

NAME = Subhan Ullah Khan

ID# = 7861

Section = B

Semster = 6th

Department = BE (Civil)

Submitted to = Engr. Sir Fawad

Subject = P.R.C. Design 1

Q NO 2

Given:-

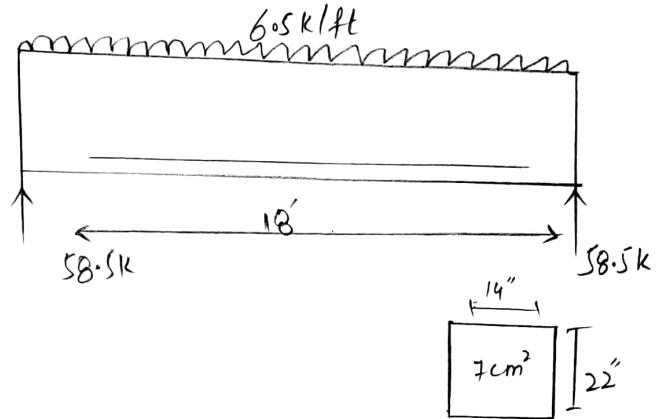
Breadth of web of beam (b_w) = 14"

Effective depth d_r = 22"

Load = 6.5k/ft

f'_c = 4ksi

f_y = 60ksi



Step: 2

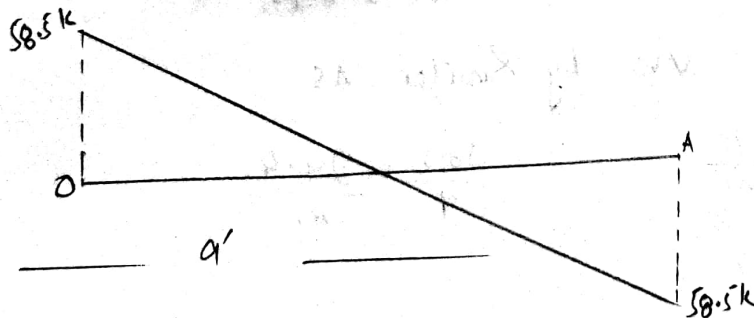
Rxn on supports

$$\frac{6.5 \times 18}{2} = 58.5 \text{ kips}$$

Step: 2

SFD

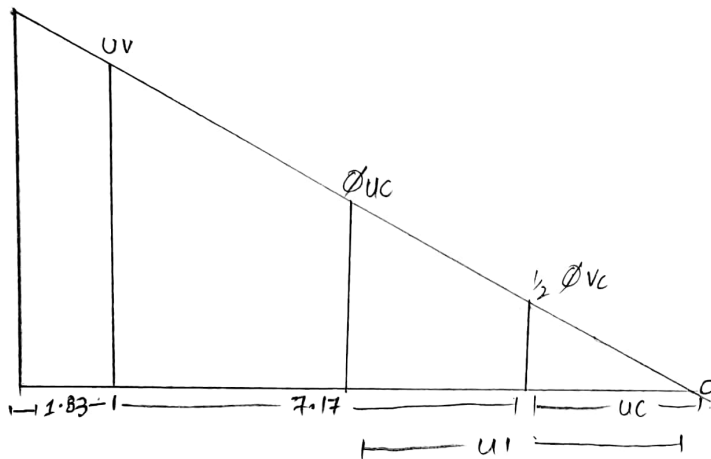
The beamwise Shear Force Diagram is



Step: 3

②

Finding value of V_u and its location
 critical shear is located at distance d from
 support $(d) = 22'' = 1.83'$



From similar AC $\frac{58.5}{9} = \frac{V_u}{8.17}$

Step: 04 $V_u = 46.61$ kips

find value of ϕV_c and $\frac{1}{2} \phi V_c$

$$\phi V_c = \phi \times 2 \times \sqrt{f'_c} \times b_w \times d$$

$$= 0.75 \times 2 \times \sqrt{4000} \times 14 \times 22 = 29219 \text{ lbs}$$

$$= 29.21 \text{ kips}$$

location of ϕV_c by similar AS

$$\frac{58.5}{9} = \frac{\phi V_c}{x_1}$$

$$\frac{58.5}{9} = \frac{29.4}{x_1}$$

$$x_1 = 4.49'$$

Similarly

(3)

