

Name : Daniel
Alam

I.D : 15385

Subject : DHD

Degree : BS-SE

Assignment # 3

Q:1

Answer:

$$A + B + C + D = 0$$

When $A=0, B=0, C=0, D=0$

Ans

Q:2

Answer

$$A + B + C + D = 1$$

if either $A=1$ or $B=1$ or $C=1$ or $D=1$

Ans

Q:3

Answer

$$ABC = 0$$

if either $A=0$ or $B=0$ or $C=0$

Ans

Date _____

Q: 4

Answer

a) $0 + 0 + 0 + 1 = 1$ Ans

b) $1 \cdot 0 \cdot 1 \cdot 0 = 0$ Ans

c) $1 \cdot 0 + 1 \cdot 0 + 0 \cdot 1 + 0 \cdot 1$

$0 + 0 + 0 + 0 = 0$ Ans

Q: 5

Answer

a) $\bar{A} \bar{B} C = 1$

only if $A=0, B=0 \Rightarrow \bar{A}=1, \bar{B}=1, C=1$

Ans

b) $\bar{A} + \bar{B} + C = 0$

only if $A=1, B=1$

$\Rightarrow \bar{A}=0, \bar{B}=0, C=0$
Ans

Q: 6

Answer

a) $(ABC)(EFG) + (HIJ)(KLM)$

Solution: \rightarrow

$$(ABC)(EFG)(HIJ)(KLM) \Rightarrow \overline{A+B} = \overline{AB}$$

$$(ABC)(EFG)(HIJ)(KLM) \Rightarrow \overline{A} = A$$

$$= (\overline{A+B+C})(\overline{E+F+G})(\overline{H+I+J})(\overline{K+L+M})$$

$$\Rightarrow \overline{ABC} = \overline{A+B+C}$$

b) $(A+B)(C+D)(E+F)(G+H)$ Ans

Solution: \rightarrow

$$(A+B)(C+D)(E+F)(G+H) \Rightarrow \overline{A} = A$$

$$(\overline{A+B})(\overline{C+D})(\overline{E+F})(\overline{G+H}) \Rightarrow \overline{A+B} = \overline{AB}$$

Answer

Q: 7

Answer:

a) $= (AB) + C$
Answer

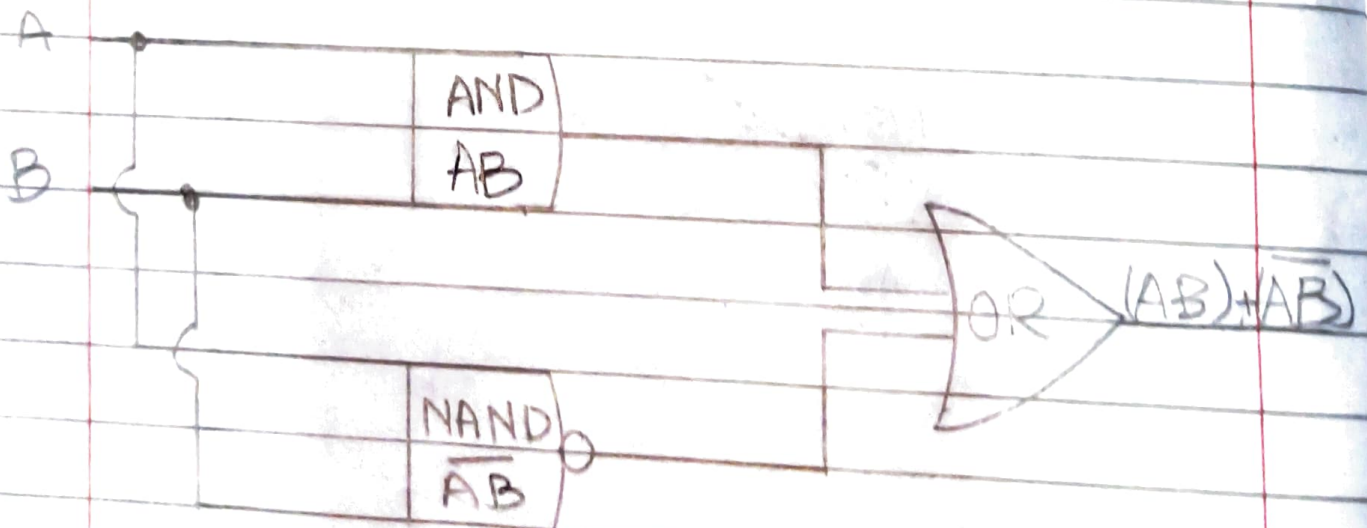
b) $= (\overline{A}B) \text{ or } (A + \overline{B})$

c) $= (A+B)C$
Ans

Ans

Q: 8

Answer



Date: _____

Q : 7

Answer

a)

ASSER

0



(LOW)

Ready

0



(LOW)

b)

LOAD

0



1

READY

Q. 19
Answer:

a) $A(A+B)$

$A(A+B) \Rightarrow$ Distributive law

$A+AB \Rightarrow AA=A$ (Rule 7)

$A \Rightarrow A+AB=A$ (Rule 10)

Ans

b) $A(A+\bar{A}B)$

$A(A+\bar{A}B) \Rightarrow A+\bar{A}B=A+B$ (Rule 11)

$AA+AB \Rightarrow$ Distributive law

$A+AB \Rightarrow$ Rule 7 $AA=A$

$A \Rightarrow$ Rule 10, $A+AB=A$

Ans

$$c) \quad BC + \overline{BC}$$

$$c) \Rightarrow A + \overline{A} = 1 \quad (\text{Rule 6})$$

$$c) \Rightarrow AA = A, \quad (\text{Rule 7})$$

Ans.

