

Q. Basic Assumption of Binomial Distribution

Ans. Binomial Distributions

Are that there is only one outcome of each trial that each trial has the same probability of success and each trial is mutually exclusive or independent of each other.

Binomial Random Distribution based on a fair coin

Suppose we have a fair coin so the head-on probability and we flip it n times if we let the random value x represent

the number of heads in the n tosses. Then clearly x is a discrete random variable and can take values

② Assumptions of Binomial Distribution

which is the generalised version of a fixed number of coin flips.

Here are the Assumptions of the Binomial Distribution that were listed in the lecture.

- ① There are fixed number of trials
- ② Each trial has 2 outcomes (Called success or Failure)
- ③ The trials are independent of one another.
- ④ The probability of success is the same for all trials.

Q2 (3)
 (i) If x is Binomially Distributed with 8 trials and probability of success fully $\frac{3}{4}$ at each attempt

(ii) Exactly 5 success (iii) At least one success

at Binomial Distribution,

$$n=8, \quad n=5$$

formula - $n=8, \quad p=\frac{3}{4}, \quad q=1-\frac{3}{4} \Rightarrow \frac{1}{4}$

$$P(5 \text{ Successes}) = {}^8C_5 \left(\frac{3}{4}\right)^5 \left(\frac{1}{4}\right)^{8-5}$$

$$\Rightarrow \frac{8!}{(8-5)! 5!} \cdot \left(\frac{3}{4}\right)^5 \left(\frac{1}{4}\right)^3$$

$$\frac{40320}{120} (0.75)^5 (0.25)^3$$

$$(336) (0.237) (0.028)$$

$$P = 0.63$$

at least one success

$$n=8, n=1$$

$$\rightarrow C_8^1 \left(\frac{3}{4}\right)^1 \left(\frac{1}{4}\right)^{8-1}$$

$$\Rightarrow \frac{8!}{(8-1)! 1!} \left(\frac{3}{4}\right)^1 \left(\frac{1}{4}\right)^7$$

$$\frac{40320}{5040}$$

$$(0.75)(0.2)^7$$

$$(8) (0.75) (0.0006125)$$

$$P_4 = 0.000768$$

Q32 ⑦ Z-TEST AND ANOVA

AND Z-TESTS A-Z TEST'S

Statistical test used to determine whether two population means are different. when the variances are known and the sample size is large. The test statistic is assumed to have a normal distribution and variance parameters such as standard deviation should be known in order for an accurate Z-test to be performed.

A Z-statistic or Z-score is a number representing how many standard deviations above or below the mean population a score derived from a Z-test is.

⑥ ANOVA TESTS

ANOVA is a statistical technique that assesses potential differences in a scale-level dependent variable by a nominal-level variable having two or more categories. The use of ANOVA depends on the research design. in three ways.

→ ONEWAY ANOVA A one way ANOVA has just one independent variable.

→ TWO WAY ANOVA A two way ANOVA is also called factorial ANOVA. ANOVA refers to an ANOVA using two independent variables.

⑦ N-WAY ANOVAS

A researcher can also use more than two independent variables and this is an n-way Anova with n being the number of independent variables you have.

Q32 part ⑤ write down the basic assumptions for chi-square test:

Ans: Chi-Square Test A chi-square test also test they can used statistical hypothesis test that is valid to perform when the test statistic is chi-square distributed. Under the null hypothesis, specific Pearson's chi-square test is an variants there of.

⑧ There are two types chi-square tests

* A chi-square goodness of fit test

if a sample data matches a population
For more details on this type
See goodness of fit test.

⑨ A chi-square test for independence

Compare two variables in a
contingency table to see if they
are related. In a more general

sense, it tests to see

whether distribution of categorical
variables differ from each other.