$$Y_2 \phi_{vc} = \phi_{vc} / 2 = \frac{29.21}{2} = 14.60 \text{ kips}$$

\Rightarrow Location of $\frac{1}{2} \phi_{vc}$ will be,

$$\frac{58.5}{9} = \frac{14.60}{u_2}$$

$$\Rightarrow u_2 = 2.24'$$

Step: 05

Finding the value of ϕ_{vs}

By formula

$$\begin{aligned} \phi_{vs} &= V_v - \phi_{vc} \\ &= 46.61 - 29.21 \end{aligned}$$

$$\phi_{vs} = 17.4 \text{ kips}$$

Step: 06

Check on section adequacy

By formula

$$\begin{aligned} &= \phi \times 8 \sqrt{f'_c} \times 6w \times d \\ &= 0.75 \times 8 \times \sqrt{4000} \times 14 \times 22 \\ &= 116877 \text{ lbs} \\ &= 116.87 \text{ kips} \end{aligned}$$

As $\phi \times 8 \times \sqrt{f_c} \times b_w \times d > \phi V_s$
is.
So section Adequate

Step : 07

check on Maximum Spacing for stirrups
By formula

$$= \phi \times 4 \times \sqrt{f_c} \times b_w \times d$$

$$= 0.75 \times 4 \times \sqrt{4000} \times 14 \times 22$$

$$= 58438.105$$

$$= 58.43 \text{ kips}$$

As

$\phi \times 4 \times \sqrt{f_c} \times b_w \times d > \phi V_s$
So maximum will be selected from the following
4 conditions

1- $s_{max} = 24"$

2- $d/2 = 22/2 = 11"$

3- $\frac{A_u \times f_y}{0.75 \times \sqrt{f_c} \times b_w}$

Here we are using #3 stirrups

$$d_p = \left(\frac{3}{8}\right)" = 0.375"$$

$$A_{req} = \frac{\pi}{4} (0.375)^2 = 0.11 \text{ in}^2$$

(5)

For 2-legged stirrup

Area $\times 2$

$$0.11 \times 2 = 0.22 \text{ in}^2$$

$$s_{\max} = \frac{0.22 \times 60000}{0.75 \times \sqrt{4000} \times 14} = 19.87''$$

$$4 - s_{\max} = \frac{A_u \times f_y}{50 \times f_w} = \frac{0.22 \times 60,000}{50 \times 14} = 18.85''$$

Step: 08

Stirrup spacing from/at critical section will be by formula

$$s = \frac{\phi \times A_u \times f_y \times d}{V_u - \phi V_c}$$

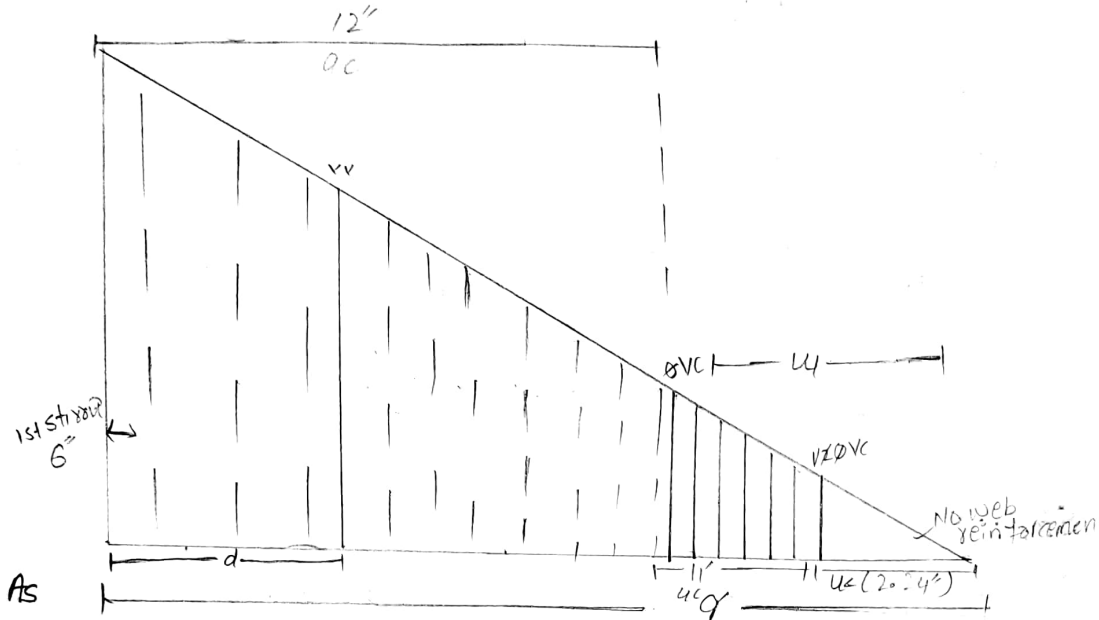
$$= \frac{0.75 \times 0.22 \times 60 \times 22}{46.61 - 29.21}$$