D. Just like part (B)

$$e) \quad \overline{ABC} + \overline{ABC} + \overline{ABC}$$

$$\overline{ABC} + \overline{ABC} + \overline{ABC} = \text{Recommuted.}$$

$$(A + \overline{A})(\overline{BC}) + \overline{ABC} = \text{Refactor } \overline{BC} \text{ (Distributive)}$$

$$1(\overline{BC}) + \overline{ABC} = A + \overline{A} = 1 \quad (\text{Rule 6})$$

$$\overline{BC} + \overline{ABC} = A \cdot 1 = A \quad (\text{Rule 9})$$

$$(\overline{A + B})C = \text{Refactor } C \text{ (Distributive)}$$

$$\overline{A}(\overline{+}BC) = \text{Distributive law.}$$

Ans.

$$\overline{B}C + (\overline{B} + C)D + BC$$

$$BC + (\overline{B} + C)D = BC + BC = BC$$

$$BC + \overline{B}D + CD = \text{Distributive laws}$$

$$BC + CD + \overline{B}D = \text{Rearranged}$$

$$BC + \overline{B}D = C + CD = C, \text{ Rule 10.}$$

$$BCD [\overline{BC} + \overline{D} (\overset{\text{Ans}}{CD + BD})]$$

$$BCD [BC + (CD\overline{D} + BD\overline{D})] \rightarrow$$

by distributive laws.

$$BCD [BC + (1) + B(0)] \Rightarrow D\overline{D} = 0 \text{ (Rule 8)}$$

$$BCD (B(1)) \Rightarrow A(0) = 0 \text{ (Rule 3)}$$

$$BCD \quad BC$$

$$BCD \Rightarrow (BC)(B) = BC$$

~~Ans~~

Date: _____

w/ $\bar{A}B + ABC + ABCD + ABCDE$

$\bar{A}B(1+C) + \bar{A}BCD + \bar{A}BCDE$ $\bar{A}B$ (common)

$\bar{A}B(1) + \bar{A}BCD + \bar{A}BCDE \Rightarrow 1+C=1$ (Rule 2)

$\bar{A}B(1+(D)) + \bar{A}B(CDE)$ $\bar{A}B$ (common)

$\bar{A}B(1) + \bar{A}B(CDE)$ $1+CD=1$ (Rule 2)

$\bar{A}B(1+(CDE))$ $\bar{A}B$ (common)

$\bar{A}B(1)$ $1+CDE=1$ (Rule 2)

$\bar{A}B$

Ans

Q = 13

Answer

a) = $[(\bar{C}\bar{D}) + B]A + \bar{A}B C = \bar{C}\bar{D}A + BA + \bar{A}B C$

b) = $(\bar{A}B) + (AC\bar{D}) + (\bar{A}B C) = (\bar{A}B) + (AC\bar{D})$

c) = $(\bar{C}\bar{D}\bar{B}) + \bar{A}B$

d) = $(\bar{A}B) + (AC\bar{D})$

~~a)~~ (b) and (d) are

equivalent.

Q: 14

Answer.

$$a) (C+D)(A+\bar{B}) (A+\bar{D})(C+\bar{D})$$

$$(A+C\bar{D}) \cdot DA+D\bar{D}$$

$$(C\bar{D}+CA+DA+D) \Rightarrow D\bar{D}=0 \text{ (Rule 8)}$$

$$C\bar{D}+AD(C+D) \Rightarrow \text{factor AD}$$

$$C\bar{D}+AD(C) = 1+C=1 \text{ (Rule 2)}$$

$$(CB) + (AD)$$

Ans

$$b) (A+C)(C\bar{D}+AC)$$

$$ACD+ACC+C\bar{C}D+ACC$$

$$ACD+\cancel{AC}+C\bar{D}+AC \Rightarrow AA=A \text{ (Rule 3)}$$

$$ACD+\cancel{AC}+AC+\bar{C}D$$

$$ACD+AC+C\bar{D} \Rightarrow AC+AC=AC$$

Date: _____

$$AC(1+D) + CD \Rightarrow \text{factor } AC$$

$$AC \cdot (1) + CD \Rightarrow 1+0=1 \text{ (Rule 2)}$$

$$(AC) + (CD)$$

Ans

$$4) B + C [BD + (C + \bar{D})E]$$

$$B + C [BD + (C + \bar{D})E] \text{ distributive law.}$$

$$B + C [BD + CE + \bar{D}E]$$

$$B + C [BE(D + \bar{D}) + CE] \Rightarrow A + \bar{A} = 1 \text{ (Rule 3)}$$

$$B + C (BE + CE)$$

$$B + C [CE(1+B)] \Rightarrow \text{factor } (C)$$

$$B + C [CE(1)] \Rightarrow 1+B=1 \text{ (Rule 3)}$$

$$B + C (CE)$$

$$B + C (CE) \Rightarrow \text{distributive law}$$

$$B + C (CE) \Rightarrow C(C) \text{ (Rule 7)}$$

Ans

d) $A(A\bar{D} + C)$

$A\bar{D} + AC \Rightarrow$ distributive law

$A\bar{D} + AC \Rightarrow A\bar{D} + A(C) = A(\bar{D} + C)$

e) $BC + DE(B\bar{C} + DE)$

$BC + DE(B\bar{C} + DE)$

$BC + DEB\bar{C} + DEDE \Rightarrow$ Distributive law

$BC + DEB\bar{C} + DEDE \Rightarrow DEDE = DE$ (Rule 7)

$BC + DE(C + B\bar{C})$ factor DE

$BC + DE(C) = 1 + B\bar{C} = 1$ (Rule 2)

$BC + DE$ Ans

f) $BC(\bar{C}\bar{D} + CE)$

$BC(\bar{C}\bar{D} + B(CE)) \Rightarrow$ distributive law

$B\bar{D}(\bar{C}) + BE(C) =$ Rearranged

$BD(0) + BE(C) \Rightarrow (\bar{C} = 0)$ (Rule 2)
 $(C = C)$ (Rule 7)

Date: _____

BCE Ans

Q: 15

Answer: →

$$a) \bar{C}\bar{D} + AD$$

CD is missing A

$$= \bar{C}\bar{D} = \bar{C}\bar{D}(A + \bar{A}) \Rightarrow \bar{C}\bar{D}A + \bar{C}\bar{D}\bar{A}$$

