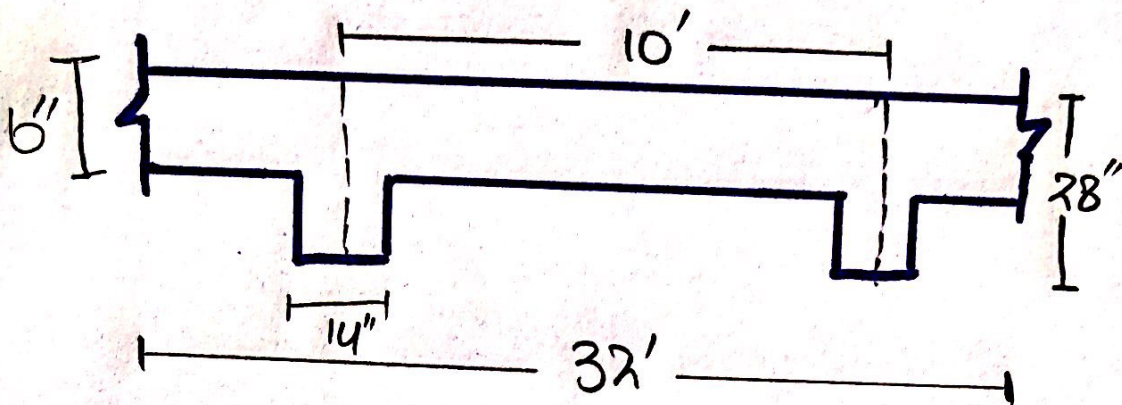
$$S.F. = 225 \text{ lb/ft}^2$$

$$f_c = 4000 \text{ psi} = 4 \text{ ksi}$$

$$f_y = 60000 \text{ psi}$$

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(14)



U.F.M

$$M_U = \frac{w \cdot x^2}{8}$$

Self weight per foot

$$wt = b \times t \times c$$

$$\Rightarrow \frac{14}{12} \times \frac{28}{12} \times 150$$

$$\Rightarrow 408.33 \text{ lb/ft.}$$

Total factored load.

$$w_u = 1.2(50 + 408.33) + 1.6(225)$$

$$w_u = 909.96 \text{ lb/ft.}$$

Moment:

$$M_u = \frac{w_u \times l^2}{8}$$

$$\Rightarrow \frac{0.909 \times (32)^2 \times 12}{8}$$

$$\Rightarrow 1396.20 \text{ kip/in}$$

Effective width

$$1 \rightarrow 16 \times h_f + b_w = 16 \times 6 + 14 \Rightarrow 110''$$

$$2 \rightarrow \text{c/c distance} = 10 \times 12 \Rightarrow 120''$$

$$3 \rightarrow \text{span} = \frac{32}{4} \times 12 = 96''$$

Choose least value i.e 96''

Check Rectangular or T-beam is needed

Trial ①

$$a = h_f = 6''$$

$$A_{ST} = \frac{M_u}{\phi \times f_y \times (d - a/2)}$$

$$\Rightarrow \frac{1396.24}{0.90 \times 60 \times 25 - (6/2)}$$

$$A_{ST} = 1.175 \text{ m}^2$$

Trial (2)

$$a = \frac{A_{st} \times f_y}{0.85 f_c \times b_e}$$

$$\Rightarrow \frac{1.175 \times 60}{0.85 \times 4 \times 96} \Rightarrow 0.22''$$

0.22'' is less than 6''

Rectangular beam is required.