$$s = 19.5'' \approx 19''$$

so 19c/c

Step #09

(6)



First stirrup from face of support =

$$\frac{s}{2} = \frac{12}{2} = 6$$

Question No 5

GIVEN

Height of flange (h_f) = 3.5

gc distance = 9

Span of beam = 16

web width (b_w) = 18

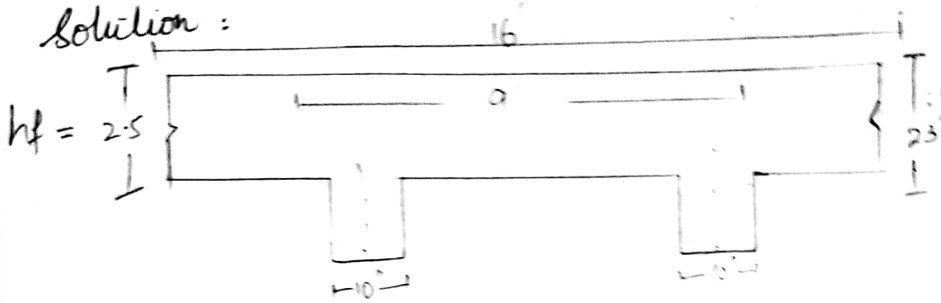
Height, (h) = 23

MU = 5800 kip-inch

$$f'c = 3 \text{ ksi}$$

$$f_y = 60 \text{ ksi}$$

Solution:



Step 01

Calculate the effective width (b_e) for T-beams

$$1 - 16 (b_f) + 6w = 16(3.5) + 10 = 66''$$

$$2 - \frac{1}{6} \text{ span distance} = 9 \times 12 = 108''$$

$$3 - \text{Span} / 4 = \frac{16}{4} \times 12 = 48''$$

Selecting the least value of b_e as,

$$b_e = 48''$$

Step 2

Check whether Rectangular or T-beam Analysis is required

Trial 01:

$$\text{let } a = h_f = 3.5'$$

$$A_{st} = \frac{M_u}{\phi \times f_y \times (d - a/2)} = \frac{(8)}{0.90 \times 60 \left(18 - \frac{3.5}{2}\right)}$$

$$= 6.61 \text{ cm}^2$$

Trial # 2

$$a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b_e}$$

$$a = \frac{6.61 \times 60}{0.85 \times 3 \times 48}$$

$$= 3.2''$$

$$3.2'' < 3.5''$$

and

$$A_{st} = 6.55 \text{ cm}^2$$

So Rectangular Beam Design is Required!

Trial # 3

$$a = 3.21''$$

and

$$A_{st} = \frac{5800}{0.90 \times 60 \left(18 - \frac{3.21}{2}\right)}$$

$$= 6.55 \text{ cm}^2$$

So Area of Steel is 6.55 cm²

(9)

Step: 03

Check s_{max} and s_{min}

$$s_{max} = 0.85 \times \beta \times \frac{f_c}{f_y} \left(\frac{E_u}{E_u + E_t} \right)$$
$$= 0.85 \times 0.85 \times \frac{3}{60} \left(\frac{0.003}{0.003 + 6.005} \right) = 0.013$$

$$\Rightarrow s_{min} = \frac{200}{f_y} = \frac{200}{60,000} = 0.003$$

$$\Rightarrow \rho = \frac{A_{st}}{b \times d} = \frac{6.55}{10 \times 18} = 0.036$$

$$s_{min} < \rho < s_{max}$$

$$0.003 < 0.036 < 0.013$$

As the value of s_{max} is less than ρ , so we have to design it as Doubly Reinforced Beam.