AD is missing C

$$= AD = AD(C + \bar{C}) \Rightarrow AD\bar{C} + AD\bar{C}$$

$$\bar{C}\bar{D}A + \bar{C}\bar{D}\bar{A} + AD\bar{C} + AD\bar{C}$$

~~Ans~~

$$b) (AC) + (CD)$$

AC is missing D

$$= AC = A(C + D) \Rightarrow AC\bar{D} + ACD$$

CD is missing A

$$= CD = C(DA + \bar{A}) \Rightarrow C\bar{D}A + CD\bar{A}$$

$$A(CD + A\bar{C}\bar{D}) + (CDA + CDA)$$

Ans

$$C \quad B + CE$$

B is missing & and E

$$= B = B(C + \bar{C}) = BC + B\bar{C}$$

$$\Rightarrow BC = BC(E + \bar{E}) \Rightarrow BC(E + B\bar{E})$$

$$\Rightarrow B\bar{C} = B\bar{C}(E + \bar{E}) \Rightarrow B\bar{C}(\bar{E} + B\bar{E})$$

CE is missing B

$$\Rightarrow CE = CE(B + \bar{B}) \Rightarrow CE(B + \bar{E}\bar{B})$$

$$BC(E + B\bar{E}) + B\bar{C}(\bar{E} + B\bar{E}) + (EB + \bar{E}\bar{B})$$

Ans

$$d/ \quad A\bar{D} + AC$$

$A\bar{D}$ is missing C

$$\Rightarrow A\bar{D} = A\bar{D}(C + \bar{C}) \Rightarrow A\bar{D}C + A\bar{D}\bar{C}$$

AC is missing D

$$\Rightarrow AC = AC(D + \bar{D}) \Rightarrow AC\bar{D} + ACD$$

$$A\bar{D}\bar{C} + A\bar{D}C + ACD + AC\bar{D}$$

Answer

$$e/ \quad BC + DE$$

BC is missing E and D

$$\Rightarrow BC = BC(D + \bar{D}) \Rightarrow BC\bar{D} + BCD$$

$$\Rightarrow BCD = BCD(F + \bar{F}) = BCD\bar{F} + BCFD$$

$$\Rightarrow BCD = BCD(E + \bar{E}) = BCD\bar{E} + BCDE$$

DE is missing BC

$$\Rightarrow DE = DE(B + \bar{B}) = DE\bar{B} + DEB$$

$$\Rightarrow DEB = DEB(C + \bar{C}) = DE\bar{B}C + DEB\bar{C}$$

$$\Rightarrow D\bar{E}\bar{B} = D\bar{E}B(C + \bar{C}) + D\bar{E}B\bar{C} + D\bar{E}B C$$

$$B\bar{C}D\bar{E} + B\bar{C}D\bar{E} + B\bar{C}D\bar{E} + B\bar{C}D\bar{E} + D\bar{E}B\bar{C} + D\bar{E}B C$$

$$+ D\bar{E}B\bar{C} + D\bar{E}B C$$

Ans

f) BCE

~~BCE is missing~~

BCE is in standard

SOP form

Q no 16

Answer.

$$a) C\bar{D}A + \bar{C}DA + ADC + AD\bar{C}$$

Sol

$$(C\bar{D}A + \bar{C}DA + A)(A + D + C)(A + D + \bar{C})$$

Ans

Solution: \rightarrow

$$(B + \overline{C} + D + E)(B + \overline{C} + D + \overline{E})(B + \overline{C} + \overline{D} + E)$$

$$(D + E + B + \overline{C})(D + E + B + C)(D + \overline{C} + \overline{E} + \overline{D})$$

$$(D + E + \overline{E} + \overline{C})$$

Answer.

f1 BCE

$$(B + \overline{C} + E)$$

Answer.

Date: _____

Q: 11

Answer

a)

A	C	D	X
0	0	0	0
0	0	1	0
0	1	0	0
0	1	0	0
1	0	0	1
1	0	1	1
1	1	0	1
1	1	1	1

\overline{ACD}

\overline{ACD}
 \overline{ACD}
 \overline{ACD}

b)

A	C	D	X
0	0	0	0
0	0	1	0
0	1	0	0
0	1	1	0
1	0	0	1
1	0	1	0
1	1	0	1
1	1	1	1

\overline{ACD}

\overline{ACD}
 \overline{ACD}

C	B	C	E	X	
0	0	0	0	0	
0	0	0	1	0	
0	1	0	0	0	
0	1	1	1	1	\overline{BCE}
1	0	0	0	1	\overline{BCE}
1	0	1	1	1	\overline{BCE}
1	1	0	0	1	\overline{BCE}
1	1	1	1	1	\overline{BCE}

A	C	D	X	
0	0	0	0	
0	0	1	0	
0	1	0	0	
0	1	1	0	
1	0	0	1	\overline{ACD}
1	0	1	0	
1	1	0	1	\overline{ACD}
1	1	1	1	\overline{ACD}

Q: 18

Answer.

a/

A	C	D	X	
0	0	0	0	$(A+C+D)$
0	0	1	0	$(A+C+D)$
0	1	0	0	$(A+C+D)$
0	1	0	1	
1	0	0	1	
1	0	1	0	$(A+C+D)$
1	1	0	1	
1	1	1	1	

b/

A	C	D	X	
0	0	0	0	$(A+C+D)$
0	0	1	0	$(A+C+D)$
0	0	1	1	
0	1	0	1	
0	1	0	0	$(A+C+D)$
1	0	0	1	
1	0	1	1	
1	1	0	1	
1	1	1	1	

c)

B	C	E	X	
0	0	0	0	$(B + C + E)$
0	0	1	0	$(B + C + E)$
0	1	0	0	$(B + C + E)$
0	1	1	0	$(B + C + E)$
1	0	0	0	$(B + C + E)$
1	0	1	1	
1	1	0	1	
1	1	1	1	

d)