$$A_{ST} = \frac{M_u}{\phi \times f_y \times (d - a/2)}$$

$$\Rightarrow \frac{1396.24}{0.90 \times 60 \times (25 - 0.2/2)}$$

$$\Rightarrow 1.04 \text{ in}^2$$

Trial (3)

$$q = \frac{1.04 \times 60}{0.85 \times 4 \times 96}$$

$$\Rightarrow 0.19''$$

$$A_{ST} = \frac{1396.24}{0.90 \times 60 \times (25 - 0.19/2)}$$

$$\Rightarrow 1.04 \text{ in}^2$$

Check f_{max} and f_{min}

$$f_{max} = 0.85 \times \beta \times \frac{\sqrt{f_c'}}{\sqrt{f_y}} \times \left(\frac{\epsilon_u'}{\epsilon_u + \epsilon_t} \right)$$

$$0.85 \times 0.85 \times \frac{4}{60} \times \left(\frac{0.003}{0.003 + 0.005} \right)$$

$$f_{max} = 0.018$$

$$f_{min} = \frac{200}{\beta g} = \frac{200}{6000}$$

$$\Rightarrow 0.003$$

$$f = \frac{A_{st}}{b \times d} = \frac{1.03}{14 \times 25}$$

$$\Rightarrow 0.0029$$

$$f_{min} < f < f_{max}$$

$$0.003 < 0.002 < 0.018$$

If f is less than f_{min} Then

$$f = \frac{A_{st}}{b \times d}$$

$$A_{st} = f_{min} \times b \times d.$$

$$0.003 \times 14 \times 25$$

$$\Rightarrow 1.05 \text{ in}^2$$

No and Selection of bar

Let use #08 Then

$$\text{dia} = (8/2) = 1''$$

$$\text{Area} = 0.785''^2$$

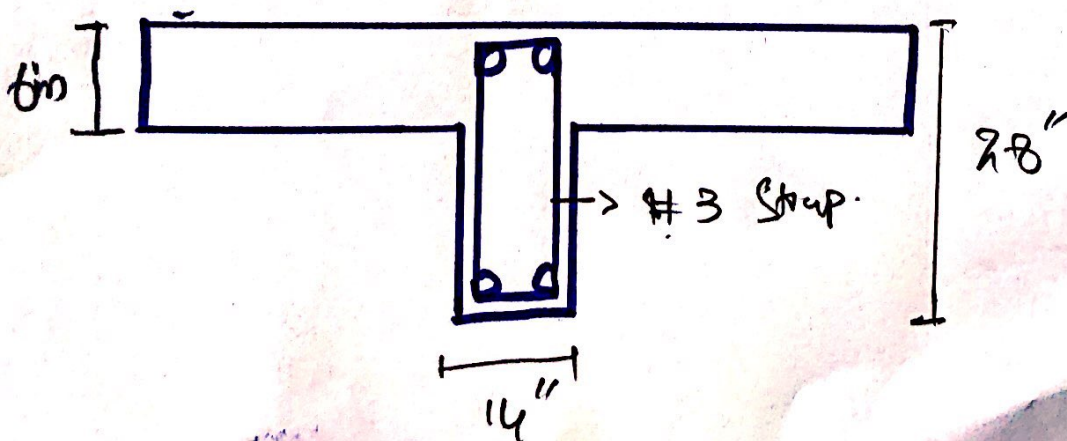
$$\text{No of bars} = \frac{1.05}{0.785} = 1.3 \approx 2 \text{ bars}$$

Minimum width

$$b_{\min} = (2 \times 1.5) + (2 \times 3/8) + 2(10/8) + 1(10/8)$$

$$\Rightarrow 7.5'' < 14''$$

It will be fine in one layer.



Design Moment.

$$M_d = \phi \times f_y \times A_{ST} \times (d - a/2)$$

$$A_{ST} = 1.27 \times 19$$

$$\Rightarrow 2.55 \text{ m}^2$$

$$a = \frac{A_{ST} \times f_y}{0.85 f_c' \times b_e}$$

$$\Rightarrow \frac{2.54 \times 60}{0.85 \times 4 \times 96}$$

$$\Rightarrow 0.46''$$

$$M_d = 0.90 \times 60 \times 2.54 \times \left(25 - \frac{0.46}{2}\right)$$

$$\Rightarrow 3396.97$$

$\Rightarrow 339.97$ is 'greater than

$$1396.24$$

Design is fine.