first we have to find the Area of steel against s_{max}

$$s_{max} = \frac{A_{st}}{b \times d}$$

$$A_{st} = s_{max} (b \times d)$$

$$A_{st} = 0.013 \times (10 \times 18)^{(10)}$$

$$A_{st} = 2.34 \text{ in}^2$$

Step - 4

Finding the value of M_u^2

By formula

$$M_u^2 = \phi \times A_{st} \times f_y \times (d - a/2)$$

First finding value of a

$$a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b}$$

$$= \frac{2.43 \times 60}{0.85 \times 3 \times 10}$$

$$a = 5.72''$$

$$M_u^2 = 0.90 \times 2.43 \times 60 \times (18 - 5.72/2)$$

$$M_u^2 = 1986.67 \text{ inch}$$

$$M_u^2 < M_u$$

$$1986.67 < 5800$$

So we have to design the beam in such
away that it can resist more bending moments
than the applied external moment (11)

Step: 05

finding difference in moments and area of steel

$$M U_1 = M U - M U_2$$

$$= 5800 - 1986.67$$

$$= 3813.33 \text{ Kip-inch}$$

By formula

$$A_{st} = \frac{M U}{\phi \times f_y \times (d-d)}$$

$$A_{st} = 4.56 \text{ in}^2$$

Step: 06

finding total steel area

$$A_s = A_{st} + A'_{st}$$

$$= 2.43 + 4.56$$

$$= 6.99 \text{ in}^2$$

Step: 07

Selection of Bar:-

(12)

In tension zone:-

let we have use #8 bar

$$\text{dia } (9/8) = 1''$$

$$\text{Area} = \pi/4 (1)^2 = 0.78 \text{ in}^2$$

By formula

$$\text{No of bars} = \frac{\text{Area of steel}}{\text{Area of single bar}} = \frac{6.99}{0.785} \approx 8.91$$

So 9 #8 bars

By formula

In Compression zone

$$= \frac{\text{Area of steel}}{\text{Area of single bar}} = \frac{6.99}{0.785} = 8.91$$

(13)

In Compression Zone

Let use no 7 bar

$$\begin{aligned} \text{Area} &= \frac{\pi}{4} d^2 = 7/8 \times \pi/4 \\ &= 0.60 \text{ in}^2 \end{aligned}$$

By formula

$$= \frac{\text{Area of steel}}{\text{Area of single bar}} = \frac{8.99}{0.785} =$$

$$4.56 = 7.5 \approx 8$$

So 8# 7 bars

Step: 08

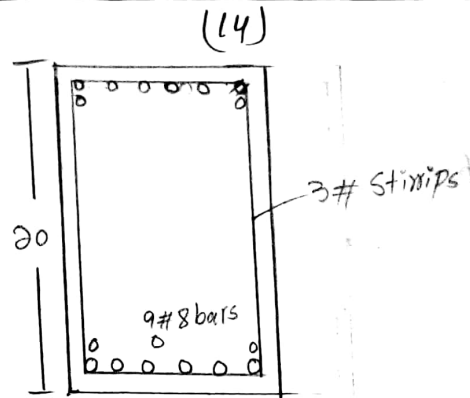
Maximum width for Accomodation of bars

$$\begin{aligned} b_{min} &= (2 \times 1.5) + (2 + 3/8) + 9(3/8) + 8(8/8) \\ &= 20.75'' \end{aligned}$$

As

$$20.75'' > 10$$

bars will be place in multiple layers



$$\text{Effective depth } (d) = 23 - 1.5 + \frac{8}{8} + \frac{8}{8} + \frac{1}{2} \left(\frac{9}{8} \right) = 19.6''$$

$$\text{Effective cover } (d') = 1.5 + \frac{3}{8} + \frac{7}{8} + \frac{1}{2} \left(\frac{7}{8} \right) = 3.18''$$

Step: 09

Finding Design Moment

$$M_d = \phi \frac{A_s \times f_y \times (d - d')}{0.85 \times f_c \times b}$$

$$= \frac{(9 \times 0.785 - 8 \times 0.601) \times 60}{0.85 \times 3 \times 10} = 5.31''$$

$$M_d = 0.90 \left[(8 \times 0.60) \times 60 \times (19.6 - 3.18) + (9 \times 0.785 - 8 \times 0.60) \times 60 \times \left(19.6 - \frac{5.31}{2} \right) \right]$$

$$M_d = 6378.88$$

$$\text{As } 6378.88 > 5800$$

⇒ so Design is OK!