A	C	D	X	
0	0	0	0	$(A + C + D)$
0	0	1	0	$(A + C + D)$
0	1	0	1	
0	1	1	0	$(A + C + D)$
1	0	0	1	
1	0	1	1	
1	1	0	1	
1	1	1	1	

Q. 10

Answer: \rightarrow

A	B	C	D	X	
0	0	0	0	1	$(\overline{A}\overline{B}\overline{C}\overline{D})$
0	0	0	1	1	$(\overline{A}\overline{B}\overline{C}D)$
0	0	1	0	0	$(\overline{A}\overline{B}C\overline{D})$
0	0	1	1	0	$(\overline{A}\overline{B}CD)$
0	1	0	0	0	$(\overline{A}B\overline{C}\overline{D})$
0	1	0	1	0	$(\overline{A}B\overline{C}D)$
0	1	1	0	0	$(\overline{A}BCL\overline{D})$
0	1	1	1	0	$(\overline{A}BCLD)$
1	0	0	0	0	$(A\overline{B}\overline{C}\overline{D})$
1	0	0	1	0	$(A\overline{B}\overline{C}D)$
1	0	1	0	0	$(A\overline{B}C\overline{D})$
1	0	1	1	0	$(A\overline{B}CD)$
1	1	0	0	0	$(A+B+\overline{C}+\overline{D})$
1	1	0	1	0	$(A+B+\overline{C}+D)$
1	1	1	0	0	$(A+B+C+\overline{D})$
1	1	1	1	0	$(A+B+C+D)$

Q : 20

ANSWER

Q/ $\overline{A}\overline{B}\overline{C} + \overline{A}B\overline{C} + A\overline{B}\overline{C}$

$000 \quad 001 \quad 101$

$(\overline{A}\overline{B}) + (A\overline{B}\overline{C})$

	C	
A \ B	0	1
0	0	0
0	0	1
1	1	0
1	0	0

~~AB~~

	C	
A \ B	0	1
0	0	1
0	1	0
1	1	0
1	0	1

b) $A C (\bar{B} + C) = A C \bar{B} + A C$

AC is missing B

$$= A C = A C (B + \bar{B}) \Rightarrow A C B + A C \bar{B}$$

$$= A C \bar{B} + A C B + A C \bar{B} \Rightarrow A C \bar{B} + A C B = A C B$$

$$= A C \bar{B} + A C B$$

$$= 110 \quad 111$$

AC \ B	0	1
0 0	0	0
0 1	0	1
1 0	1	0

$\Rightarrow A C$

Answer

Date: _____

c) $A(B\bar{C} + BC) + A(B\bar{C} + BC)$

$\bar{A}BC + \bar{A}\bar{B}\bar{C} + AB\bar{C} + ABC$

011 010 111 110

A	B	C	
0	0	0	0
0	1	1	1
1	1	1	1
1	0	0	0

= (B)

Answer

d) $\bar{A}\bar{B}\bar{C} + ABC + \bar{A}\bar{B}\bar{C} + ABC$

000 100 010 110

A	B	C	
0	0	0	0
0	1	1	0
1	1	1	1
1	0	0	0

= (C)

Ans

$$e/ A + BC + CD$$

A is missing BCD

$$A = 0 \quad A(B+B) = AB + A\bar{B}$$

$$A\bar{B} = AB(C+\bar{C}) = ABC + A\bar{B}\bar{C}$$



$$AB = AB(C+\bar{C}) = ABC + A\bar{B}\bar{C}$$

$$A\bar{B}\bar{C} = A\bar{B}\bar{C}(D+\bar{D}) = A\bar{B}\bar{C}D + A\bar{B}\bar{C}\bar{D} \text{ (1)}$$

$$ABC = ABC(D+\bar{D}) = ABCD + ABC\bar{D} \text{ (1)}$$

$$A\bar{B}\bar{C} = A\bar{B}\bar{C}(D+\bar{D}) = A\bar{B}\bar{C}D + A\bar{B}\bar{C}\bar{D} \text{ (1)}$$

$$A\bar{B}\bar{C} = A\bar{B}\bar{C}(D+\bar{D}) = A\bar{B}\bar{C}D + A\bar{B}\bar{C}\bar{D} \text{ (1)}$$

$B\bar{C}$ is missing AD

$$B\bar{C} = B\bar{C}(A+\bar{A}) = B\bar{C}A + B\bar{C}\bar{A}$$

$$B\bar{C}A = B\bar{C}A(D+\bar{D}) = B\bar{C}AD + B\bar{C}A\bar{D} \text{ (1)}$$

$$B\bar{C}\bar{A} = B\bar{C}\bar{A}(B+\bar{B}) = B\bar{C}\bar{A}B + B\bar{C}\bar{A}\bar{B} \text{ (1)}$$

CD is missing AB

Date: _____

$$AB = AB(1 + \bar{C}) = ABC + AB\bar{C}$$

$$ABC = ABC(D + \bar{D}) = ABCD + ABC\bar{D}$$

$$AB\bar{C} = AB\bar{C}(D + \bar{D}) = AB\bar{C}D + AB\bar{C}\bar{D}$$

$$= \bar{A}\bar{B}C\bar{D} + \bar{A}B\bar{C}\bar{D} + AB\bar{C}D + AB\bar{C}\bar{D} + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}\bar{C}\bar{D}$$

(011) (101) (0111) 1110 1001 (000)

$$+ \bar{A}B\bar{C}D + \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}D + \bar{A}B\bar{C}\bar{D}$$

