



Mid Exam Summer

Submitted By:

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BS (SE-8) Section: A

Submitted To:

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Q1)

a) $45.25_{10} = (?)_2$

2		45
2		22 - 1
2		11 - 0
2		5 - 1
2		2 - 1
		1 - 0

Happened $45_{10} = 101101_2$

Now .25

0		.25
.		2
<hr/>		
0		5
*		2
1		0

$0.25_{10} = 0.01$

$= 101101_2 + 0.01_2$

101101.01_2

b)

$$0111111 \cdot 1010_2 = (?)_{10}$$

Solution:

$$\begin{aligned} 0111111 \cdot 1010_2 &= 0 \cdot 2^7 + 1 \cdot 2^6 + 1 \cdot 2^5 + 1 \cdot 2^4 + 1 \cdot 2^3 + 1 \cdot 2^2 + 1 \cdot 2^1 + 1 \cdot 2^0 \\ &= 0 + 64 + 32 + 16 + 8 + 4 + 2 + 1 + 0.5 + 0 \\ &= 127.625_{10} \end{aligned}$$

c) $3A6F_{16} = (?)_2$

Solution:

3	A	6	F
1	1	1	1
0011	1010	0110	1111

$$3A6F_{16} = (0011101001101111)_2$$

d) e) $-1_{10} = (?)_2$

Solution:

$$-1_{10} = (?)_2$$

$$\begin{array}{r|l} 2 & -1 \\ \hline & 0 \quad 1 \end{array} \quad \bullet \quad \text{1's complement}$$

$$\bullet (1) = (-1)_2$$

Digital Logic Design.

f) 156_{10}

Solution:-

$$156_{10} = (\quad)_{BCD}$$

$$\begin{array}{ccc} 1 & 5 & 6 \\ 0001 & 0101 & 0110 \end{array}$$

$$(156)_{10} = (000101010110)_{BCD}$$

d)

$$(10101010)_2 = (?)_{10}$$

Solution:-

$$(10101010)_2 = (\quad)_{10}$$

$$10101010$$

$$\begin{aligned} &= 1 \times 2^7 + 0 \times 2^6 + 1 \times 2^5 + 0 \times 2^4 + 1 \times 2^3 + \\ &0 \times 2^2 + 1 \times 2^1 + 0 \times 2^0 \\ &= 170 \Rightarrow (10101010)_2 = (170)_{10} \end{aligned}$$

$$g) \quad 1001010_2 = (?)_{\text{Gray}}$$

Solution:

$$1001010 = ?$$

$$g_6 = b_6 = 1$$

$$g_5 = b_6 \oplus b_5 = 1 \oplus 0 = 1$$

$$g_4 = b_5 \oplus b_4 = 0 \oplus 0 = 0$$

$$g_3 = b_4 \oplus b_3 = 0 \oplus 1 = 1$$

$$g_2 = b_3 \oplus b_2 = 1 \oplus 0 = 1$$

$$g_1 = b_2 \oplus b_1 = 0 \oplus 1 = 1$$

$$g_0 = b_1 \oplus b_0 = 1 \oplus 0 = 1$$

$$1001010_2 = (1101111)_{\text{Gray Code}}$$

$$h) \quad 111000 = (101001)_{\text{even parity}}$$

Solution:-

101001 is odd since its not divisible by 2,

As remainder is equal to 1, when divided by 2)

Answer# 2:

Q2

a) $9B_{16} + 8A_{16}$

Solution:

$$\begin{array}{r} \textcircled{1} \\ \textcircled{1} \quad 9 \quad B \\ + \quad 8 \quad A \\ \hline \quad \quad 2 \quad 5 \end{array}$$

$$\begin{aligned} 1) B_{16} + A_{16} &= 11_{10} + 10_{10} \\ &\Rightarrow 21_{10} \\ &= 16 \times 1 + 5 \Rightarrow 15_{16} \\ \text{Sum} &= 5, \text{ carry} = 1 \end{aligned}$$

$$\begin{aligned} 2) & \\ &= 1 + 9_{16} + 8_{16} \\ &= 1 + 9_{10} + 8_{10} \\ &= 18_{10} \Rightarrow 16 \times 1 + 2 \\ &= 12_{16} \\ \text{Sum} &= 2, \text{ carry} = 1 \end{aligned}$$