Question No : 06 (15)

Solution

Breadth (b) = 14"

Height (h) = 26"

Concrete Compression strength $f'_c = 4 \text{ ksi}$

Steel Tensile strength (f_y) = 60 ksi

Mu = 6000 kip-in

Effective depth of beam (d) = 22"

Assume effective cover (d') = 2.5"

Step: 01 (Reinforcement Ratio)

By formula

$$s_{max} = 0.85 \times B \times \frac{f'_c}{f_y} \times \left(\frac{\epsilon_u}{\epsilon_u + \epsilon_y} \right)$$

$$= 0.85 \times 0.85 \times \frac{4}{60} \times \left(\frac{0.003}{0.003 + 0.005} \right)$$

$$s_{max} = 0.0180$$

Step: 2 (Area of steel)

As we know that

$$s_{max} = \frac{A_{st}}{b \times d} \Rightarrow A_{st} = s_{max} \times (b \times d)$$

$$= 0.0180 \times (14 \times 22) \quad (16)$$

$$= 5.54 \text{ in}^2$$

Step: 03 (Design Moment)

By using formula

$$M_{U2} = \rho \times A_{st} \times f_y \times (d - \frac{a}{2})$$

$$a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times b} = \frac{5.54 \times 60}{0.85 \times 4 \times 14}$$

$$= 6.98''$$

So

$$M_{U2} = 0.90 \times 5.54 \times 60 \left(22 - \frac{6.98}{2} \right)$$

$$= \del{5537.4} 5537.4 < 6000$$

So, we have to design a section as doubly reinforced

Step: 04 (Difference In Moment)

$$M_{U1} = M_U - M_{U2}$$

$$= 6000 - 5537.4$$

$$= 462.6 \text{ kip-inches}$$

Step: 05 = (Area of steel)⁽¹⁷⁾

$$M_u = \phi \times A_{st} \times f_y \times (d - d')$$

So Area of steel in compressive zone will be

$$\Rightarrow A_{st} = \frac{M_u}{\phi \times f_y \times (d - d')} = \frac{462.6}{0.90 \times 60 \times (22 - 2.5)}$$

$$\Rightarrow A_{st} = 4.44 \text{ in}^2$$

Step #06

(Total steel Area)

$$\begin{aligned} A_s &= A_{st} + A_{sc} \\ &= 5.54 + 0.44 \\ &= 5.98 \text{ in}^2 \end{aligned}$$

Step: 07

1- Steel in tension zone:-
we use #7 bars

$$\text{dia} = \left(\frac{7}{8}\right) = 0.875 \text{ ''}$$

$$\begin{aligned} \text{Area} &= \frac{\pi}{4} (0.875)^2 \\ &= 0.60 \text{ in}^2 \end{aligned}$$

$$\begin{aligned} \text{No of bars} &= \frac{A_{st}}{\text{Area of single bar}} \quad (18) \\ &= \frac{5.98}{0.601} = 9.9 \approx 10 \text{ bars} \end{aligned}$$

So 10 # 7 bars

2- Steel in Compressive zone:

We use # 5 bars

$$\text{dia} = 5/8 = 0.625''$$

$$\begin{aligned} \text{Area} &= \frac{\pi}{4} (0.625)^2 \\ &= 0.306 \text{ in}^2 \end{aligned}$$

$$\begin{aligned} \text{No of bars} &= \frac{A_{st}}{\text{Area of single bar}} \\ &= \frac{0.44}{0.306} = 1.435 \approx 2 \text{ bars} \end{aligned}$$

So 2 # 5 bars

step: 8

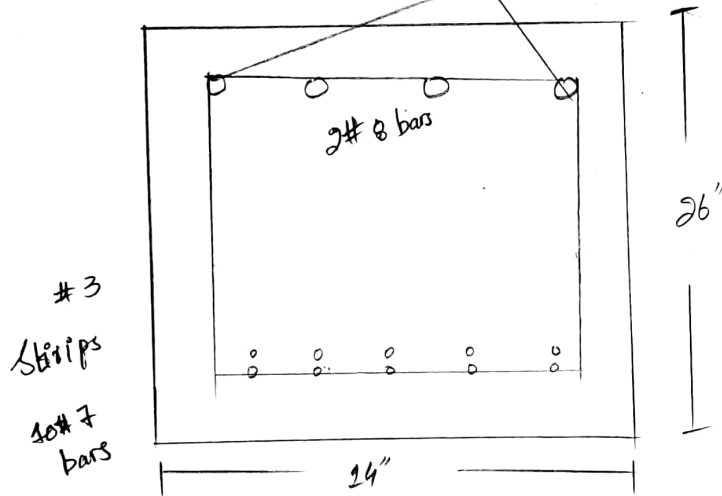
(19)