$$+ \bar{A}B\bar{C}D + \bar{A}B\bar{C}\bar{D}$$

$$+ AB\bar{C}D + AB\bar{C}\bar{D} + B\bar{C}AD + B\bar{C}A\bar{D}$$

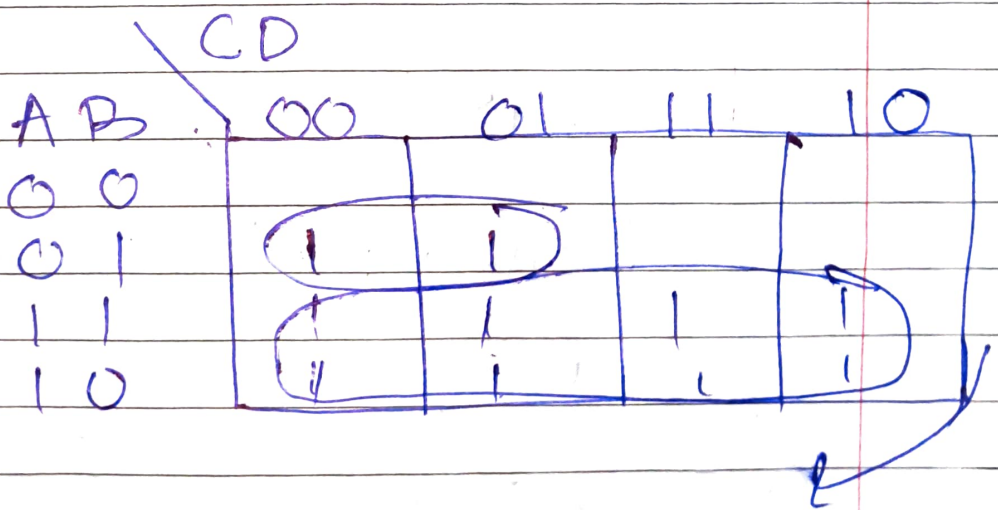
1101 1100 1011 1010

$$+ B\bar{C}AD + B\bar{C}A\bar{D} + AB\bar{C}D + AB\bar{C}\bar{D}$$

1001 1000 1110 1111

$$+ AB\bar{C}D + AB\bar{C}\bar{D}$$

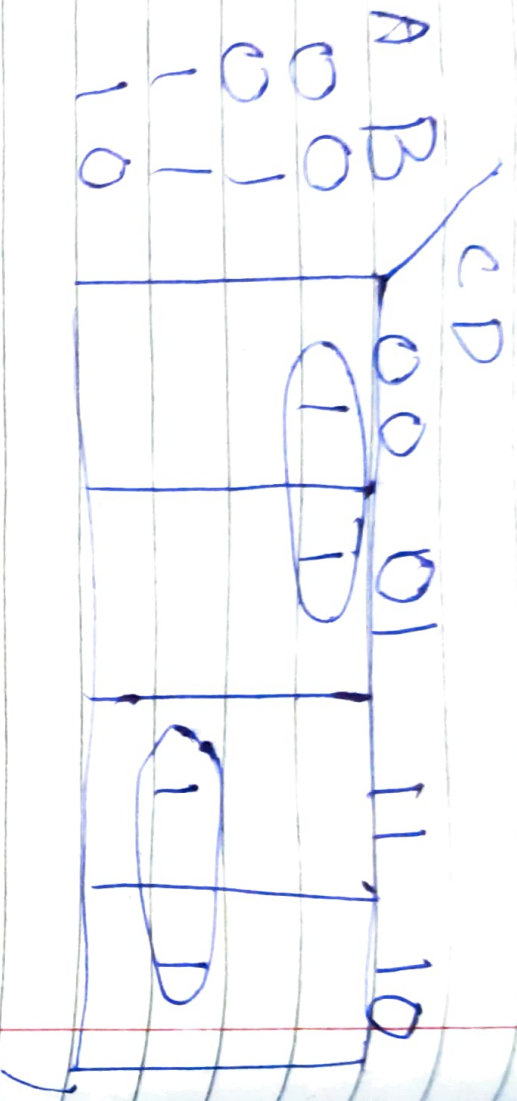
1101 1101



$$= (\bar{A}B) + (A)$$

Ans

$$\bar{A}B\bar{C}D + \bar{A}B\bar{C}D + \bar{A}B\bar{C}D + \bar{A}B\bar{C}D$$



$$= (\bar{A}B) + (AB)$$

g) $\bar{A}B + A\bar{B} + \bar{C}D + CD$

$\bar{A}B$ is missing CD

$$\bar{A}\bar{B} = \bar{A}\bar{B}(C+C) = \bar{A}\bar{B}C + \bar{A}\bar{B}\bar{C}$$

$$AB\bar{C} = \bar{A}\bar{B}\bar{C}(D+\bar{D}) = \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}\bar{C}\bar{D}$$

$$AB\bar{C} = \bar{A}\bar{B}\bar{C}(D+\bar{D}) = \bar{A}\bar{B}\bar{C}D + \bar{A}\bar{B}\bar{C}\bar{D}$$

$A\bar{B}$ is missing CD

$$\Rightarrow AB = AB\bar{C}D + AB\bar{C}\bar{D} + AB\bar{C}D + AB\bar{C}\bar{D}$$

$\bar{C}\bar{D}$ is missing AB

$$CD = AB\bar{C}D + \bar{A}B\bar{C}D + \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}\bar{D}$$

CD is missing AB

$$C\bar{D} = A\bar{B}C\bar{D} + \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}D + A\bar{B}C\bar{D}$$

$$= \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}C\bar{D}$$

$$+ \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}C\bar{D}$$

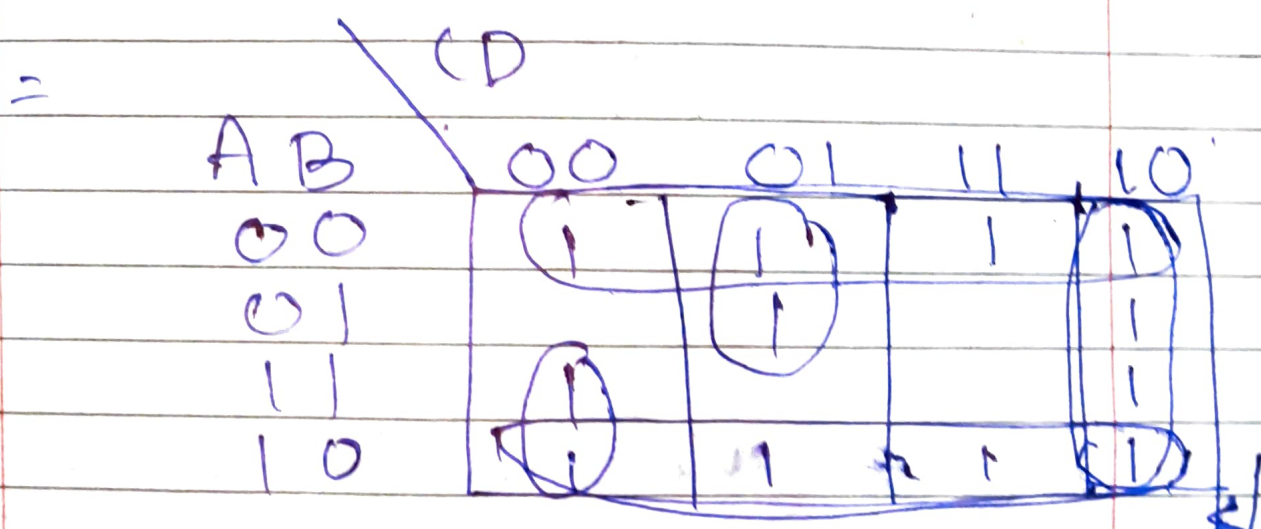
$$+ \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}C\bar{D}$$