b) $F7_{16} - D6_{16}$

Sol.:

$$\begin{array}{r} F \quad 7 \\ - D \quad 6 \\ \hline 2 \quad 1 \end{array}$$

$$\begin{aligned} \therefore 7 - 6, 7 > 6 \\ 8_0, \Rightarrow 7 - 6 \Rightarrow 1_{16} \\ \therefore F - D, F = 15, D = 13 \\ \therefore 15 - 13 = 2_{16} \end{aligned}$$

c)

$$1100_2 + 1011_2$$

Sol:

$$\begin{array}{r} \textcircled{1} \quad 1 \quad 1 \quad 0 \quad 0 \\ + \quad 1 \quad 0 \quad 1 \quad 1 \\ \hline 0 \quad 1 \quad 1 \quad 1 \end{array}$$

1)

$$\therefore 0_2 + 1_2 \Rightarrow 0_{10} + 1_{10}$$

$$\Rightarrow 1_{10} = 1_2$$

$$\text{Sum} = 1$$

3)

$$\therefore 1_2 + 0_2 \Rightarrow 1_{10} + 0_{10}$$

$$\Rightarrow 1_{10} = 1_2$$

$$\text{Sum} = 1$$

2)

$$\therefore 0_2 + 1_2 \Rightarrow 0_{10} + 1_{10}$$

$$= 1_{10} \Rightarrow 1_2$$

$$\text{Sum} = 1$$

4)