(Minimum width of Beam)

$$b_{min} = 2(1.5) + 2(3/8) + 10(7/8) + 9(7/8)$$

$$b_{min} = 20.37 > 14"$$

So not good in one supporting layer



Now

$$\text{Effective depth } (d) = 26 - 1.5 - 3/8 - 7/8 - \frac{1}{2} \left(\frac{7}{8} \right)$$
$$= 22.82"$$

$$\text{Effective cover } (d') = 1.5 + \frac{3}{8} + \frac{1}{2} \left(\frac{5}{8} \right)$$
$$= 2.18"$$

Step = 9 (Design Moment)

$$M_d = \phi [A_{st} \times f_y \times (d - d') + (A_{st} - A'_{st}) \times f_y \times (d - \frac{a}{2})]$$

$$a = \frac{(A_{st} - A'_{st}) \times f_y}{0.85 \times f'_c \times b}$$

$$= \frac{(10 \times 0.667 - 2 \times 0.306) \times 60}{0.85 \times 4 \times 14} \quad (20)$$

$$= 6.80''$$

$$M_d = 0.90 \left[(2 \times 0.306) \times 60 \times (22.82 - 2.18) + (10 \times 0.601 - 2 \times 0.306) \times 60 \times (22.82 - 6.80/2) \right]$$

$$M_d = 7047.6 \text{ kip-inches}$$

$$M_d = 7047.6 \text{ kip-inches}$$

$$\text{As } 7047.67 < 6000$$

Design is ok

Q No 1

Explain in detail types of stirrups with figures and also explain ACI codes for shear design,

ANSWER

STIRRUP:

Stirrups are closed-loop bars tied at regular intervals in beam reinforcement to hold the bars in position.

Types of stirrups:

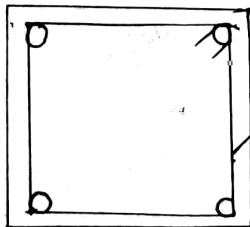
1- Single Legged stirrup:

The single legged stirrups have rarely been used because they are mostly used when binding only two rods.



2- Two-Legged stirrup:

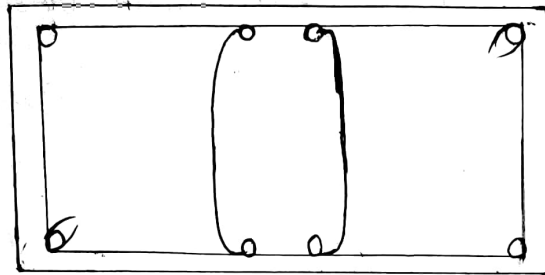
It is most commonly and widely used stirrup. Minimum 4 bars are required for providing this stirrup.



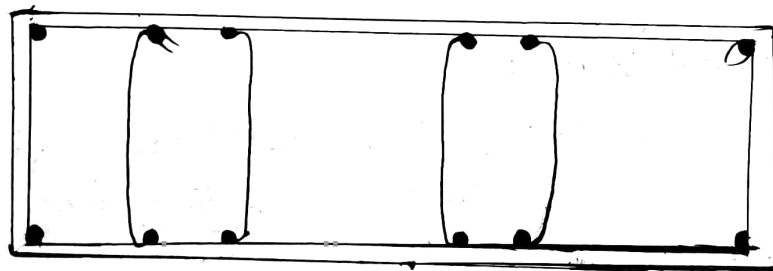
2 Legged stirrups

3- Four Legged stirrup:

These stirrups are used in case of web reinforcement



4. Six Legged stirrup:



ACI CODES FOR SHEAR DESIGN OF A BEAM:

According to ACI-318, following are the shear design of a beam

← Critical section: Critical section occurs at 45° and is at distance " d " from the face of support which is equal to effective depth.