Q4x① The p.d.f of the ages of babies
 x years being brought to a post-natal
 clinic is given by

$$f(x) = \begin{cases} \frac{3}{4} \cdot \frac{3}{4} x(3-x) & 0 < x < 2 \\ 0 & \text{otherwise} \end{cases}$$

Solution (Eight months) = $\frac{2}{3}$ years. so

$$P(x < \frac{2}{3}) = \int_0^{\frac{2}{3}} \frac{3}{4} x(3-x) dx$$

$$= \frac{3}{4} \int_0^{\frac{2}{3}} (3x - x^2) dx$$

$$= \frac{3}{4} \left(\frac{3x^2}{2} - \frac{x^3}{3} \right) \Big|_0^{\frac{2}{3}}$$

$$= \frac{3}{4} \left(\frac{4}{9} - \frac{8}{81} \right) - (0)$$

$$= \frac{3}{4} \cdot \left(\frac{28}{81} \right) = \frac{7}{27} \Rightarrow 0.259$$

So The Expected number of
 babies under 8 months

- (10)
- Total Babies = 45
 - $45(0.259)$
 - 11.655

Q1 Students at multiple grade schools were asked what their personal goals (get good grades, be popular, be good at sports) was and how important having money were to them (1 very important and 4 least important). Do the data provide enough evidence to show that goals attainment and importance of money are independent in following give table test at 5% level.

| Goals | Importance of money | | | | Row Total |
|-------|---------------------|----|-----|-----|-----------|
| | 1 | 2 | 3 | 4 | |
| 1 | 14 | 34 | 71 | 128 | 248 |
| 2 | 14 | 29 | 35 | 63 | 141 |
| 3 | 6 | 12 | 26 | 44 | 90 |
| 4 | 34 | 75 | 132 | 239 | 478 |

11

| | E | $O - E$ | $(O - E)^2$ | $(O - E)^2 / E$ |
|----------|-----|---------|-------------|-----------------|
| 401 | 3 | 3 | 9 | 3.00 |
| 479 14 | 24 | 31 | 961 | 40.04 |
| pop 14 | 29 | 35 | 1225 | 42.24 |
| Sp0 6 | 12 | 26 | 676 | 28.00 |
| Total 24 | 75 | 132 | 2377 | 478 |

| 1 | 2 | 3 | 4 |
|--------|--------|--------|--------|
| 17.56 | 38.75 | 68.209 | 122.46 |
| 10.029 | 22.12 | 38.93 | 69.91 |
| 6.401 | 14.121 | 24.85 | 44.62 |

| Observed | Expected | $O - E$ | $(O - E)^2$ | $\frac{(O - E)^2}{E}$ |
|----------|----------|---------|-------------|----------------------------|
| 14 | 17.56 | -3.56 | 12.67 | 0.725 |
| 34 | 38.75 | -4.75 | 22.56 | 0.582 |
| 71 | 68.20 | 2.8 | 7.84 | 0.114 |
| 128 | 122.46 | 5.54 | 30.69 | 0.250 |
| 141 | 10.029 | 3.971 | 15.76 | 1.571 |
| 29 | 22.12 | 6.88 | 47.33 | 2.139 |
| 35 | 38.93 | -3.93 | 15.44 | 0.396 |
| 63 | 69.91 | -6.91 | 47.74 | 0.682 |
| 6 | 6.401 | -0.401 | 0.160 | 0.024 |
| 12 | 14.121 | -2.121 | 4.498 | 0.318 |
| 26 | 24.85 | -0.85 | 0.7225 | 0.326 |
| 46 | 44.62 | -1.38 | 1.90 | 0.042 |
| | | | | $\frac{\sum (O - E)^2}{E}$ |
| | | | | $\chi^2 = 6.822$ |

degree of freedom = (columns) \times (rows) - 1

$$(4-1) (3-1) = 3 \times 2 = 6$$

Significance level = 0.05

Tabular value is 12.59

$$\chi^2 \text{ tabular} = 12.59$$

$$\chi^2 \text{ Calculated} = \text{~~12.59~~ } 6.828$$

$$\chi^2 \text{ Calculated} < \chi^2 \text{ tabular}$$