

## Page # 1

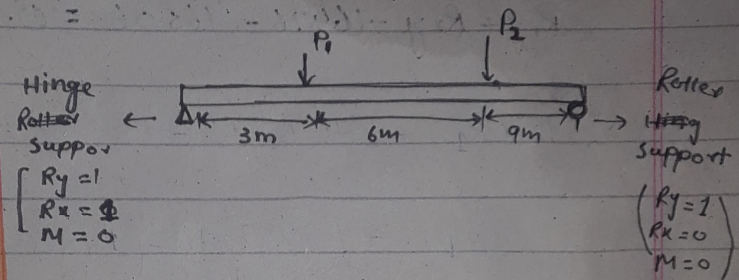
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## Page 2

Q 1

Find the support

Ans  $P_1 = 20 + 1D$  ;  $P_2 = 50 + 1D$

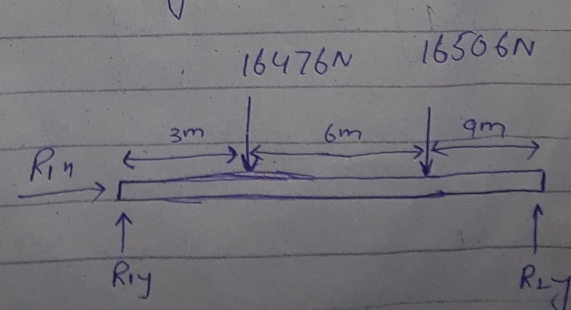


Solution

$$P_1 = 20 + (16456) = 16476N$$

$$P_2 = 50 + (16456) = 16506N$$

So, Diagram as:



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So,

$$R_1x = 0$$

$$\sum F_x = 0$$

we know that

$$R_{1y} + R_{2y} - 16476 - 16506 = 0 \rightarrow \text{eq 2}$$

$$18 \times R_{2y} - 16476 \times 15 = 16506 \times 9 = 0$$

$$18 \times R_{2y} - (247140) - (148554) = 0$$

$$18 \times R_{2y} - (395694) = 0$$

$$18 \times R_{2y} = 395694$$

$$R_{2y} = \frac{395694}{18}$$

$$R_{2y} = 21983$$

Put the value of  $R_{2y}$   
in eq no (2) for find

$R_{1y}$

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So,

$$R_{1y} + R_{2y} - 16476 - 16506 = 0$$

$$R_{1y} + (21983) - 16476 - 16506 = 0$$

$$R_{1y} + 21983 - (32982)$$

$$R_{1y} = 32982 - 21983$$

$$R_{1y} = 10999 \text{ N}$$

$$R_{2y} = 21983 \text{ N}$$

Ans

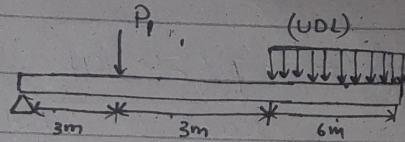
$$\rightarrow \text{Support \#1} = R_{1x} = 0$$

$$\rightarrow \text{Support \#2} = R_{1y} = 10999 \text{ N}$$

$$\rightarrow \text{Support \#3} = R_{2y} = 21983 \text{ N}$$

Q2

shear force.



$$P_1 = 100 + 1D, \quad P_2$$

$$UDL = 150 + 1D$$

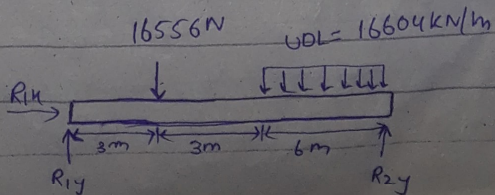
Solution:

$$P_1 = 100 + 16456 = 16556 \text{ N}$$

$$UDL = 150 + 16456 \text{ kN/m} = 16604 \frac{\text{kN}}{\text{m}}$$

Steps for find shear force:

① Find support reactions:



$$P_2 = UDL \times x$$

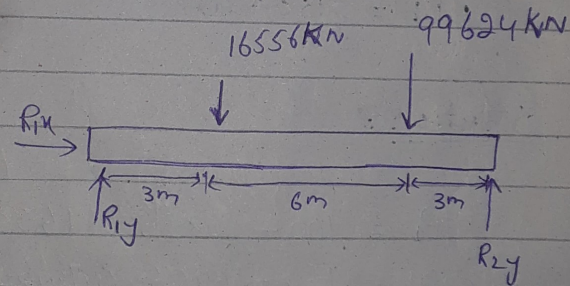
$$P_2 = 16604 \text{ kN/m} \times 6 \text{ m}$$

$$P_2 = 99624 \text{ kN}$$

react at middle

where the UDL react

so Diagram as:



so

$$R_{1x} = 0$$

$$\sum F_x = 0$$

$$R_{1y} + R_{2y} - 16556 - 99626 = 0 \quad \text{--- (1)}$$

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and

$$R_{2y} \times 12 - R_2 \times 9 - P_1 \times 3 = 0$$

$$R_{2y} \times 12 - (99624 \times 9) - (16556 \times 3) = 0$$

$$R_{2y} \times 12 - (896616) - (49668) = 0$$

$$R_{2y} \times 12 - 946284 = 0$$

$$R_{2y} = 946284 / 12$$

$$R_{2y} = 78857$$

Put the value of  $R_{2y}$  in eq (1)

$$R_{2y} + R_{1y} - 16556 - 99626 = 0$$

$$R_{2y} + R_{1y} - 116182 = 0$$

$$78857 + R_{1y} - 116182 = 0$$

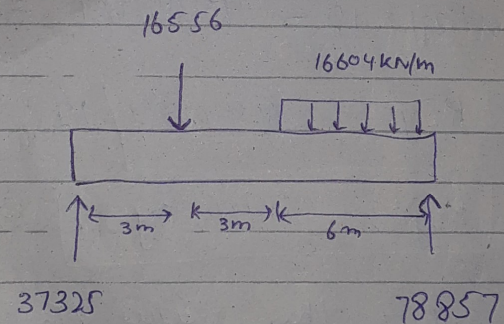
(4)

(6) (7)

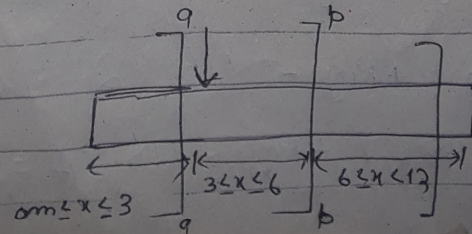
$$R_{1y} = 116182 - 78857$$

$$R_{1y} = 37325 \text{ kN}$$

$$R_{1y} = 37325 \text{ N}$$



step # 2: shear force at different section.



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Section a<sub>g</sub>

$$\sum f_y = 0$$

$$-v_{a9} + 37325 = 0$$

$$v_{a9} = 37325 \text{ eq (1)}$$

① aī x = 0m eq (1) v<sub>a9</sub> = 37325

② aī x = 3m v<sub>a9</sub> = 37325

Section b<sub>b</sub>

$$3 \leq x \leq 6$$

$$-v_{bb} - P_3 + 37325 = 0$$

$$v_{bb} = 37325 - 16556$$

$$v_{bb} = 20769 \text{ eq (2)}$$

① aī x = 3 =  $\overset{v_{bb}}{20769}$

aī x = 6 = v<sub>bb</sub> = 20769

99

aī

Section c<sub>c</sub>

$$6m \leq x \leq 12 \quad \text{UDL} = ?$$

$$P_2 = 16604x - 6$$

$$P = 16604x - 99624$$

$$\sum f_y = 0$$

$$-V_{cc} - P_2 + 37325$$

$$V_{cc} = -(16604(x-6)) + 37325$$

$$V_{cc} = -16604x + 99627 + 37325$$

$$V_{cc} = -16604x + 136952$$

① ~~-16604~~

① aī x = 6 v<sub>cc</sub> = -16604x + 136952

$$v_{cc} = 16604(6) + 136952$$

$$v_{cc} = -99624 + 136952$$

(10)