$$+ \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}C\bar{D}$$

$$+ \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}C\bar{D}$$

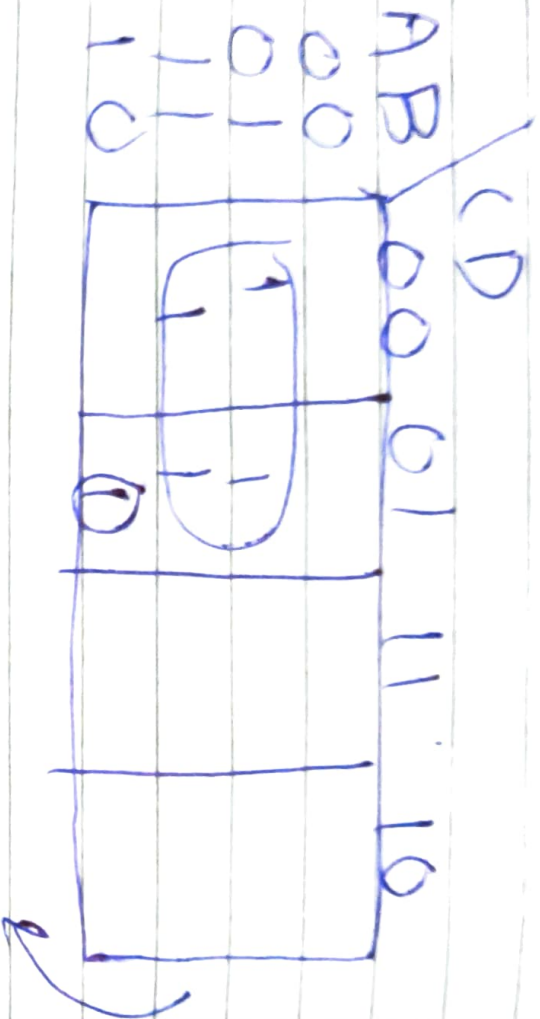
$$+ \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}C\bar{D}$$

$$1010 + 0010$$



$$= (\bar{A}\bar{B}) + (\bar{A}\bar{B}) + (\bar{A}\bar{B}) + (\bar{A}\bar{B})$$

$$\begin{aligned}
 h) & AB(C\bar{D} + \bar{C}D) + AB(\bar{A} + \bar{B} + \bar{C}D) + AB\bar{C}D \\
 & = AB\bar{C}\bar{D} + AB\bar{C}D + AB\bar{C}\bar{D} + AB\bar{C}D + AB\bar{C}D + AB\bar{C}D \\
 & \quad + AB\bar{C}D + AB\bar{C}D + AB\bar{C}D + AB\bar{C}D + AB\bar{C}D + AB\bar{C}D + AB\bar{C}D + AB\bar{C}D
 \end{aligned}$$



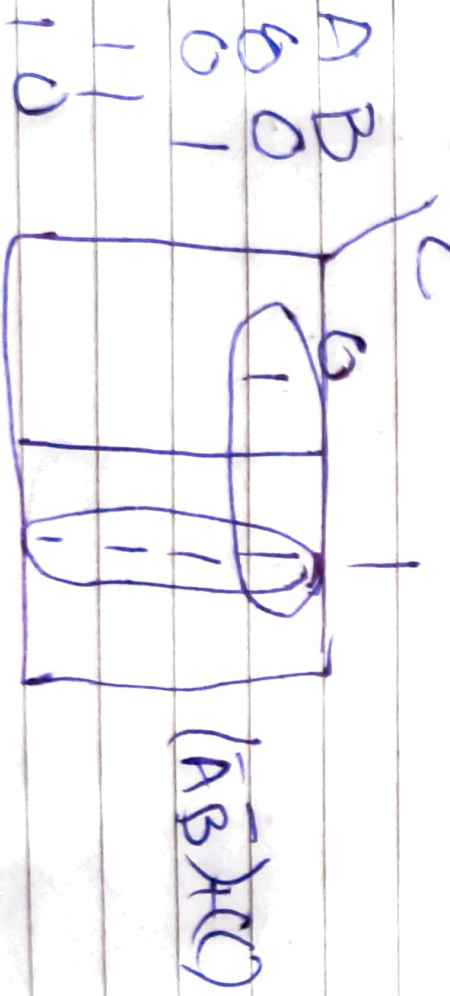
$$= (B) + (A\bar{B}\bar{C}D)$$

Ans

Q: 21

ANSWER

$$\begin{aligned}
 & (\bar{A}\bar{B}\bar{C}) + (\bar{A}\bar{B}C) + (\bar{A}B\bar{C}) + (\bar{A}BC) \\
 & \quad + (A\bar{B}\bar{C}) + (A\bar{B}C) + (AB\bar{C}) + (ABC)
 \end{aligned}$$



$$(\bar{A}\bar{B})\bar{C}$$

Q : 22

Answer

$$\begin{array}{r} \bar{A}\bar{B}C\bar{D} + \bar{A}\bar{B}C\bar{D} + \bar{A}B\bar{C}\bar{D} + \bar{A}B\bar{C}D \\ 0001 \quad 0010 \quad 0101 \quad 0111 \\ + A\bar{B}C\bar{D} + A\bar{B}C\bar{D} + ABC\bar{D} \\ 1000 \quad 1010 \quad 1100 \\ + AB\bar{C}D + ABCD \\ 1101 \quad 1111 \end{array}$$