2 - Shear Strength Capacity of Concrete is,

$$V_c = 2 \times \sqrt{f'_c} \times b_w \times d$$

3. Minimum web Reinforcement ::

If $V_u \leq \phi V_c$, then theoretically no web reinforcement is required. However ACI code require provision of at least minimum area of web reinforcement equal to

4. For Minimum Reinforcement Area ::

If $V_u \leq \phi V_c$, then theoretically no web reinforcement is required. However ACI Code require provision of at least minimum area of web reinforcement

$\phi = 0.75 \rightarrow$ For shear design.

$$A_{u\min} = \frac{0.75 \times \sqrt{f'_c} \times b_w \times s}{f_y}$$

By interchanging the formula, we can obtain the formula for maximum spacing

$$s_{\max} = \frac{A_u \times f_y}{0.75 \times \sqrt{f'_c} \times b_w} \quad \text{or} \quad \frac{A_u \times f_y}{250 \times b_w}$$

4: No web reinforcement is provided if

$$V_u \leq \frac{1}{2} \phi V_c$$

⇒ Between critical section " V_u " and " ϕV_c " spacing b/w web reinforcement can be found by

$$s = \frac{\phi \times A_u \times f_y \times d}{V_u - \phi V_c}$$

5: If $V_u \leq 4 \times \sqrt{f'_c} \times b_w \times d$, then max spacing for stirrups will be the smallest of the following

1 - 24"

2 - $\frac{1}{2}d$

3 - $S_{max} = \frac{A_u \times f_y}{0.75 \times \sqrt{f'_c} \times b_w}$

4 - $S_{max} = \frac{A_u \times f_y}{50 \times b_w}$

If $V_u > 4 \times \sqrt{f'_c} \times b_w \times d$

Max spacing will be halved.

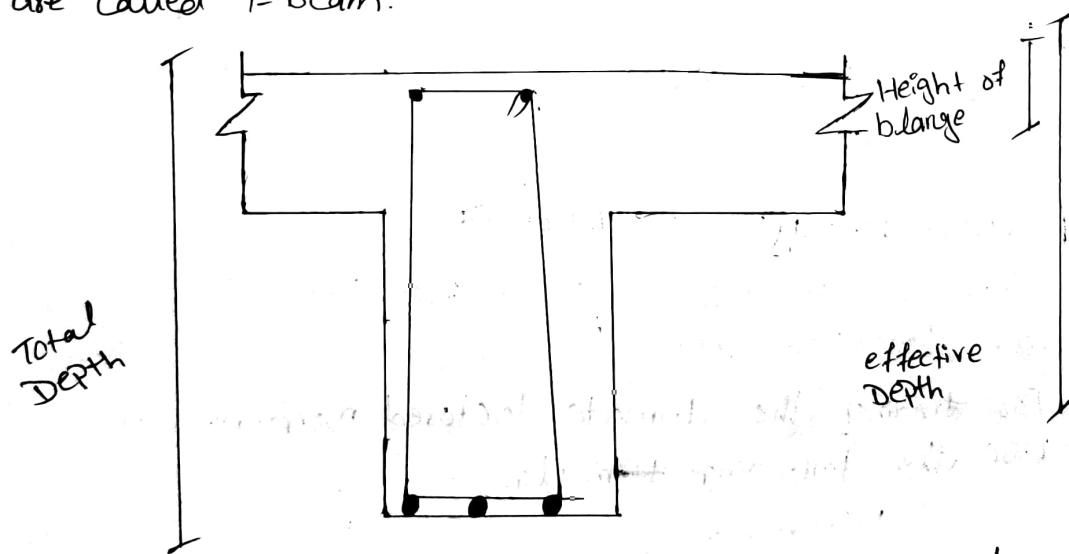
Question No: 3

Define both the T-Beam and L-Beam with the help of diagram. Also explain the usual analysis of T-Beam.

ANSWER

T-BEAM

In most of reinforcement concrete slabs are cast monolithically with the slab so, in this case the beam that act as an intermediate beam are called T-beam.

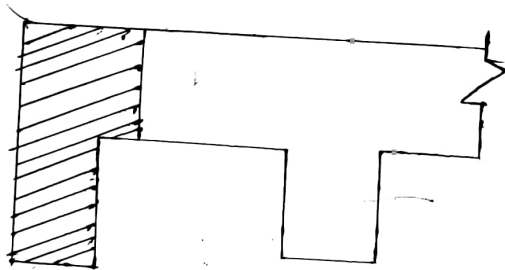


Because of their T-shape these beams are called T-beams

⇒ It is provided at the center of the slab let resists the load.