$$V_{CC} = -37328$$

$$\text{at } x = 12 \quad V_{CC} = ?$$

$$V_{CC} = -16604x + 136952$$

$$V_{CC} = -16604(12) + 136952$$

$$V_{CC} = -199248 + 136952$$

$$V_{CC} = -62296$$

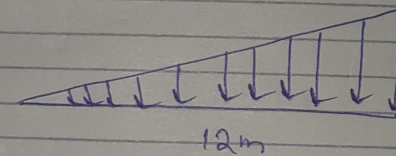
- |             |                             |
|-------------|-----------------------------|
| ① at $x=0$  | $V_{AA} = 37325$            |
| ② at $x=3$  | $V_{AA} = 37325$            |
| ③ at $x=3$  | $V_{BB} = 20769 \text{ N}$  |
| ④ at $x=6$  | $V_{BB} = 20769 \text{ N}$  |
| ⑤ at $x=6$  | $V_{CC} = -37328 \text{ N}$ |
| ⑥ at $x=12$ | $V_{CC} = -62296$           |

PE 13

Q3

Draw shear force and bending moment

shear force



$$UDL = 10/1000$$

$$UDL = 16456/1000 \text{ kN/m}$$

$$UDL = 16.4 \text{ kN/m}$$

$$P = U \times L$$

$$P = 16.4 \text{ kN/m} \times 12 \text{ m}$$

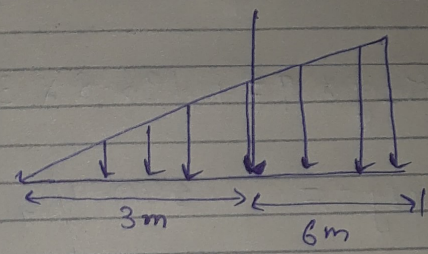
$$P = 196.8 \text{ kN}$$

This  $P$  act on one

(12)

3<sup>rd</sup> Distance from maximum

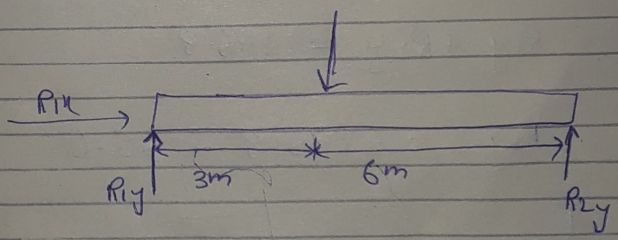
196.8 kN



Step # 1

find support reaction.

196.8



so,

$$R_{1x} = 0, \quad \sum F_x = 0$$

(13)

$$\Rightarrow R_{1y} + R_{2y} = 196.8 \quad \text{--- (1)}$$

$$R_{2y} \times 9 = 196.8 \times 3$$

$$R_{2y} = 590.4 / 9$$

$$R_{2y} = 65.6 \text{ kN}$$

put in eq (1)

$$R_{1y} + R_{2y} = 196.8$$

$$R_{1y} = 196.8 - 65.6$$

$$R_{1y} = 131.2 \text{ kN}$$

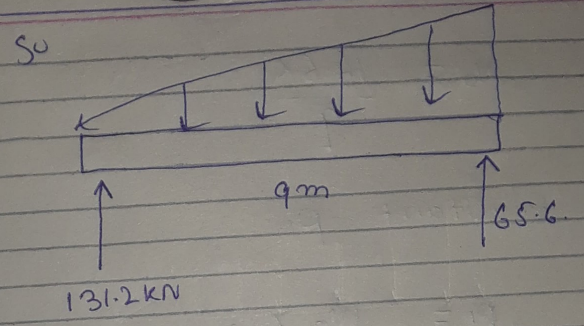
$$R_{1x} = 0 \text{ kN}$$

$$R_{1y} = 131.2 \text{ kN}$$

$$R_{2y} = 65.6 \text{ kN}$$

(14)

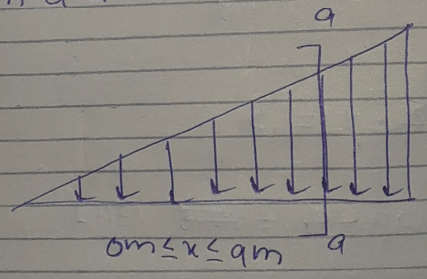
$w = 16.6$



Step # 2

Shear force at different section.