AB \ CD	00	01	11	10
00		0		0
01			1	1
11	1	1	1	1
10	1			1

$$= (\bar{A}\bar{B}\bar{C}D) + (A\bar{C}\bar{D}) + (\bar{A}B)$$

$$+ (AB) + (A\bar{C}\bar{D}) + (A\bar{B}C\bar{D})$$

Ans

Q: → 23

Answer

$$\begin{matrix} (A+B+C) & (A+B+C) & (A+B+C) \\ 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{matrix}$$

~~$$\begin{matrix} A & B & C \\ 0 & 0 & 0 \\ 0 & 0 & 0 \\ 0 & 0 & 0 \end{matrix}$$~~

$$\begin{matrix} A & B & C \\ 0 & 0 & 0 \\ 0 & 0 & 0 \\ 1 & 1 & 0 \end{matrix}$$

0	0	1
---	---	---

$= (A+C) \overline{(AB)}$

Ans

$$P / (X + \bar{Y}) (X + 2) (X + Y + 2) (X + Y + 2)$$

$X + Y$ is missing Z

$$X + \bar{Y} = X + Y + (2Z) = (X + Y + 2)(X + Y)$$

$X + 2$ is missing Y

$$X + Z = X + 2 + (Y\bar{Y}) = (X + Y + 2)(\bar{Y} + Y + Z)$$

$$= (X + \bar{Y} + 2) (X + Y + 2) (X + Y + 2) (X + Y + 2)$$

$$0 \ 1 \ 0 \ 0 \ 1 \ 1 \ 1 \ 0 \ 0 \ 1 \ 1 \ 0$$

$$+ (X + \bar{Y} + 2) (\bar{X} + Y + 2)$$

$$1 \ 0 \ 0 \ 1 \ 1 \ 1 \ 1 \ 1 \ 0$$

$\sqrt{2}$

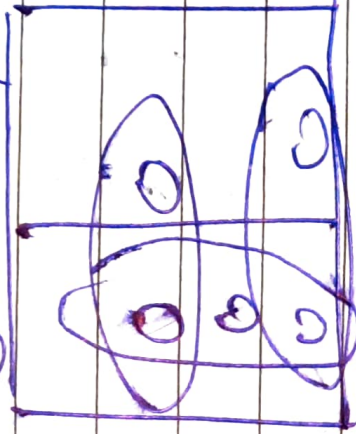
$$X \bar{Y} \ 0 \ 1$$

$$0 \ 0$$

$$0 \ 1$$

$$1 \ 1$$

$$1 \ 0$$



$$= (X + Y)(2)(X)$$

Ans

$$\text{of } A(B+C)(A+C)(A+B+C)(A+B+C)$$

AB is missing B+C

$$A = (A+B+C)(A+B+C)(A+B+C)(A+B+C)(A+B+C)$$

B+C is missing A

$$B+C = (A+B+C)(A+B+C)$$

$$= (A+B+C)(A+B+C)(A+B+C)$$

$$\begin{array}{ccc|ccc} 0 & 0 & 0 & 0 & 1 & 0 & 0 & 0 & 1 \end{array}$$

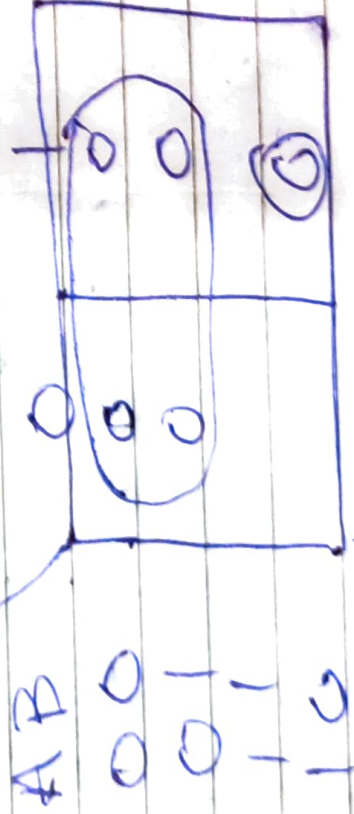
$$(A+B+C)(A+B+C)(A+B+C)$$

$$\begin{array}{ccc|ccc} 0 & 1 & 0 & 0 & 0 & 1 & 0 & 0 & 1 \end{array}$$

$$(A+B+C)(A+B+C)$$

$$\begin{array}{ccc|ccc} 0 & 1 & 0 & 0 & 1 & 0 & 0 & 1 \end{array}$$

C



$$= (A)(A+B+C)$$

Ans

Date: _____

Q: \rightarrow 24

Answer

$$(A+B+C) (\bar{A}+\bar{B}+C)$$

0	1	0	1	1	0
---	---	---	---	---	---

		C		
AB	0	0	1	
00				
01		⊗		
10		⊗		
11				

$\Rightarrow (A+\bar{B}+C)(\bar{A}+B)$

Ans

Q: \rightarrow 25

Answer

$$(A+B+(+D)) (A+B+(+D)) (A+B+(+D))$$

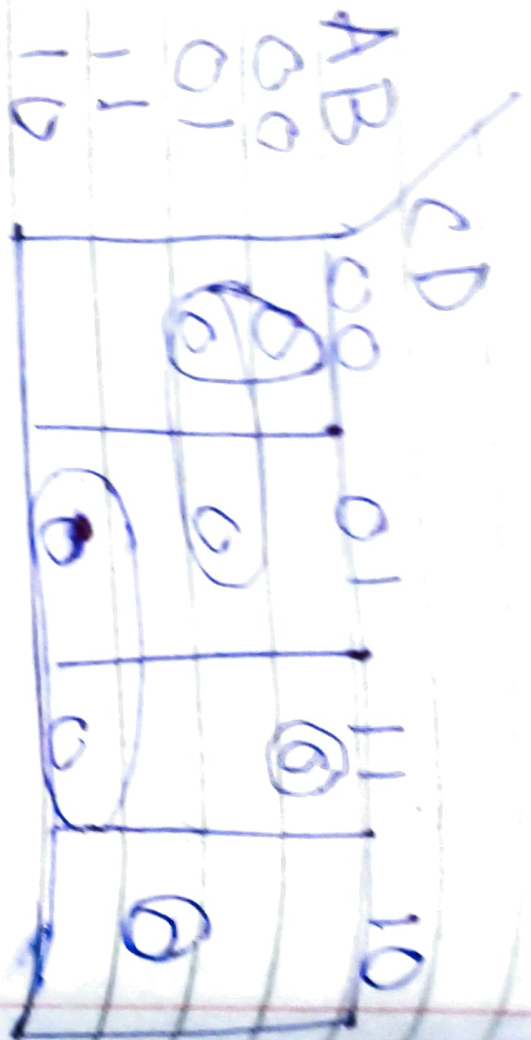
0	0	0	0	0	0	1	1	0	1	0	0
---	---	---	---	---	---	---	---	---	---	---	---