$$\therefore 1_2 + 1_2 \Rightarrow 1_{10} + 1_{10}$$

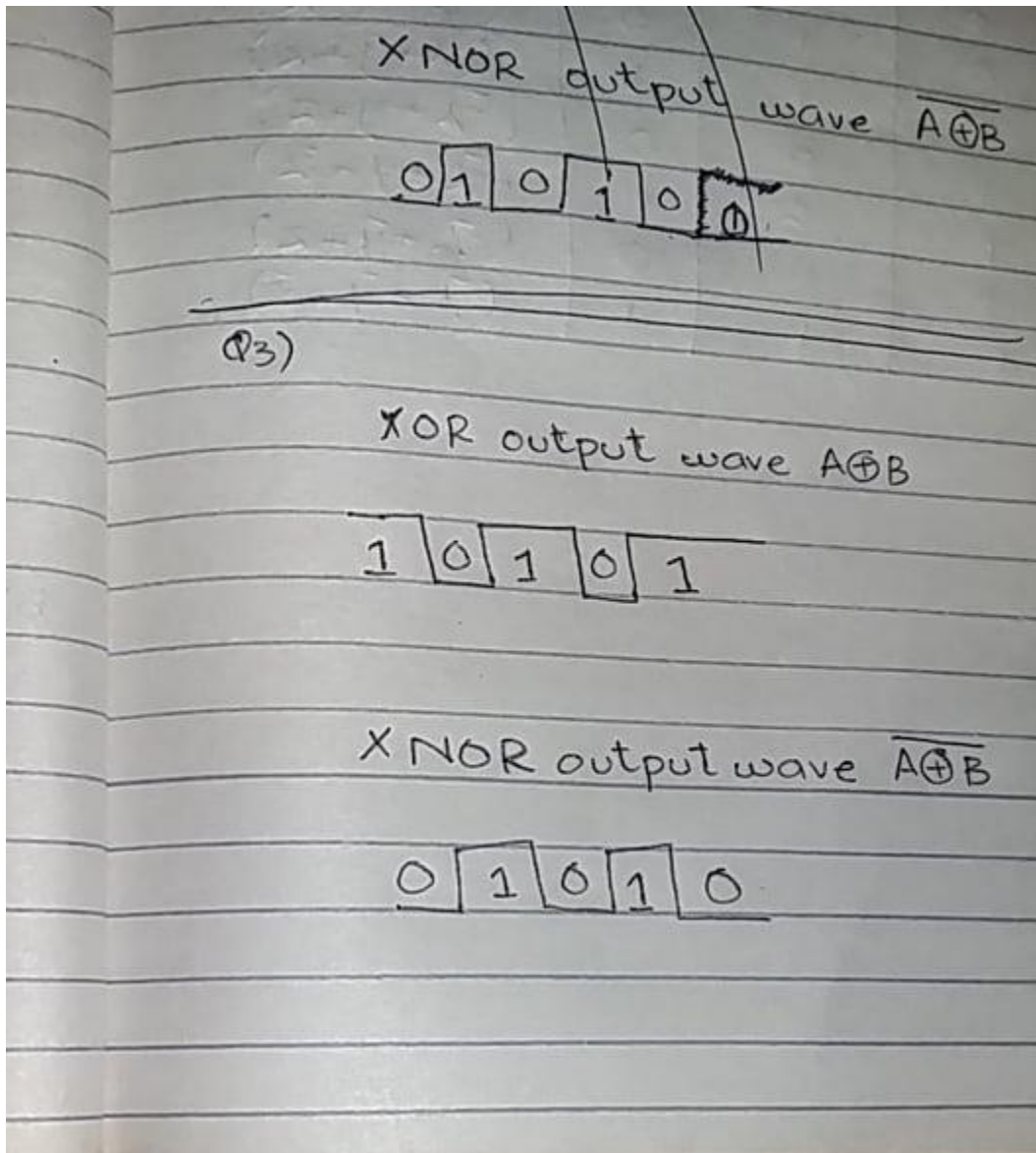
$$2_{10} \Rightarrow 2 \times 1 + 0$$

$$= 10_2, \text{Sum} = 0, \text{Carry}$$

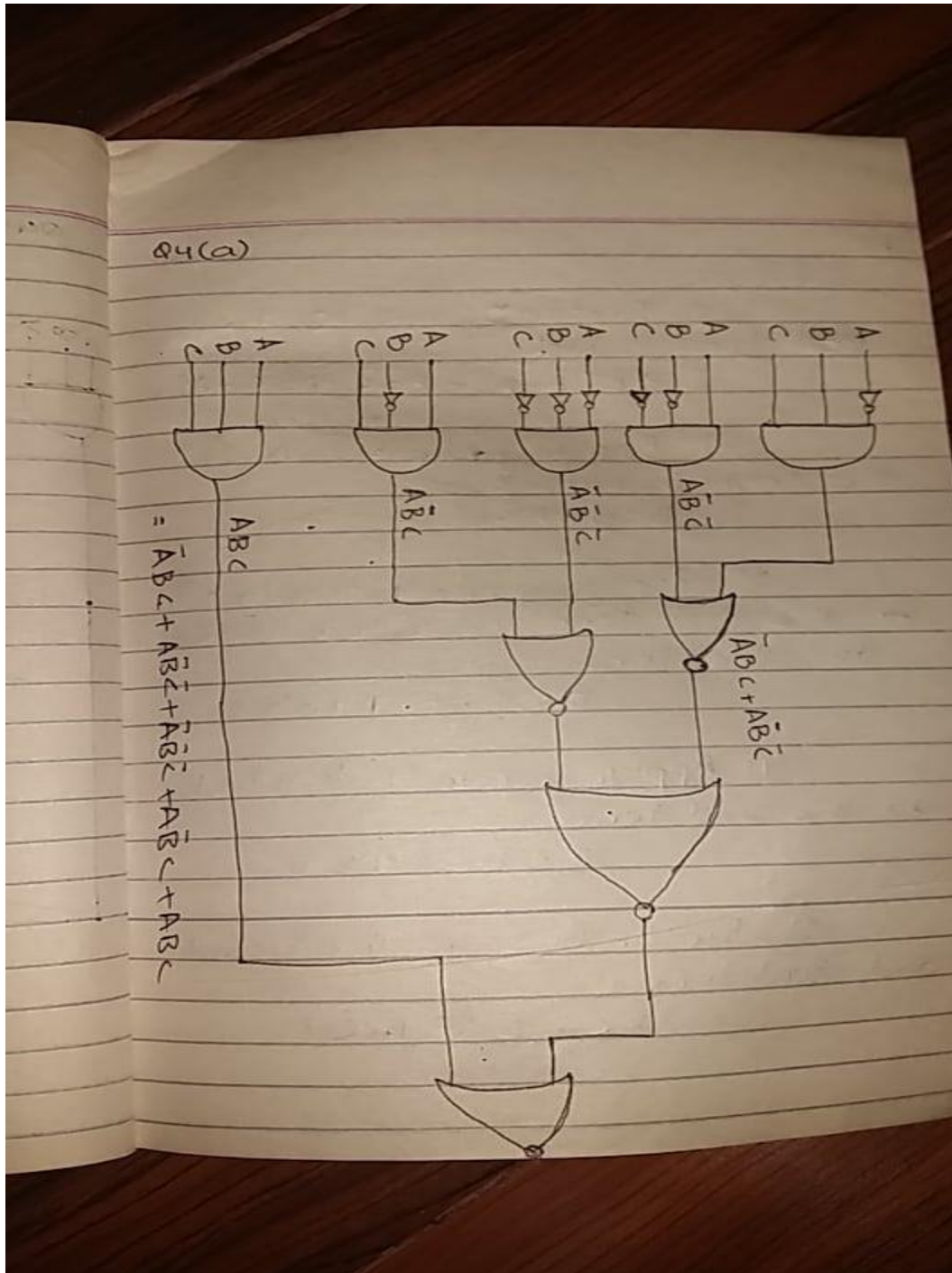
d) $01111111_2 - 00000111_2$

$$\begin{array}{r} \text{Sol:} \quad 01111111 \\ - \quad 00000111 \\ \hline 01111000 \end{array}$$

Answer# 3:



Answer# 4(A):



Answer# 4(B):

b)

Solution.

1) Factor BC out of the ~~first~~ first & last
 $BC(\bar{A}+A) + \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + \bar{A}B\bar{C}$

2) Applying rule b ($\bar{A}+A=1$) to the term in paranthesis
 $BC \cdot 1 + \bar{A}\bar{B}(\bar{C}+C) + \bar{A}B\bar{C}$

3) Applying rule 4 (drop the 1) to the first term and rule b ($\bar{C}+C=1$) to the term
 $BC + \bar{A}\bar{B} \cdot 1 + \bar{A}B\bar{C}$

4) Applying rule 4 (drop the 1) to the 2nd term
 $BC + \bar{A}\bar{B} + \bar{A}B\bar{C}$

5) Factor \bar{B} from the second and 3rd terms
 $BC + \bar{B}(A + \bar{A}\bar{C})$

6) Apply rule 11 ($A + \bar{A}\bar{C} = A + \bar{C}$) to the term in parenthesis
 $BC + \bar{B}(A + \bar{C})$

7) Use the distributive and commutative laws to get the following expressions:

$$BC + A\bar{B} + \bar{B}C$$

Q5

$$a) A = \overline{X+Y+Z}$$

Sol:-

$$A = \overline{\overline{\overline{X+Y+Z}}}$$

$$A = \overline{\overline{X} + \overline{Y} + \overline{Z}}$$

$$A = X \cdot Y \cdot Z$$

part(b)

$$A = XY\overline{Z}$$

There are total 8 combinations
the SOP contains 1 of these,
So the POS must contain the
other 7 which are

000, 010, 011, 100, 101, 110, 111

$$\begin{aligned} & (X+Y+Z)(X+\overline{Y}+Z)(X+\overline{Y}+\overline{Z})(\overline{X}+Y+Z) \\ & (\overline{X}+Y+\overline{Z})(\overline{X}+\overline{Y}+Z)(\overline{X}+\overline{Y}+\overline{Z}) \end{aligned}$$

part (C)

X	Y	Z	Expressions
0	0	0	$(x+y+z)$
0	0	1	$(x+y\bar{z})$
0	1	0	$(x+\bar{y}+z)$
0	1	1	$(x+\bar{y}+z)$
1	0	0	$(\bar{x}+y+z)$
1	0	1	$(\bar{x}+y+\bar{z})$
1	1	0	$(\bar{x}+\bar{y}+z)$
1	1	1	$(\bar{x}+\bar{y}+\bar{z})$

Q6(a)

$$X = \bar{A}\bar{B}\bar{C} + \bar{A}\bar{B}C + \bar{A}B\bar{C} + \bar{A}BC + A\bar{B}\bar{C} + A\bar{B}C + AB\bar{C} + ABC$$

AB \ C	0	1
00	1	0
01	1	1
11	0	1
10	0	1

$$X = ABC + A\bar{B}\bar{C} + A\bar{B}C + \bar{A}B\bar{C} + \bar{A}BC + \bar{A}\bar{B}\bar{C}$$

b)

AB \ C	0	1
00	0	1
01	0	0
11	1	0
10	1	0

$$X = (A+B+\bar{C})(\bar{A}+\bar{B}+C)(\bar{A}+B+C)$$