Section a-a



we know that

$$\frac{16.6 \text{ kN/m}}{9 \text{ m}} = \frac{w \text{ kN/m}}{x - m}$$

(15)

$$w_0 = \frac{16.6x}{9}$$

Resultant  $P_1$

$$P_1 = w_0 \times \frac{x}{2}$$

$$p = \frac{16.6x}{9} \cdot \frac{x}{2}$$

$$p = \frac{16.6x^2}{18}$$

so,

$$\sum f_y = 0$$

$$-v_{aa} - P_1 + 131.2$$

$$-v_{aa} - \left[ \frac{16.6x^2}{18} \right] + 131.2$$

$$v_{aa} = 16.6 = 16.6x$$



(16)

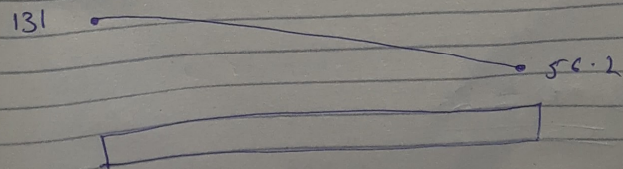
$$v_a = \frac{16.6x^2}{18} + 131.2 \quad \text{---} \times 2$$

step # 3

- ① at  $x=0m$        $v_a = 131.2 \text{ kn}$   
② at  $x=9m$        $v_a = 56.5$

$\frac{16.6(81)}{18} + 131.2$
$-74.7 + 131.2$
$56.5$

The graph as

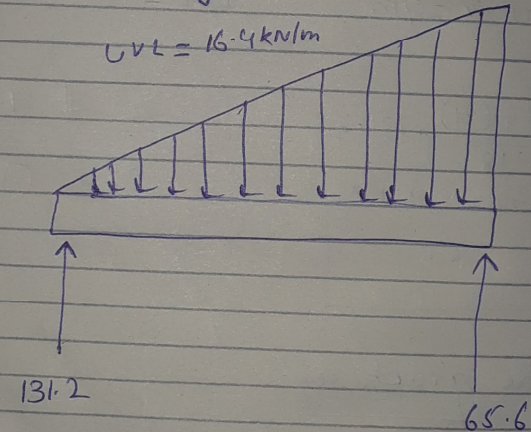


(17)

② bending moment.

Step 1

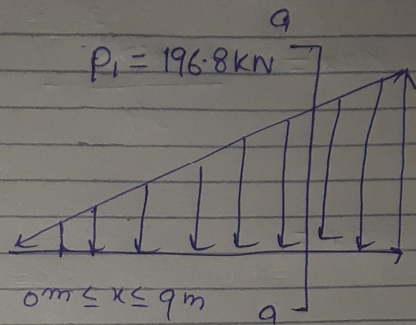
find support reaction  
was already calculated.



step # 2

shear force at different  
section.

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$$P_1 = \frac{16.6x^2}{18} \quad \text{which was already calculated.}$$

We know that the U/L will act at  $x/3$  of length from the maximum side.

So,

$$\sum M = 0$$

$$M_{aa} + x/3 P_1 - 131.2$$

$$M_{aa} = -x/3 P_1 + 131.2$$

$$M_{aa} = -\frac{x}{3} \left( \frac{16.6x^2}{18} \right) + 131.2$$

(19)

$$M_{aa} = \frac{-16.6x^3}{54} + 131.2$$

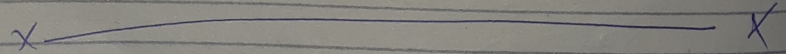
$$M_{aa} =$$

at section a-a.