$$(A+B+(+D)) (A+B+(+D))$$

0	1	0	1	0	0	0	1	
---	---	---	---	---	---	---	---	--

$$(A+B+(+D)) (A+B+(+D))$$

1	0	1		1	1	1	0	
---	---	---	--	---	---	---	---	--



$$(A + C + D)(A + B + C)(A + B + C + D)$$

$$(A + B + C + D)(\bar{A} + B + D)$$

Ans

Q: 2b

Answer

Q1 $(A + \bar{B})(A + \bar{C})(\bar{A} + \bar{B} + C)$

$A + \bar{B}$ is missing C

$$A + \bar{B} = (A + \bar{B} + C)(A + \bar{B} + \bar{C})$$

$A + \bar{C}$ is missing B

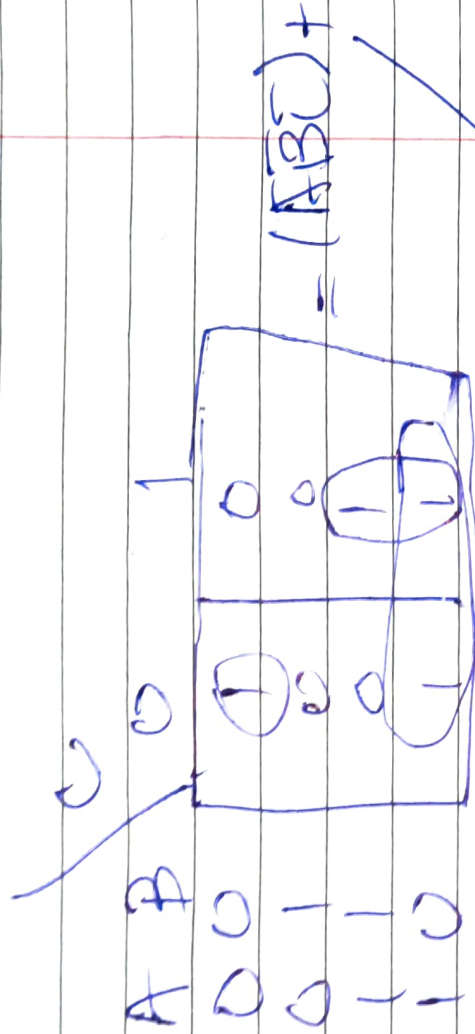
$$A + \bar{C} = (A + B + \bar{C})(A + \bar{B} + \bar{C})$$

Date: _____

$$(A + \bar{B} + C) (A + \bar{B} + \bar{C}) (A + B + C)$$

0	1	0	0	0	1
(A + \bar{B} + C)	(A + \bar{B} + \bar{C})	(A + B + C)			

$$0 \ 1 \ 1 \quad | \quad 1 \ 1 \ 0$$



$$(AC) + (AB)$$

Ans

b) $(\bar{A} + B) (\bar{A} + \bar{B} + \bar{C}) (B + \bar{C} + D)$

$(\bar{A} + \bar{B} + \bar{C} + \bar{D})$

$\bar{A} + B$ is missing (and)

$$\bar{A} + B = (\bar{A} + B + (C + D)) (\bar{A} + B + \bar{C} + \bar{D})$$

$$(\bar{A} + B + \bar{C} + \bar{D}) (A + B + \bar{C} + \bar{D})$$

$\bar{A} + B + \bar{C}$ is missing D

$$\bar{A} + \bar{B} + \bar{C} = (A + B + C + D)(\bar{A} + \bar{B} + \bar{C} + D)$$

B + C + D is missing A

$$B + C + D = (A + B + C + D)(\bar{A} + B + C + D)$$

$$= (A + B + C + D)(\bar{A} + B + C + D)$$

$$\begin{matrix} 1 & 0 & 0 & 0 & 1 & 0 & 1 & 0 \\ (A + B + C + D) & (\bar{A} + B + C + D) \end{matrix}$$

$$\begin{matrix} 0 & 0 & 0 & 1 & 1 & 0 & 1 & 1 \\ (A + B + C + D) & (A + B + C + D) \end{matrix}$$

$$\begin{matrix} 1 & 1 & 1 & 0 & 1 & 1 & 1 & 1 \\ (A + B + C + D) & (A + B + C + D) \end{matrix}$$

$$= (A + B + C + D)(\bar{A} + B + C + D)$$

$$\begin{matrix} 1 & 0 & 0 & 0 & 1 & 0 & 1 & 0 \\ (A + B + C + D) & (\bar{A} + B + C + D) \end{matrix}$$

$$\begin{matrix} 0 & 0 & 0 & 1 & 1 & 0 & 1 & 1 \\ (A + B + C + D) & (A + B + C + D) \end{matrix}$$

$$\begin{matrix} 1 & 1 & 1 & 0 & 1 & 1 & 1 & 1 \\ (A + B + C + D) & (A + B + C + D) \end{matrix}$$

$$\begin{matrix} 0 & 0 & 1 & 0 & 1 & 0 & 1 & 0 \\ (A + B + C + D) \end{matrix}$$

$$\begin{matrix} 0 & 1 & 1 & 1 \end{matrix}$$

Date: _____

AB		CD			
		00	01	11	10
00	00	1	0	1	0
00	01	1	1	0	0
11	01	0	1	0	0
11	10	0	1	0	0

$$= (\bar{A}\bar{C}\bar{D}) + (\bar{A}B\bar{C}D) + (BC\bar{D}) + (A\bar{C}D)$$

Ans