L-BEAM

L-shaped structure that is in contact with the slab and present at the corner of the floor is called L-Beam.



⇒ L-beam are also called Edge Beam

⇒ It is always provided at the corner of the slab.

Flexural Analysis of T-BEAM:

Flexural Analysis of T-Beam consists of the following steps

• For finding the ultimate factored moment, we use the following formula.

$$M_u = \frac{w_u \times L^2}{8}$$

• Effective width (b_e) for T-Beam is calculated as:

$$1 - b (hf) + bw$$

$$2 - \frac{c}{6} \cdot \text{distance}$$

$$3 - \text{Span } 4$$

$$4 - \frac{CTs}{2} + bw$$

3 - Checking Whether Rectangular or T-Beam ^{Analysis}

(i) If $a > hf \rightarrow$ Special Analysis Required

(ii) If $a < hf \rightarrow$ Rectangular beam analysis is required

$a =$ Depth of compression block

$hf =$ Height of flange

4. For finding Area of Steel, we have to use

$$A_{st} = \frac{M_u}{\phi \times f_y \times (d - \frac{a}{2})}$$

where

$$a = \frac{A_{st} \times f_y}{0.85 \times f'_c \times bw}$$

5- For checking the range of Reinforcement ratio.

$$s_{max} = 0.85 \times \beta \times \frac{f'_c}{f_y} \times \left(\frac{\epsilon_u}{\epsilon_u + \epsilon_y} \right)$$

$$s_{min} = \frac{200}{f_y}$$

$$s = \frac{A_{st}}{b \times d}$$

Question NO 4

What is the difference b/w Case-I and Case-2 in the Design of T-Beam?

ANSWER:

Case - I

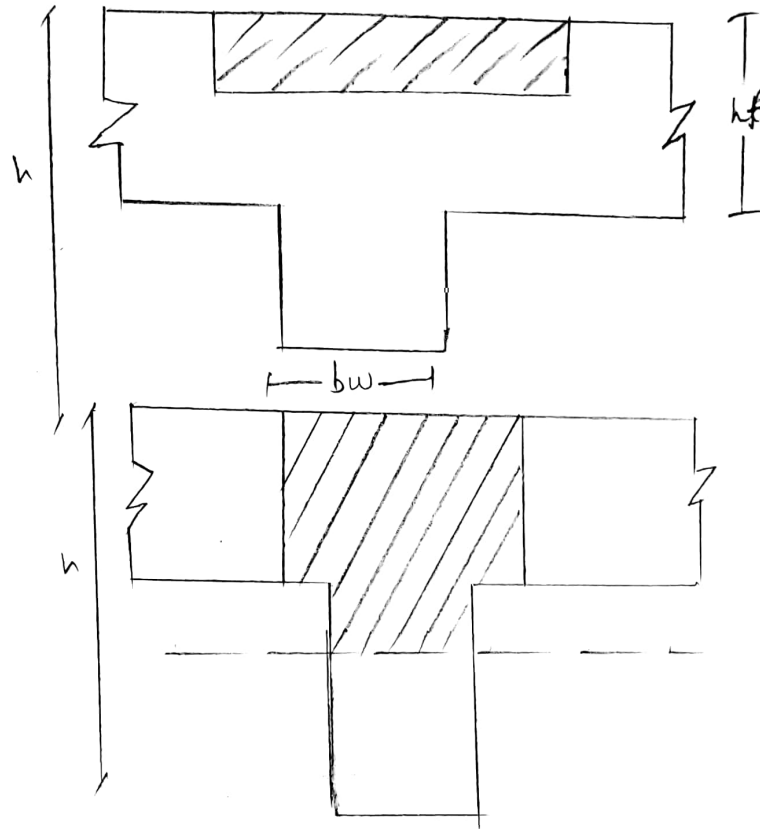
From the figure

$a < hf$

So in this case, Rectangular Beam Analysis is required so,

The Design moment formula will be

$$M_d = \phi \times f_y \times A_{st} \times (d - \frac{a}{2})$$



Case - II

From figure

$$a > h_f$$

So in this special beam analysis is required

So

the required Design moment-

$$M_d = \phi \times [A_s \times f_y \times (d - \frac{h_f}{2}) + (A_s - A_{st}) \times f_y \times (d - \frac{a}{2})]$$