Step # 03

① at  $x=0m$ ,  $M_{aa} = 0 \text{ kN-m}$

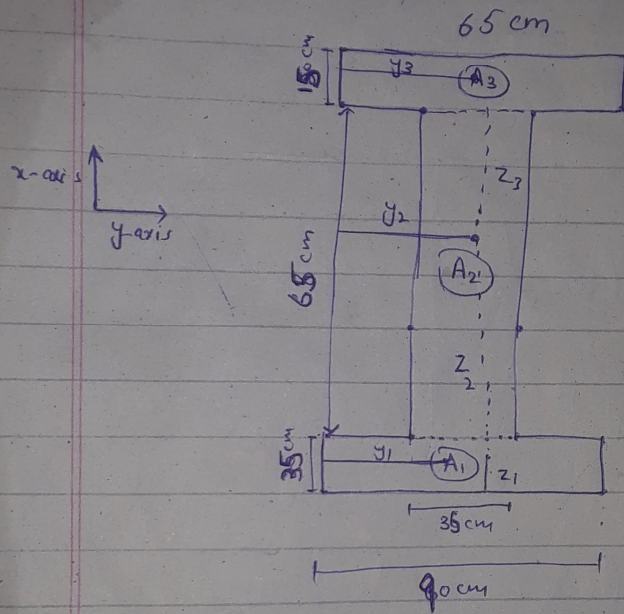
② at  $x=9m$  Put value left  
Time short



1102

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Q) find Centroid.



\* establish the Co-ordinate

\* divide the area into different simple area show in fig.

→ Area = L x W

$$A_1 = \frac{15}{100} \text{ m} \times \frac{90}{100} \text{ m} = .15 \times .9 = \boxed{.05 \text{ m}^2}$$

$$A_2 = \frac{65}{100} \text{ m} \times \frac{35}{100} \text{ m} = .65 \times .35 = \boxed{.1 \text{ m}^2}$$

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$$A_3 = \frac{65}{100} \text{ m} \times \frac{15}{100} \text{ m} = .65 \times .15 = .08 \text{ m}^2$$

\* Then find the Center point of each area from origin.

$$y_1 = \frac{90}{100} / 2 = \frac{.9}{2} = \boxed{.45 \text{ m}}$$

$$y_2 = \frac{35}{100} \text{ m} / 2 = \frac{.35}{2} = \boxed{.175 \text{ m}}$$

$$y_3 = \frac{65}{100} \text{ m} / 2 = \frac{.65}{2} = \boxed{.325 \text{ m}}$$

$$z_1 = \frac{35}{100} \text{ m} / 2 = \frac{.35}{2} = \boxed{.175 \text{ m}}$$

$$z_2 = .35 + \frac{80}{100} / 2 = .35 + .4 = \boxed{.75 \text{ m}}$$

$$z_3 = .35 + .8 + \frac{15}{100} / 2 = \boxed{1.15 \text{ m}}$$

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$$y_c = \frac{A_1 y_1 + A_2 y_2 + A_3 y_3}{A_1 + A_2 + A_3}$$

$$y_c = \frac{1.05(.45) + 1(.45) + .8(.345)}{1.05 + 1 + .8}$$

$$y_c = \frac{.4725 + .45 + .276}{2.85}$$

$$y_c = \frac{1.2825}{2.85}$$

$$y_c = .45 \text{ m}$$

$$z_c = \frac{A_1 z_1 + A_2 z_2 + A_3 z_3}{A_1 + A_2 + A_3}$$

$$z_c = \frac{.183(-.75) + 1(-.75) + .8(-1.15)}{1.05 + 1 + .8}$$

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$$z_c = \frac{.183 + .75 + .92}{2.85}$$

$$z_c = \frac{1.853}{2.85}$$

$$z_c = .6501 \text{ m}$$

(b)

(1)

moment of inertia.

$$I_y = bh^3/12$$

$$I_z = b^3h/12$$

so we find this as:

$$b = \frac{35}{100} = .175 \text{ m}$$

$$h = \frac{65}{100} = .325 \text{ m}$$

24(a)

put the value.

$$I_y = bh^3/12$$

$$I_y = \cdot 325 \cdot (385)^3 / 12$$

$$I_y = (\cdot 325)(\cdot 034) / 12$$

$$I_y = \cdot 015 / 12$$

$$I_y = \cdot 0012$$

$$I_z = b^3 h / 12$$

$$I_z = (\cdot 45)^3 (\cdot 65) / 12$$

$$I_z = (\cdot 091)(\cdot 65) / 12$$

$$I_z = \cdot 00493$$

24(b)

② Radius Gyration

$$r_y = \sqrt{\frac{I_y}{A}}, \quad r_z = \sqrt{\frac{I_z}{A}}$$

$$A = \frac{65}{100} \text{ m} \times \frac{35}{100} \text{ m}$$

$$A = \cdot 65 \times \cdot 35$$

$$A = \cdot 2275 \text{ m}^2$$

$$I_y = \cdot 0012$$

$$I_z = \cdot 00493$$

put in eq

$$r_y = \sqrt{\frac{\cdot 0012}{\cdot 2275}}$$

$$r_z = \sqrt{\frac{\cdot 00493}{\cdot 2275}}$$

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\* WORK \*

work can be define as, work is the product of force and displacement.

→  $w = f \cdot d$

→ Its unit is joule

→ 1 joule: a work is to be 1 joule if we exert one newton force on a body and it displace by one meter.

Example # 1

If we displace the block of 2m by 4N force, The work will be

$w = f \cdot s \Rightarrow 2(4) = 8j$

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\* Passitive work:

a work will be +ive if the body displace toward force.

Such as force exert on any object and it displace toward force

\* Negative <sup>work</sup> force:

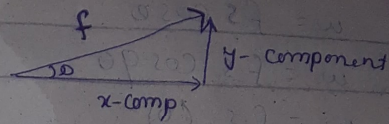
a work will be negative, if the body displace against the force such as - کرکری ذریعہ کوں سے پانی نکالنا

\* work done by force an angle:

We know that only the x-component of a force converted to work.

So, The x-component of a work calculated as.

(27)



$$f_x = f \cos \theta$$

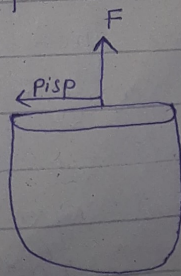
$$W = f s$$

$$W = f \cos \theta s$$

This is the equation of work when force exert at some angle.

∴ Example :

if we displace some a fallen pot of water, then, the angle b/w force and displacement is  $90^\circ$  so.



(28)

$$W = f \cdot s \cos \theta$$

$$W = f \cdot s \cos 90^\circ$$

$$W = f \cdot s (0)$$

$$W = 0$$

x ————— x

### \* Energy :

→ Energy is define as the ability of a body to do work.

when we say that a certain body has energy, we mean that it has the ability of external force on another body and of doing work on it

→ there are many type of energy

- ① - kinetic energy
- ② - gravitational P.E
- ③ - elastic energy

(29)

\* P.E and K.E are interconvertible.

→ when we throw an object to upper side, then its height increases, as a result the K.E changes to P.E.

at peak point, the K.E is zero and the P.E is maximum.

Science states that, energy can't be created nor destroyed, but it is transferred from one form to another. Like the above statement.

(30)

\* Power:

the rate at which work is done or the rate at which energy is transferred.

or

Example: He displaces the object by some force for several times.

Mathematically, it can be written as.

$$\rightarrow P = \frac{W}{t}$$

$$\rightarrow P = \frac{f \cdot s}{t}$$

$$\rightarrow P = f \cdot \frac{s}{t}$$

$$= P = fV$$



(31)

→ Power is ~~measured~~  
measured in watt but  
Time take in Second.

→ Power efficiency is the  
ratio of useful work  
done by the system, to  
that of the total work  
done

$$\text{Efficiency} = \frac{W(\text{useful})}{W(\text{Total})}$$

→ efficiency of power of  
any body must be  
less than 1 or 100%